### A Quasi One-dimensional Simulation of a 4 Stroke Spark Ignition Hydrogen Fuelled Engine

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Abstract: Active research and development on hydrogen-fuelled engine had been done for few decades since hydrogen serves as a potential of infinite fuel supply. This paper discussed analytically and provides data on effects of compression ratio, equivalence ratio and spark timing of a hydrogenfuelled engine as a guideline for the engine design. The change in thermodynamic properties of the fuel was considered through the engine cycle. A modified version of Olikara and Borman method was presented to track the mole fraction of the equilibrium state of combustion products for hydrogen fuel. The equilibrium values of each species were used to predict the NO<sub>x</sub> formation, which is the main concern of study for hydrogen-fuelled engine.

**Key words:** Hydrogen, knock, NO<sub>x</sub>, spark ignition and Olikara and Borman

### INTRODUCTION

The rapid increasing world wide demand for the energy and the progressive depletion of fossil fuels has led to an intensive search for alternative fuels which can be produced on a renewable basis. Hydrogen becomes the right candidate due to its desirable characteristics such as clean burning, no unburned hydrocarbons, particulate matter, sulphur dioxide, smoke and etc. Hydrogen has wide range of flammability, low ignition energy, small quenching distance, high autoignition temperature, flame speed and diffusivity, which are suitable characteristics of as an engine fuel. However, these will bring the adverse effect in certain circumstances. The low ignition energy enables the conventional ignition system to be effective with a very low energy spark but at the same time it makes the system susceptible to surface ignition. Surface ignition is a highly undesirable combustion phenomenon because it precipitates flashback, pre ignition (knock) and rapid rate of pressure rise. The small quenching distance of hydrogen, makes the flame in a hydrogen-air mixture escapes more readily to the intake valve. Therefore, the fuel properties directly affect the engine design.

Descriptions of the mathematical model: The mathematical model was applicable in any types of fuels provided the fuel induction technique was used or in other words the carburetion system. The simulation is to predict the hydrogen gas inducted through the air inlet and serves as an alternative fuel to combust with fresh air. From the first law of thermodynamics, the open system can be define as

$$\Delta U = Q - W \tag{1}$$

Where the change of internal energy of a system is equal to the difference between the heat and work generated by the system. Taking the derivative of equation (1) yields

$$m\frac{du}{d\theta} + u\frac{dm}{d\theta} = \frac{dQ}{d\theta} - P\frac{dV}{d\theta} - \frac{\dot{m}_1 h_1}{\omega} \tag{2}$$

Where  $m_1$  is mass flow rate,  $h_1$  is enthalpy of the blowby masses, u is internal energy, o is heat transfer, p is pressure, V is volume,  $\theta$  is crank angle and  $\omega$  is the engine speed

Thermodynamic properties: Equation (2) shows that the thermodynamic properties change with respect to the crank angle, but at the same time the properties are also functions of temperature and pressure as well.

Table 1: Thermodynamics properties expression<sup>[1]</sup>

Specific internal energy 
$$u = u(T, P)$$
  $u = \frac{U}{m} = xu_b + (1-x)u_u$ 

Specific volume  $v = v(T, P)$   $v = \frac{U}{m} = xv_b + (1-x)v_u$ 

Specific entropy  $s_u = s(T_u, P)$  -

Specific enthalpy  $h = h(T, P)$  -

The subscript b&u represent the burned and unburned gas zone whereby x is the fraction between them. The entropy is only considered in the unburned gas zone since the unburned gas was treated as an open system losing mass due to leakage and during

combustion process. The specific heat change indicates the enthalpy change with respect to temperature and specific heat is obtained from curve fitted polynomial equation. Table 2 shows the thermodynamics properties expressed as a function of crank angle, pressure and temperature.

Table 2: Thermodynamic properties expressed as a function of crank angle and temperature<sup>[1]</sup>

Specific internal energy

$$\begin{split} \frac{du_b}{d\theta} &= \left(c_{Pb} - \frac{Pv_b}{T_b} \frac{\partial \ln v_b}{\partial \ln T_b}\right) \frac{dT_b}{d\theta} - v_b \left(\frac{\partial \ln v_b}{\partial \ln T_b} + \frac{\partial \ln v_b}{\partial \ln P}\right) \frac{dP}{d\theta} \\ \frac{du_u}{d\theta} &= \left(c_{Pu} - \frac{Pv_u}{T_u} \frac{\partial \ln v_u}{\partial \ln T_u}\right) \frac{dT_u}{d\theta} - v_u \left(\frac{\partial \ln v_u}{\partial \ln T_u} + \frac{\partial \ln v_u}{\partial \ln P}\right) \frac{dP}{d\theta} \end{split}$$

