# Unusual high-frequency oscillations in the Kepler $\delta$ Scuti star KIC 4840675 

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#### Abstract

We show that the star KIC 4840675 observed by Kepler is composed of three stars with a rapidly rotating A-type star and two solar-type fainter companions. The A-type star is a $\delta$ Scuti variable with a dominant mode and many other modes of lower amplitude, including several low-frequency variations. The low-frequency variation with highest amplitude can be interpreted as rotational modulation with the light curve changing with time. However, the most interesting aspect of this star is a triplet of independent modes in the range 118-129 $\mathrm{d}^{-1}$ $(1.4-1.5 \mathrm{mHz})$, which is far outside the range of typical $\delta$ Scuti frequencies. We discuss the possibility that these modes could be solar-like oscillations, oscillations of the roAp type or due to an unseen pulsating compact companion.


Key words: asteroseismology - binaries: spectroscopic - stars: individual: KIC 4840675 stars: oscillations - stars: variables: $\delta$ Scuti.

## 1 INTRODUCTION

The $\delta$ Scuti ( $\delta$ Sct) variables are dwarfs or giants with spectral types between A2 and F5 and frequencies in the range $5-50 \mathrm{~d}^{-1}$. Most of the pulsational driving in these stars is by the $\kappa$ mechanism operating in the $\mathrm{He}_{\text {II }}$ partial ionization zone. In the cooler $\delta$ Sct stars the convective blocking mechanism (Guzik et al. 2000), which is the principal source of driving for the $\gamma$ Dor stars, also plays a significant role in driving the higher frequency p-modes (Dupret et al. 2005). The excited modes are radial or non-radial p modes or mixed modes of the p and g type. There is no known example of a star

[^0]with frequencies typical of $\delta$ Sct stars and also with the high frequencies associated with roAp stars. Most $\delta$ Sct stars do not pulsate at frequencies higher than about $50 \mathrm{~d}^{-1}$ (Balona \& Dziembowski 2011).

The Ap stars are slowly rotating, chemically peculiar A-F-type stars with non-uniform distributions of chemical elements, both laterally across the surface and vertically in the atmosphere. The chemical peculiarity is thought to be due to diffusion of elements in a strong magnetic field (Michaud 1970). The axis of the magnetic field in these stars is tilted with respect to the axis of rotation. A small number of the cooler Ap stars have been found to pulsate with periods of $3-24 \mathrm{~min}$ (frequencies of $60-500 \mathrm{~d}^{-1}$ or $0.7-5.5 \mathrm{mHz}$ ). These are the roAp stars (Kurtz 1982). The mechanism that drives the pulsations is not known, but could be the $\kappa$ mechanism operating in the H ionization zone in regions of the star where convection has been suppressed (Balmforth et al. 2001). It is thought that diffusion in the strong magnetic field of an Ap star will deplete He from the driving zone which therefore tends to suppress the $\delta$ Sct pulsations. Energy losses from magnetoacoustic coupling also tend to dampen
these modes in Ap stars (Saio 2005). However, the Ap star HD 21190 (F2III SrEuSi) does pulsate with a frequency of $6.68 \mathrm{~d}^{-1}$ and other pulsation modes are probably present (Koen et al. 2001). The star is the most evolved Ap star known which may be a clue to why it pulsates.
Space missions, such as MOST, CoRoT and Kepler, have been extremely successful in extending our understanding of stellar pulsations. KIC 4840675 (2MASS J19325792+3958452; RA $=$ $19^{\mathrm{h}} 32^{\mathrm{m}} 58^{\mathrm{s}}$, Dec. $=+39^{\circ} 58^{\prime} 45^{\prime \prime}$, J2000) has been observed by the Kepler satellite and listed as a $\delta$ Sct variable by Uytterhoeven et al. (2011). There is no spectral type or spectroscopy of any kind available from the literature. The Kepler Input Catalog (KIC; Brown et al. 2011) lists the following values: $\mathrm{Kp}=9.67 \mathrm{mag}, T_{\text {eff }}=7100 \mathrm{~K}$, $\log g=3.55$ and $[\mathrm{Fe} / \mathrm{H}]=-0.2$. Recently, Pinsonneault et al. (2012) have re-examined the KIC temperature scale and found that the KIC temperatures are too low by about 100 K , but this result applies to stars with effective temperatures in the region $6000-7000 \mathrm{~K}$. The KIC effective temperature for KIC 4840675 may also be somewhat too cool. We will show that the star has multiple components which in any case renders the photometric temperature rather unreliable.
In addition to pulsations typical of $\delta$ Sct stars, the periodogram of this star shows a few low-amplitude peaks at around $120 \mathrm{~d}^{-1}$ ( $1300 \mu \mathrm{~Hz}$ or periods of about 12 min ). Such high-frequency peaks are unknown in any other $\delta$ Sct star. In some $\delta$ Sct stars, harmonics of a dominant mode sometimes do have frequencies approaching this value, but these are not independent modes. The presence of such high-frequency peaks in a $\delta$ Sct star calls to mind the possibility that it might be an Ap star and that these are roAp pulsations. Alternatively, there is a possibility that the high-frequency peaks could be solar-like oscillations excited by stochastic convective motions or perhaps arise in an unseen compact companion.