Specific volume

$$\begin{split} \frac{dv_b}{d\theta} &= \frac{v_b}{T_b} \frac{\partial \ln v_b}{\partial \ln T_b} \frac{dT_b}{d\theta} + \frac{v_b}{P} \frac{\partial \ln v_b}{\partial \ln P} \frac{dP}{d\theta} \\ \frac{dv_u}{d\theta} &= \frac{v_u}{T_u} \frac{\partial \ln v_u}{\partial \ln T_u} \frac{dT_u}{d\theta} + \frac{v_u}{P} \frac{\partial \ln v_u}{\partial \ln P} \frac{dP}{d\theta} \end{split}$$

Specific entropy 
$$\frac{ds_u}{d\theta} = \left(\frac{C_{p_u}}{T_u}\right) \frac{dT_u}{d\theta} - \frac{v_u}{T_u} \frac{\partial \ln v_u}{\partial \ln T_u} \frac{dP}{d\theta}$$

Specific enthalpy

$$\begin{split} \left(\frac{\partial h}{\partial T}\right)_p &= C_p \\ \frac{C_p}{R} &= a_1 + a_2 T + a_3 T^2 + a_4 T^3 + a_5 T^4 \end{split}$$

**Solution procedure:** Recalling equation (2) and combining all the derivatives will enable the pressure and temperature to be expressed as a function of crank angle, pressure, unburned gas temperature and burned gas temperature.

$$\frac{dP}{d\theta}, \frac{dT_b}{d\theta}, \frac{dT_u}{d\theta} = f_1(\theta, P, T_b, T_u)$$
(3)

Solving the above equations with appropriate input data enable determination of the indicated work, enthalpy and heat loss throughout the system since indicated work, enthalpy and heat loss can be expressed as a function of pressure and temperature as well.

$$\frac{dW}{d\theta} = f_4(\theta, P) \tag{4}$$

$$\frac{dQ_l}{d\theta} = f_5(\theta, P, T_b, T_u) \tag{5}$$

$$\frac{dH_{I}}{d\theta} = f_{6}(\theta, P, T_{b}, T_{u}) \tag{6}$$

The derivatives of equation (3–6) with the combination of the thermodynamic properties equations are:

$$\frac{dP}{d\theta} = \frac{A+B+C}{D+E} \tag{7}$$

$$\frac{dT_b}{d\theta} = \frac{-h\left(\frac{\pi b^2}{2} + \frac{4V}{b}\right)x^{1/2}\left(T_u - T_w\right)}{\omega mc_p x} +$$
(8)

$$\frac{v_b}{c_R} \frac{\partial \ln v_b}{\partial \ln T_b} \left( \frac{A + B + C}{D + E} \right) + \frac{h_u - h_b}{x c_R} \left[ \frac{dx}{d\theta} - \left( x - x^2 \right) \frac{C}{\omega} \right]$$

$$\frac{dT_u}{d\theta} = \frac{-h\left(\frac{\pi b^2}{2} + \frac{4V}{b}\right) (1 - x^{1/2}) (T_u - T_w)}{\omega m c_{P_u} (1 - x)} + \frac{v_u}{c_P} \frac{\partial \ln v_u}{\partial \ln T_u} \left(\frac{A + B + C}{D + E}\right)$$
(9)

$$\frac{dW}{d\theta} = P\frac{dV}{d\theta} \tag{10}$$

$$\frac{dQ_{l}}{d\theta} = \frac{h}{\omega} \left( \frac{\pi b^{2}}{2} + \frac{4V}{b} \right) \left[ x^{1/2} (T_{b} - T_{u}) + (1 - x^{1/2}) (T_{u} - T_{w}) \right]$$
(11)

$$\frac{dH_1}{d\theta} = \frac{Cm}{\omega} \left[ (1 - x^2) h_u + x^2 h_b \right]$$
 (12)

where

$$A = \frac{1}{m} \left( \frac{dV}{d\theta} + \frac{VC}{\omega} \right) \tag{13}$$