In this paper we show that KIC 4840675 is composed of at least three stars. The most luminous component is a rapidly rotating A star which is the most probable source of the $\delta$ Sct pulsations. The other two stars appear to be similar to the Sun. We discuss the frequencies of the $\delta$ Sct component. The dominant low frequency may be the rotational frequency of the star. Finally, we attempt to locate the origin of the rapid light variation and the mechanism which drives these pulsations.

## 2 THE KEPLER PHOTOMETRY

The Kepler photometric observations mostly have exposures of about 30 min (long-cadence, LC), but some stars were observed in short-cadence (SC) mode in which the exposure time is about 1 min . Characteristics of SC data are described in Gilliland et al. (2010), while Jenkins et al. (2010b) describe the characteristics of LC data. Jenkins et al. (2010a) describe the Kepler science processing pipeline. LC data are available for quarters $0-9$, most of which are in the public domain. Since the Nyquist frequency for LC data is only about $24 \mathrm{~d}^{-1}$, these data are of limited use for our purposes. KIC 4840675 was observed in SC mode in the last part of quarter 3 and for the whole of quarter 9 (see Table 1 for a log of the observations).

For the Kepler data, we use the simple aperture photometry on which only basic calibration is performed. The SC light curve was examined and outliers removed by inspection. There are small magnitude jumps between different data sets which were adjusted by visual inspection. Part of the light curve (from Q3.3) is shown in Fig. 1. Periodograms of the combined data are shown in Fig. 2. Note, in particular, the presence of three peaks in the region around

Table 1. Log of Kepler SC observations for KIC 4840675. The Kepler quarter name, the start and ending truncated Julian day, the duration and the number of data points, $N$, are shown.

| Quarter | Julian day | Days | $N$ |
| :--- | :--- | :--- | :--- |
| Q3.3 | $55156.5-55182.5$ | 26.0 | 38047 |
| Q9.1 | $55641.5-55677.9$ | 36.4 | 53320 |
| Q9.2 | $55678.6-55707.1$ | 28.5 | 41748 |
| Q9.3 | $55707.8-55738.9$ | 31.2 | 45609 |



Figure 1. Part of the Kepler light curve of KIC 4840675.


Figure 2. Periodograms of the combined data for KIC 4840675. The bottom panel shows the dominant frequency $f_{1}=22.069 \mathrm{~d}^{-1}$. The middle panel shows the same part of the periodogram on an expanded scale. The top panel shows the outlying high-frequency triplet.
$120 \mathrm{~d}^{-1}$. It is these high frequencies which have motivated this paper.

It is important to understand the source of these high-frequency peaks as they could originate in a fainter star within the same aperture. For this purpose, we made a thorough check at the pixel level using the Q9.3 SC target pixel data. First, we checked the light curves of all available pixels within the downloaded region. None of the individual pixels shows the high-frequency triplet above the noise level. This is a strong indication that there is no close contaminator within the spatial resolution of Kepler that shows these high-frequency variations. In order to be detected when all the pixels
are summed, any pixel would have to vary with large amplitude at these frequencies. There are two fainter stars within the downloaded region, but these are well separated from KIC 4840675 . These stars also do not exhibit the frequencies in question.

Saturation will occur for such a bright target, but the total flux is preserved which allows for precise photometry. However, we noticed that the saturated pixels have a strange non-linear variation. Instead of a constant saturated flux, saturation seems to occur at discrete flux levels. The jumps between these levels appear to be random. The mean flux in the optimal aperture is $1.88 \times 10^{6} \mathrm{e} \mathrm{s}^{-1}$ and the flux difference between the levels is about $50 \mathrm{e} \mathrm{s}^{-1}$, so the relative variation is similar to the amplitudes of the three high frequencies. In addition, because the time interval varies between successive saturation level jumps, one needs to consider whether this frequency modulation may cause spurious side frequencies (Benkő, Szabó \& Paparó 2011). The irregular frequency modulation is hard to treat analytically, so we created an artificial data set containing only the flux jumps and averaged out the pulsation. We found no significant peaks in the relevant frequency region of the periodogram resulting from this simulation. It is not clear whether these jumps reflect a real charge distribution or a result of the readout process or other instrumental effect. Most probably this behaviour averages out when the flux of all the pixels is summed, because the jumps do not occur at the same time in all pixels.

Another possibility which needs to be considered is that the high frequencies are of instrumental origin. This can be ruled out as none of these frequencies appears in the list of spurious frequencies in Kepler data by Baran (2012), nor do they appear in the periodograms of any of the over 2000 stars observed in SC mode and analysed by one of us (LAB). We conclude that the high frequencies are not an instrumental effect nor do they originate in any faint star within the aperture. They are almost certainly caused by a variation in one of the stars in the KIC 4840675 system.

## 3 SPECTROSCOPY

A single medium-resolution optical spectrum of KIC 4840675 was obtained using the cross-dispersed, Fibre-fed Échelle Spectrograph (FIES) attached to the Nordic Optical Telescope (NOT) at Observatorio Roque de los Muchachos, La Palma. The wavelength range is $3700-7300 \AA$, with a spectral resolution of 46000 and a signal-tonoise ratio of about 100 at $5500 \AA$. The spectrum was reduced using FIESTOOL and consists of bias subtraction, scattered light correction, division by a normalized flat-field and wavelength calibration. The continuum was normalized using sPLAT, the spectral analysis tool from the starlink project (Draper et al. 2005).

It is clear from inspection of the spectrum that the lines are broad, but there are many, weaker, sharp lines. Both the Mg b and CaK lines are consistent with $\log g \approx 4.0 \pm 0.5$ dex. To analyse this spectrum, we generated synthetic spectra using the sPectrum code (Gray 2010) and model atmospheres by Castelli, Gratton \& Kurucz (1997). Cross-correlation of the observed spectrum with an unbroadened synthetic spectrum as template ( $T_{\text {eff }}=7000 \mathrm{~K}, \log g=$ 4.00 and solar metallicity) shows that there are at least three stars in the system (Fig. 3). There is one broad-lined component and two other stars with sharp lines. The cross-correlation enables us to obtain the radial velocity of each component in the system.

We need to determine the stellar parameters of all three stars given the spectrum and constraints imposed by the relative brightnesses. Our approach is to assume initial values and iterate until we converge to the best solution. We started by ignoring the two faint components B and C and assuming that the spectrum is due only to the bright A


Figure 3. Cross-correlation between the observed spectrum and a synthetic template spectrum over the wavelength range 4950-5810 $\AA$. The dashed curve is the cross-correlation with the best-fitting synthetic composite spectrum.
component. From the broad peak in the cross-correlation function, we estimated $v \sin i \approx 220 \mathrm{~km} \mathrm{~s}^{-1}$ for star A. This estimate was obtained after several trials in which the synthetic spectrum was broadened by different amounts. The above value is the best fit in matching the broad peak in the synthetic cross-correlation function with the broad peak in the observed cross-correlation function.

We created a grid of synthetic spectra with solar abundances, $v \sin i=220 \mathrm{~km} \mathrm{~s}^{-1}$ and $6000 \leq T_{\text {eff }} \leq 10000 \mathrm{~K}$ in steps of 250 K and $2.5 \leq \log g \leq 5.0$ in steps of 0.5 dex. We fitted the $\mathrm{H} \alpha$ (6500$6620 \AA$ ) and $\mathrm{H} \beta$ ( $4800-4930 \AA$ ) line profiles to these models to estimate the effective temperature and surface gravity of the A component. The best match occurs for $T_{\text {eff }} \approx 7250 \mathrm{~K}$ and $\log g \approx$ 3.5. Using the above parameters for star A and assumed values of $T_{\text {eff }}=6000 \mathrm{~K}, \log g=4.5$ for components B and C, we generated synthetic combined spectra. For this purpose, we used the radial velocities derived from cross-correlation and initial guesses for the relative brightnesses and line broadenings. By comparing the crosscorrelation function of the combined synthetic spectrum with the observed cross-correlation function (using the same template), we can adjust the relative brightnesses of the three components until we obtain a good match for the relative heights of the three peaks.

With improved relative brightnesses obtained in this way, we repeated the process of matching the $\mathrm{H} \alpha$ and $\mathrm{H} \beta$ line profiles. After one or two iterations we found no change in the solution which gives for star A $T_{\text {eff }}=7250 \mathrm{~K}, \log g=3.5$ for the $\mathrm{H} \alpha$ line and $T_{\text {eff }}=$ $7500 \mathrm{~K}, \log g=4.0$ for $\mathrm{H} \beta$. The $\mathrm{H} \alpha$ line is contaminated with several sharp telluric lines. The values of $T_{\text {eff }}$ and $\log g$ shown in Table 2 were obtained by fitting both lines simultaneously. Lowering the adopted effective temperatures of the B and C components to $T_{\text {eff }}=5000 \mathrm{~K}$ has the effect of slightly increasing $T_{\text {eff }}$ of A to about 7500 K while decreasing the surface gravity to $\log g \approx 3.0$.