$$B = h \frac{\left(\frac{\pi b^{2}}{2} + \frac{4V}{b}\right) \left[\frac{v_{b}}{c_{P_{b}}} \frac{\partial \ln v_{b}}{\partial \ln T_{b}} x^{1/2} \frac{T_{b} - T_{w}}{T_{b}} + \frac{v_{u}}{c_{P_{u}}} \frac{\partial \ln v_{u}}{\partial \ln T_{u}} (1 - x^{1/2}) \frac{T_{u} - T_{w}}{T_{u}}\right]}$$
(14)

$$C = -(v_b - v_u)\frac{dx}{d\theta} - v_b \frac{\partial \ln v_b}{\partial \ln T_b} \frac{h_u - h_b}{c_b T_b} \left[ \frac{dx}{d\theta} - \frac{(x - x^2)C}{\omega} \right]$$
 (15)

$$D = x \left[ \frac{v_b^2}{c_{P_b} T_b} \left( \frac{\partial \ln v_b}{\partial \ln T_b} \right)^2 + \frac{v_b}{P} \frac{\partial \ln v_b}{\partial \ln P} \right]$$
 (16)

$$E = (1 - x) \left[ \frac{v_u^2}{c_{P_u} T_u} \left( \frac{\partial \ln v_u}{\partial \ln T_u} \right)^2 + \frac{v_u}{P} \frac{\partial \ln v_u}{\partial \ln P} \right]$$
 (17)

**Equilibrium combustion products:** In order to track  $NO_x$  formation, the equilibrium state of  $O_2$  and  $O_2$  need to be determined. Therefore, from the Olikara and Borman method, the chemical equilibrium of the combustion products can be determined by considering the dissociation effects of the  $O_1H_1OH_2NO_2$  species.

The general chemical formula is [1,2]:

$$\varepsilon\phi C_{\alpha}H_{\beta}O_{\gamma}N_{\delta} + (0.21O_{2} + 0.79N_{2}) \rightarrow v_{1}CO_{2}$$

$$+v_{2}H_{2}O + v_{3}N_{2} + v_{4}O_{2} + v_{5}CO + v_{6}H_{2} + v_{7}H + v_{8}O + v_{9}OH + v_{10}NO$$
(18)

However, in this case the C atom does not exist since the hydrogen fuel was being used. Thus, the chemical formula becomes:

$$\varepsilon \phi H_{\beta} O_{\gamma} N_{\delta} + (0.21O_{2} + 0.79N_{2}) \rightarrow y_{1} H_{2} O$$

$$+ y_{2} N_{2} + y_{3} O_{2} + y_{4} H_{2} +$$

$$y_{5} H + y_{6} O + y_{7} O H + y_{8} N O$$
(19)

Since atoms are conserved, three equations for the unknowns are obtained as below:

$$\varepsilon\phi\beta = (2y_1 + 2y_4 + y_5 + y_7)N\tag{20}$$

$$\varepsilon\phi\gamma + 0.42 = (y_1 + 2y_3 + y_6 + y_7 + y_8)N \tag{21}$$

$$\varepsilon\phi\delta + 1.58 = (2y_2 + y_8)N \tag{22}$$

Where, N is the total number of moles and y is the mole fraction. Thus, the total number of mole fraction must be equal to one and this gives:

$$\sum_{i=1}^{10} y_i - 1 = 0 (23)$$

The dissociation effect of O, H, OH, NO species gives the following five equations as listed in Table  $3^{[1]}$ .

Table 3: Equations to express the dissociation effect for distinct gases

gases	
$\frac{1}{2}H_2 \Leftrightarrow H$	$K_1 = \frac{y_5 P^{1/2}}{y_4^{1/2}}$
$\frac{1}{2}O_2 \Leftrightarrow O$	$K_2 = \frac{y_6 P^{1/2}}{y_3^{1/2}}$
$\frac{1}{2}H_2 + \frac{1}{2}O_2 \Leftrightarrow OH$	$K_3 = \frac{y_7}{y_3^{1/2} y_4^{1/2}}$
$\frac{1}{2}O_2 + \frac{1}{2}N_2 \Leftrightarrow NO$	$K_4 = \frac{y_8}{y_3^{1/2} y_2^{1/2}}$
$\boldsymbol{H}_2 + \frac{1}{2}\boldsymbol{O}_2 \Leftrightarrow \boldsymbol{H}_2\boldsymbol{O}$	$K_5 = \frac{y_1}{y_3^{1/2} y_4 P^{1/2}}$