Using the adopted values for star A and still fixing $T_{\text {eff }}=6000 \mathrm{~K}$, $\log g=4.5$ for components B and C, we proceeded to fine tune the relative brightnesses. The relative peak heights in the crosscorrelation function are sensitive to the values chosen for the relative brightnesses, so these important quantities can be determined quite precisely. However, they do depend on the adopted value of $v \sin i$ for B and C. By varying all parameters, we found a best fit for the values listed in Table 2. The observed cross-correlation function is compared with the synthetic cross-correlation function in Fig. 3. The match between observed and synthetic spectra in the $\mathrm{H} \beta$ region for the parameters listed in Table 2 is shown in Fig. 4. In this figure we also show part of the spectrum after removing the contribution of $\operatorname{star} \mathrm{A}$.

Table 2. Parameters for the three components in the spectrum. For each star, the effective temperature $T_{\text {eff }}(\mathrm{K})$, gravity $\log g$, projected rotational velocity $v \sin i\left(\mathrm{~km} \mathrm{~s}^{-1}\right)$, metal abundance $[\mathrm{Fe} / \mathrm{H}]$, radial velocity $V_{r}\left(\mathrm{~km} \mathrm{~s}^{-1}\right)$ and relative brightnesses, $l / l_{\text {tot }}$, are listed. Estimates of mass, radius and luminosity for the A component are from the calibration of Torres, Andersen \& Giménez (2010). Stars B and C are assumed to have approximately solar values.

|  | A | B | C |
| :---: | :---: | :---: | :---: |
| $T_{\text {eff }}$ | $7400 \pm 200$ | $6000 \pm 300$ | $5900 \pm 300$ |
| $\log g$ | $4.0 \pm 0.3$ | $4.5 \pm 0.3$ | $4.5 \pm 0.3$ |
| $v \sin i$ | $220 \pm 5$ | $5 \pm 5$ | $5 \pm 5$ |
| $[\mathrm{Fe} / \mathrm{H}]$ |  | $-0.07 \pm 0.30$ | $-0.10 \pm 0.26$ |
| $V_{r}$ | $-10.0 \pm 2$ | $-7.0 \pm 0.5$ | $-50.9 \pm 0.5$ |
| $l / l_{\text {tot }}$ | $0.880 \pm 0.01$ | $0.066 \pm 0.01$ | $0.054 \pm 0.01$ |
| $M / \mathrm{M}_{\odot}$ | $1.7 \pm 0.3$ | $\approx 1.0$ | $\approx 1.0$ |
| $R / \mathrm{R}_{\odot}$ | $2.2 \pm 0.9$ | $\approx 1.0$ | $\approx 1.0$ |
| $\log (L / \mathrm{L} \odot)$ | $1.1 \pm 0.4$ | $\approx 0.0$ | $\approx-0.1$ |

We measured the equivalent widths of as many unblended Fe lines as possible in the wavelength region $6000-6800 \AA$. A total of 22 lines were identified and measured for both stars. A microturbulence of $1 \mathrm{~km} \mathrm{~s}^{-1}$ was assumed. The effective temperature for each star was adjusted until there was no abundance trend with excitation potential. This yielded the values of $T_{\text {eff }}$ shown in Table 2 for stars B and C. The surface gravity was then adjusted to bring the ionization balance between $\mathrm{Fe}_{\mathrm{I}}$ and $\mathrm{Fe}_{\text {II }}$ into agreement. This indicated $\log g=4.5 \pm 0.3$ dex for both stars. The iron abundances for the two stars were found to be $[\mathrm{Fe} / \mathrm{H}]=-0.07 \pm 0.30$ and $-0.10 \pm 0.26$, respectively. The projected rotational velocities for $B$ and $C$ are close to zero; the fit to the cross-correlation function suggests $v \sin i \approx 5 \mathrm{~km} \mathrm{~s}^{-1}$. A macroturbulence of $\xi=3 \mathrm{~km} \mathrm{~s}^{-1}$ was adopted based on the Bruntt et al. (2010) calibration. An upper limit of $\xi \lesssim 5 \mathrm{~km} \mathrm{~s}^{-1}$ appears to be reasonable.