Experimental data for  $K_1, K_2, K_3, K_4 \& K_5$  in the form of curve fits were then put into equations inside Table 3 for calculations<sup>[1]</sup>. Through algebraic manipulations, the nine equations can be reduced into four equations with four unknowns. The equations are

nonlinear and solved by using the Newton method. The general form of Newton method for nonlinear systems is

$$G(x) = x - A(x)^{-1} F(x)$$
(24)

Where, A(x) is the Jacobian matrix and F(x) is the functions and the functional iterations procedure evolves from

$$x^{(k)} = G(x^{(k-1)}) = x^{(k-1)} - J(x^{(k-1)})^{-1} F(x^{(k-1)})$$
 (25)

The solution is generally expected to give quadratic convergence, provided that a sufficiently accurate initial guess and the inverse of Jacobian matrix exist. Thermodynamic properties such as enthalpy, internal energy, entropy can be determined as the temperature and pressure change based on the concentrations of the 8 constituents. A modified version of the Olikara and Borman method for hydrogen fuel is presented in the Fig. 1 for investigation of distinct gas mole fraction as the temperature change. In order to validate the subroutine, the mole fraction change with respect to temperature of the Octane fuel based on the general chemical formula is compared with the diagram provided<sup>[1]</sup>. Good agreement was obtained.

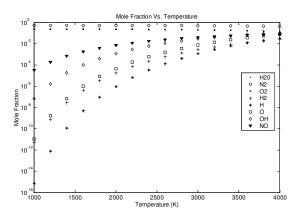


Fig. 1: Mole fraction vs. temperature data generated by the program@  $P = 50atm \& \phi = 0.8$ 

**The**  $NO_x$  **model:** The  $NO_x$  is the general term for the combination of NO and  $NO_2$ . In high temperature combustion e.g hydrogen gas with oxygen, the  $NO_x$  formation is the main concern since  $NO_x$  can brings the adverse effect to the environment. The mechanism of NO formation is expressed as the following:

$$O + N_2 = NO + N$$
  
 $N + O_2 = NO + O$   
 $N + OH = NO + H$ 

The rate of *NO* formation has strong temperature dependence and the reaction rate was expressed as:

$$\frac{d[NO]}{dt} = k_1^+[O][N_2] + k_2^+[N][O_2] + k_3^+[N][OH]$$

$$-k_1^-[NO][N] - k_2^-[NO][O] - k_3^-[NO][H]$$
(26)

Likewise for the *N* formation

$$\frac{d[N]}{dt} = k_1^+[O][N_2] - k_2^+[N][O_2] - k_3^+[N][OH]$$

$$-k_1^-[NO][N] + k_3^-[NO][O] + k_3^-[NO][H]$$
(27)

The [[N]] represents the mole concentration and  $k_i$  was the rate constant<sup>[3]</sup>. In most engine combustion cases, the steady state approximation for N formation  $\left(\frac{dN}{dt}=0\right)$  was considered to eliminate [N] since the concentration of [N] is approximately zero. Thus, equation (27) becomes

$$\frac{dNO}{dt} = 2k_1^+[O][N_2] \frac{1 - [NO]^2 / (K[O_2][N_2])}{1 + k_1^-[NO] / (k_2^+[O_2] + k_3^+[OH])}$$
(28)

From the assumption<sup>[3]</sup>, the post flame gases is much of concern in all in-cylinder combustion as the post flame gases always dominates the flame front gases, the concentrations of  $O, O_2, OH, H$  and  $N_2$  was assumed by their equilibrium values at local pressure and temperature. Thus, equation (28) becomes

$$\frac{d[NO]}{dt} = \frac{6x10^{16}}{T^{1/2}} \exp\left(\frac{-69090}{T}\right) [O_2]_{\epsilon}^{1/2} [N_2]_{\epsilon}$$
 (29)

Where,  $[O_2]_e$  and  $[N_2]_e$  is the equilibrium state of mole fraction obtain from the equilibrium combustion products model. Figure 2 shows the [NO] formation rate with respect to temperature for  $H_2$  fuel.