We have not been able to find any sign of Ap or Am characteristics in the bright A-type star, but this would in any case be very difficult to detect in such a broad-lined star. Abt \& Morrell (1995) found that all rapid rotators have normal spectra and nearly all slow rotators have abnormal spectra (Ap or Am). There does not seem to be any
spectral peculiarities in the $B$ and $C$ companions. The lines due to stars B and C appear weaker in the blue compared to the red, as would be expected from the temperature difference.

We assume that components A, B and C form a bound system because the chances of finding three stars within the spectroscopic aperture are very remote. Furthermore, the relative brightnesses of the stars determined from spectroscopy are consistent with the three stars being at the same distance. Unfortunately, we do not have information on the orbit which could prove the point The radial velocity difference of about $40 \mathrm{~km} \mathrm{~s}^{-1}$ between A and C is certainly consistent with orbital motion given the expected masses provided that the distance between A and C is less than about 9.4 au $\left(2000 \mathrm{R}_{\odot}\right)$. In any case, whether the stars are bound or not will not affect any of the conclusions in this paper.

## 4 STELLAR PARAMETERS FROM PHOTOMETRY

We have used broad-band photometry from TYCHO-2, USNOB1.0 R-mag, TASS-I, CMC14 r' and Two Micron All Sky Survey (2MASS) to estimate the total observed bolometric flux. The infrared flux method (IRFM; Blackwell \& Shallis 1977) was then used with 2MASS magnitudes to determine $T_{\text {eff }}$. This gives $T_{\text {eff }}=$ $7030 \pm 150 \mathrm{~K}$, which is somewhat smaller, but consistent with the spectroscopic value. Although the luminosity of the A star is nearly 90 per cent of the total luminosity of the system in the blue region of the spectrum (Table 2), it would be less dominant in the near-infrared, leading to a somewhat cooler effective temperature.

The spectrum reveals strong interstellar NaD lines with $V_{r}=$ $-18 \pm 1 \mathrm{~km} \mathrm{~s}^{-1}$, and an equivalent width $(\mathrm{EW})=0.15 \pm 0.02 \AA$. Using the Munari \& Zwitter (1997) relation we estimate $E(B-V)=$ $0.05 \pm 0.01$. This raises the effective temperature determined from the IRFM to $T_{\text {eff }}=7380 \pm 160 \mathrm{~K}$, which is in good agreement with that estimated from Balmer line spectroscopic fitting.

The IRFM might be affected by the presence of cool companions (Smalley 1993). The modified IRFM would increase the effective temperature of the primary to about $T_{\text {eff }} \approx 8000 \mathrm{~K}$ for two mainsequence companions (both with $T_{\text {eff }} \approx 6000 \mathrm{~K}$ ), if the primary is

Figure 4. Bottom panel: the observed spectrum around $\mathrm{H} \beta$ (red) and the best-fitting synthetic spectrum (green) with $T_{\text {eff }}=7400 \mathrm{~K}, \log g=4.0$. Top panel: residual spectrum after subtracting this synthetic spectrum showing lines from the cooler, fainter, components.


Figure 5. Possible locations of the three components in the KIC 4840675 system in the HR diagram (filled circles). One standard deviation error bars are shown for the A companion. The ZAMS and several evolutionary sequences with solar composition (Bertelli et al. 2008) are shown. The sequences are spaced at intervals of $0.2 \mathrm{M}_{\odot}$ with masses of two tracks labelled. The trapezoidal figure is the approximate boundary of Kepler $\delta$ Sct stars from Balona \& Dziembowski (2011). Open circles are approximate locations of roAp stars.
also main sequence, but to no more than about 7600 K for a more evolved primary with $R \approx 3 \mathrm{R}_{\odot}$. This suggests that the bright A star might be somewhat evolved with $\log g \lesssim 4.0$ dex.

Fig. 5 shows the location of the three stars in the HR diagram based on our limited knowledge of their parameters. The evidence suggests that star A is slightly evolved but still on the main sequence. We have assumed that stars B and C are on the zero-age main sequence (ZAMS). If the three stars are gravitationally bound, as seems likely, they should also be coeval. However, the errors in the parameters are such that this cannot be tested. If we take the relative brightnesses of the three stars into account and assume that B and C are on the ZAMS, then for star $\mathrm{A} \log L / \mathrm{L}_{\odot} \odot 1.1$, which agrees with the deduced spectroscopic value.

## 5 FREQUENCY ANALYSIS

There are several hundred significant frequencies that can be extracted from the Kepler SC photometry. Although the inclusion of the data from Q3.3 does allow the frequencies to be refined, the large gap between this data set and the Q9 SC data lead to a complex window function. We decided to omit Q3.3 and use only the combined Q9 SC data ( 97.5 d ) for the purpose of frequency extraction. In Table 3 we list some of the frequencies with highest amplitudes. Most of the variability is confined to the range $15-45 \mathrm{~d}^{-1}$, but there are quite a number of highly significant low frequencies as well.