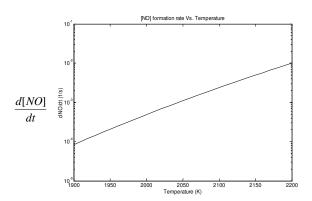


Fig. 2: The [NO] formation rate Vs. Temperature for  $H_2$  fuel

Equation (29) shows that the NO formation is highly dependent on temperature in the exponential

term. However, *NO* concentration will change as the time changes  $\left(\frac{d[NO]}{dt}\right)$ . Therefore, the characteristic

time for the NO formation process is defined as

$$\tau_{NO}^{-1} = \frac{1}{[NO]_e} \frac{d[NO]}{dt}$$
 (30)

and  $\tau_{NO}$  is given by

$$\tau_{NO} = \frac{8x10^{-16}T\exp(58300/T)}{p^{1/2}}$$
 (31)

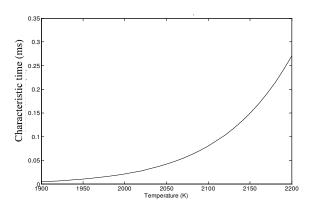


Fig. 3: The characteristic time vs. temperature

The characteristic time changes as the local temperature changes as shown in Fig. 3, but the pressure remains constant for the case of adiabatic constant pressure combustion, which is applicable for each element of fuel that burns in an engine. Figure 4 shows the variation of the [NO] mole fraction against characteristic time

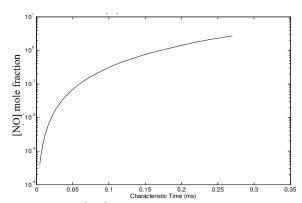


Fig. 4: The [NO] mole fraction vs. characteristic time

#### RESULTS

**Effects of equivalence ratio:** In order to simulate a realistic case, a Nissan A15 engine specification was used for the simulation study. This engine was applicable in gasoline, LPG and CNG fuels operation. The simulation is to predict the engine modifications

required for hydrogen fuel. Table 4 shows the specifications of the engine.

Table 4: Nissan A15 engine specifications

Specifications	
Intermittent output	46Hp @ 3,600rpm
Continuous output	39Hp @ 3,600rpm
Peak torque	11kg.m @ 2,200rpm
Minimum fuel consumption	225g/Hp.hr @ 3,200rpm
Cylinder arrangement	4 in line
Combustion chamber	Wedge shape
Bore x Stroke	76 x 82mm
Total piston displacement	1,487cc
Compression ratio	9:1

Figure 5 shows the result of IMEP and indicated thermal efficiency for different equivalence ratios. The simulation test was run at 3,600 rpm, which is the maximum output for gasoline fuel. This simulation helps to predict the best equivalence ratio to operate hydrogen-fuelled engine. The indicated mean effective pressure rises as the equivalence ratio increases, however it starts to drop from 0.6. Thermal efficiency starts to decrease exponentially as the equivalence ratio increases. For complete hydrogen-air combustion or a stoichiometric combustion, the air fuel ratio is 34.3, which means that hydrogen fuel operates better under an ultra-lean condition<sup>[4]</sup>. The thermal efficiency drop indicated the incomplete combustion of hydrogen-air mixture inside the combustion chamber. In this case, a 0.5 value of equivalence ratio was chosen for the following simulation since equivalence ratio of 0.6 gives a rather low thermal efficiency.

# IMEP & Thermal efficiency. Vs. Equivalence ratio

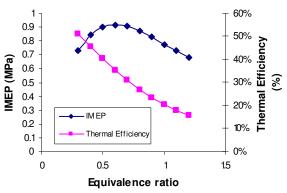


Fig. 5: IMEP and indicated thermal efficiency vs. equivalence ratio @ 3,600rpm

Effects of compression ratio: The engine default compression ratio was 9:1; however this should be changed to suit the hydrogen fuel operation. In order to predict the suitable compression ratio for hydrogen fuel, the simulation test was run at 0.5 equivalence ratio. Figure 6 shows the variation of IMEP and thermal efficiency with the compression ratio.

## IMEP & Thermal efficiency. Vs. Compression ratio

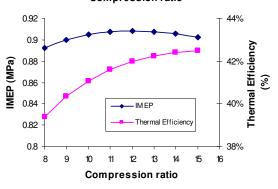


Fig. 6: IMEP and indicated thermal efficiency vs. compression ratio @3,600rpm &  $\phi = 0.5$ 

### IMEP & Thermal efficiency Vs. Spark Angle

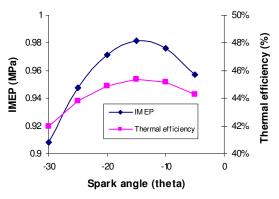


Fig. 7: IMEP & thermal efficiency vs. spark angle @3,600rpm,  $\phi = 0.5$  & CR=12

The results indicate that as the compression ratio increases, the indicated thermal efficiency start to increase exponentially but IMEP start to drop at compression ratio 12. Theoretically, compression ratio has a great effect on the terminal combustion pressure. The increase of compression ratio results in increase of cylinder top pressure as well as cylinder temperature. However, a high temperature and pressure environment may cause knock to happen inside the combustion chamber. Autoignition may occur as the compression ratio increase more than 12.

Effects of spark timing: Spark timing is a major operating parameter that affects spark ignition engine performance, efficiency and emissions at any given load and speed. If combustion starts too early in the cycle, the work transfer from the piston to the gases at the end of the compression stroke is too large. If the combustion starts too late, the peak cylinder pressure is reduced and the expansion stroke work transfer from the gas to the piston decreases. In order to optimize, the best results from the previous simulation were used and

the parameters were used as inputs for the following simulation to predict the optimum spark timing. Figure 7 shows the effect of spark timing on of the IMEP and thermal efficiency.

The results indicate that the best spark timing was at -15° BTDC since it gives the best IMEP and indicated thermal efficiency output. Hydrogen has low ignition energy but the autoignition temperature is high compared to gasoline<sup>[5]</sup>. Thus, hydrogen is hard to burn with air in a compression ignition engine. However, in this case the spark plug aids the ignition of the hydrogen-air mixture which solves the major problem<sup>[6,7]</sup>. As mentioned earlier, the ignition delay may cause the peak pressure to reduce which results in IMEP decrease since the work done through the control volume is less<sup>[8]</sup>.

Figures 8 and 9 shows the pressure history of the engine cycle where the maximum output pressure was expected to be 80MPa. Figures 10 and 11 show the temperature and heat flux for both burned and unburned gasses in the engine cycle. The heat flux was actually determined by making use of the temperature history in Figure 10 and applying the Newton's law. The IMEP variation with crank angle is shown in Fig. 12. The heat transfer and losses of the engine are shown in Fig. 13 and 14, respectively, where the adiabatic flame temperature is used as the initial temperature of the burned gas at the start of heat release. The temperature is then iteratively adjusted until the burned and unburned enthalpies are equal. Figure 15 shows the graphical user interface of the program.

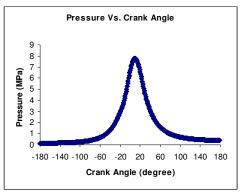


Fig. 8: Pressure vs. crank angle

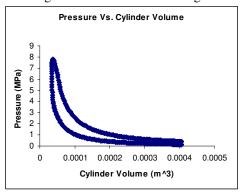


Fig. 9: Pressure vs. volume

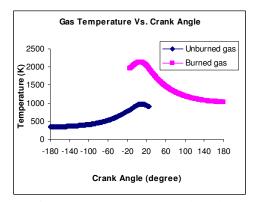


Fig. 10: Temperature vs. crank angle

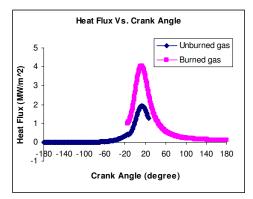


Fig. 11: Heat flux vs. crank angle

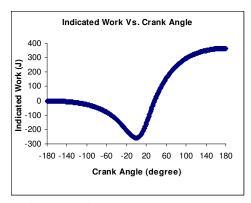


Fig. 12: Indicated work vs. crank angle

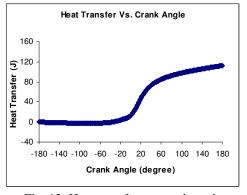


Fig. 13: Heat transfer vs. crank angle

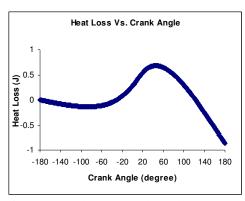


Fig. 14: Heat loss vs. crank angle

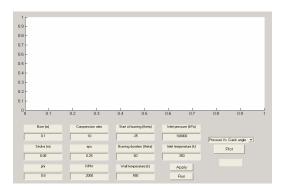


Fig. 15: The graphical user interface (GUI) of the program

### **CONCLUSION**

The mathematical model used to predict the engine performance for fuel inducted type spark ignition engine is presented. Based on the Olikara and Borman method, a subroutine for equilibrium combustion product was developed and compared with [1]. Good agreement was obtained. A model based on modified Olikara and Borman method for hydrogen fuel calculations was developed and the simulation result agreed well with those reported [1] with no carbon content exist. The  $NO_x$  model was developed based on the equilibrium combustion products of  $O_2$  and  $O_2$  and  $O_3$  species mole fraction at equilibrium state. The result of  $O_3$  formation rate was comparable with [3].

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