The variability is dominated by a mode at $f_{1}=22.07 \mathrm{~d}^{-1}$ with amplitude $A_{1}=1.37 \mathrm{mmag}$. In spite of the dominance of this mode, there is no indication of harmonics. There is a peak very close to $2 f_{1}$, but its amplitude is only about $5 \mu \mathrm{mag}$ and its significance is doubtful. The LC data (see Table 5 for a log of the observations) are useful for testing long-term amplitude variations. The amplitude of this mode is clearly variable as can be seen in Fig. 6 where the amplitude at each data set is shown. Note that the amplitudes obtained from LC data are underestimated because a considerable fraction of the pulsational cycle is sampled. It is possible to correct for this effect (Huber et al. 2010), but here we are only interested in the relative amplitude variation.

There appear to be smaller amplitude variations for some other modes, but these are less clear and less regular than for $f_{1}$. Neverthe-

Table 3. Frequencies, $f_{N}$ (in $\mathrm{d}^{-1}$ ), and amplitudes, $A_{N}$ (in mmag), of modes in KIC 4840675. The numbers in brackets are the two last digits of the standard deviations. Only frequencies with the highest amplitudes are listed.

| $N$ | $f_{N}$ | $A_{N}$ | $N$ | $f_{N}$ | $A_{N}$ |
| ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | $22.06872(01)$ | $1.3715(09)$ | 21 | $7.94407(37)$ | $0.0625(09)$ |
| 2 | $33.81286(08)$ | $0.2936(09)$ | 22 | $6.96310(39)$ | $0.0614(09)$ |
| 3 | $23.44574(09)$ | $0.2551(09)$ | 23 | $20.07914(39)$ | $0.0614(09)$ |
| 4 | $24.97014(09)$ | $0.2529(09)$ | 24 | $26.63867(43)$ | $0.0553(09)$ |
| 5 | $16.39243(10)$ | $0.2260(09)$ | 25 | $18.10069(45)$ | $0.0529(09)$ |
| 6 | $27.22668(10)$ | $0.2179(09)$ | 26 | $31.56580(47)$ | $0.0507(09)$ |
| 7 | $30.01549(12)$ | $0.1942(09)$ | 27 | $11.23126(47)$ | $0.0502(09)$ |
| 8 | $19.90851(14)$ | $0.1664(09)$ | 28 | $28.71056(48)$ | $0.0503(09)$ |
| 9 | $21.24281(16)$ | $0.1415(09)$ | 29 | $28.19591(48)$ | $0.0492(09)$ |
| 10 | $31.36071(19)$ | $0.1223(09)$ | 30 | $0.11758(52)$ | $0.0454(09)$ |
| 11 | $30.34339(22)$ | $0.1075(09)$ | 31 | $5.29624(54)$ | $0.0444(09)$ |
| 12 | $18.54189(22)$ | $0.1052(09)$ | 32 | $24.32143(55)$ | $0.0436(09)$ |
| 13 | $21.40450(24)$ | $0.0954(09)$ | 33 | $17.10252(56)$ | $0.0422(09)$ |
| 14 | $27.99361(27)$ | $0.0889(09)$ | 34 | $43.26449(57)$ | $0.0420(09)$ |
| 15 | $21.10408(27)$ | $0.0875(09)$ | 35 | $4.50995(60)$ | $0.0393(09)$ |
| 16 | $22.20490(27)$ | $0.0854(09)$ | 36 | $23.99176(61)$ | $0.0392(09)$ |
| 17 | $42.52881(28)$ | $0.0837(09)$ | 37 | $42.75982(64)$ | $0.0369(09)$ |
| 18 | $20.70656(29)$ | $0.0829(09)$ | 38 | $24.15737(66)$ | $0.0362(09)$ |
| 19 | $2.64929(32)$ | $0.0731(09)$ | 39 | $37.61171(67)$ | $0.0355(09)$ |
| 20 | $21.73407(33)$ | $0.0727(09)$ | 40 | $25.99328(68)$ | $0.0351(09)$ |



Figure 6. The amplitude of the dominant mode, $f_{1}$, as a function of time from LC data.
less, these are probably real as they are uncorrelated with each other and therefore cannot be ascribed to instrumental effects. Amplitude variations are quite common in $\delta$ Sct stars (Handler et al. 2000; Breger \& Pamyatnykh 2006; Breger \& Lenz 2008). After removing the dominant frequency, two sidelobes, separated by about $0.06 \mathrm{~d}^{-1}$ from the pre-whitened main peak, remain. This may be a result of the long-term amplitude variability. There are a large number of other frequency peaks with amplitudes in the range $0.05-0.20 \mathrm{mmag}$.

Mode identification requires multicolour photometry. The amplitudes of the $\delta$ Sct modes are well below the level which can be observed from the ground, except possibly for the mode of highest amplitude. Therefore mode identification will not be available in the foreseeable future and very little information can be extracted from these frequencies. However, there does seem to be a preferred separation. We have calculated all possible separations between pairs of frequencies in the range 5-50 $\mathrm{d}^{-1}$ and with amplitudes greater than 0.02 mmag. The distribution of separations shows a peak at $2.2 \mathrm{~d}^{-1}$ and, perhaps, lower peaks at about 3.5 and $6.5 \mathrm{~d}^{-1}$ (Fig. 7).

The concentration of modes having a separation of $2.2 \mathrm{~d}^{-1}$ may reflect the rotational splitting, but without further evidence this cannot be verified. Note that even in rapidly rotating stars, where the frequency multiplets due to rotational splitting are not equally spaced, equal frequency spacing is still preserved between modes


Figure 7. Histogram showing numbers of frequency pairs with the given frequency separation.
with positive and negative values of the same azimuthal number, $m$, and remains $2 m$ times the rotation rate (Deupree 2011). In this regard, we note that the dominant low frequency, $f_{19}=2.649 \mathrm{~d}^{-1}$, is possibly the rotational frequency of star A (see below). Rotational splitting should be close, but not identical, to the rotational frequency. The peak frequency in the distribution of Fig. 7 seems to satisfy this condition.

Balona \& Dziembowski (2011) found that about 10 per cent of Kepler $\delta$ Sct stars have one dominant mode, often with a side peak of lower amplitude. KIC 4840675 may be regarded as belonging to this group. These stars appear to obey period-luminosity and periodtemperature relationships, suggesting that the high-amplitude mode has the same spherical harmonic degree, $l$, in all stars. This is likely to be $l=0$ not only because of the high amplitude, but also because rotational effects would tend to destroy any correlation between frequency and luminosity or temperature. It is therefore interesting to consider the implications if we assume that $f_{1}$ is the fundamental radial mode in KIC 4840675.

Models of $\delta$ Sct stars with masses in the range $1.3<M / \mathrm{M}_{\odot}<2.5$ were constructed using the Warsaw-New Jersey code (Paczyński 1970). These non-rotating models use opal opacities, no core overshoot and a mixing length, $\alpha=1.0$. Pulsation frequencies for each model were obtained using the nADROT code (Dziemblowski 1977). The average large separation, $\Delta v$, for unstable modes was calculated from frequencies of sequential $\ell=0$ and 1 modes for all models on the ZAMS until the end of core hydrogen burning. A reasonably tight correlation between $\Delta v$ and $\log g$ is found. A least-squares fit, which includes both $\ell=0$ and 1 , is given by
$\log \Delta v=-2.4948+0.7656 \log g$,
where $\Delta v$ is in $\mathrm{d}^{-1}$. The frequency of the fundamental radial mode, $f_{01}$, as a function of surface gravity is well represented by
$\log f_{01}=-2.0637+0.7865 \log g$,
where $f_{01}$ is in $\mathrm{d}^{-1}$. If we assume that $f_{1}$ is the fundamental radial mode, we obtain $\log g \approx 4.3$ and $\Delta v \approx 6.6 \mathrm{~d}^{-1}$. There is, in fact, a peak at $6.5 \mathrm{~d}^{-1}$ in Fig. 7 which may be the large separation. The surface gravity is certainly consistent with the spectroscopic value. Thus our assumption that $f_{1}$ is the fundamental radial mode appears to be at least consistent with what we know of the star.

## 6 HIGH FREQUENCIES

Of particular interest is the presence of three high-frequency peaks at around $120 \mathrm{~d}^{-1}$, as shown in the top panel of Fig. 2 and listed in Table 4. To prevent confusion with the $\delta$ Sct frequencies, which we label by $f_{N}$, we label these high frequencies as $v_{N}$. According to the

Table 4. Frequencies, $v_{N}$, and amplitudes, $A_{N}$ (in mmag), of the three high-frequency peaks.

| $N$ | $v_{N}\left(\mathrm{~d}^{-1}\right)$ | $v_{N}(\mu \mathrm{~Hz})$ | $A_{N}$ |
| ---: | ---: | ---: | ---: |
| 1 | $129.031(4)$ | $1493.41(04)$ | $0.0058(06)$ |
| 2 | $123.801(4)$ | $1432.88(05)$ | $0.0054(06)$ |
| 3 | $118.430(5)$ | $1370.72(06)$ | $0.0044(05)$ |



Figure 8. Periodograms in the high-frequency region for different independent data subsets. All three peaks appear in each subset.

Lomb-Scargle false alarm probability (Scargle 1982), the peaks are highly significant. In any case, there is little doubt of their reality because all three frequency peaks are clearly seen in periodograms of independent subsets of the data (Fig. 8). None of these frequencies can be attributed to a harmonic of $f_{1}$ or a combination frequency.
The three frequencies form a triplet with nearly equal spacing: $v_{1}-v_{2}=5.230, v_{2}-v_{3}=5.371 \mathrm{~d}^{-1}$. Notice that the frequency separation $v_{1}-v_{3}$ is exactly $4 f_{19}$ within the errors. Rotational splitting of a mode depends on the mode and structure of the star and, to first order, is given by $v=v_{0}+m(1-C) \Omega$, where $v_{0}$ is the frequency in the absence of rotation, $m$ is the azimuthal order, $\Omega$ the rotational frequency and $C$ the Ledoux coefficient (Ledoux \& Walraven 1958). Since $f_{19}$ may be the rotational frequency, and since the Ledoux coefficient is practically zero at these high frequencies, $4 f_{19}$ is the expected value for the rotational splitting of modes of the same $l$ and $m=(2,-2)$. This may be a coincidence, but if true it would imply that these high frequencies originate in the A component.
The individual peaks are shown in more detail in Fig. 9. The window function has the same shape as the peaks, which means that the high-frequency peaks disappear completely when pre-whitened. This indicates that they are stable frequencies with long lifetimes. Significant frequency or amplitude variations, as might occur for stochastically excited modes would leave a residual signal after prewhitening. However, such a residual signal might still be present at the level of the background noise.
Although frequencies larger than $100 \mathrm{~d}^{-1}$ are seen in a few Ke pler $\delta$ Sct stars, they can invariably be attributed to harmonics of a dominant frequency. In KIC 4840675 this is clearly not the case, nor can they be explained as a combination of lower frequency modes. Therefore we need to consider the excitation mechanism which can lead to such a high frequency. Since the normal $\kappa$ mechanism acting in the $\mathrm{He}_{\text {II }}$ ionization zone is not capable of destabilizing such high frequencies (Balona \& Dziembowski 2011), we can only suppose that they must be a result of another mechanism. We know of only two mechanisms which could give rise to these frequencies:


Figure 9. Detail of the periodogram in the region of the three high frequencies.
stochastic excitation (solar-like oscillations) or oscillations of the roAp type. If we admit the presence of an unseen white dwarf in the system, it is also possible that the high frequencies may be a result of pulsations in a ZZCet, V777 Her or sdB star.

Solar-like oscillations have been suggested to explain some modes in the Am star HD 187547 (Antoci et al. 2011). The problem is that there is no simple method of discriminating between different driving mechanisms. In the case of HD 187547, the modes attributed to driving by solar-like oscillations are only of moderately high frequency (around $65 \mathrm{~d}^{-1}$ ). Although independent modes in this frequency range are not common, they certainly exist in many Kepler $\delta$ Sct stars (Balona 2011). Therefore, driving by the standard $\kappa$ mechanism cannot be entirely ruled out, as mentioned by Antoci et al. (2011). Further examples of solar-like modes in other $\delta$ Sct stars are required.

A test for solar-like oscillations is that they have quite short lifetimes, but the high frequencies are stable to within the noise limits, so their lifetimes must about as long as the duration of the time series ( 90 d ). Furthermore, in all other stars where solar-like oscillations are present, there is a fairly dense comb-like spectrum of modes within a symmetric amplitude envelope centred at a frequency $v_{\text {max }}$. On the contrary, in KIC 4840675 we see only three isolated modes. If these are the highest amplitude peaks then it is reasonable to assume that the frequency separation of about $61 \mu \mathrm{~Hz}$ is the large separation.

These arguments are not sufficient to rule out solar-like oscillations in star A, though this seems very unlikely. The star has a mass of about $1.7 \mathrm{M}_{\odot}$ and a radius of about $2.2 \mathrm{R}_{\odot}$. From a comparison with a grid of models with various chemical compositions and core overshooting using ASTEC (Christensen-Dalsgaard 2008a) and ADIPLS (Christensen-Dalsgaard 2008b), we find a large separation $\Delta \nu \approx 54 \mu \mathrm{~Hz}$. This, in turn results in maximum power at $\nu_{\text {max }} \approx 990 \mu \mathrm{~Hz}$ from the scaling relationship of Stello et al. (2009), which is significantly lower than observed. On the other hand, if we look for models with $\Delta v \approx 60 \mu \mathrm{~Hz}$, similar to the separation between peaks, and $T_{\text {eff }}=7400 \mathrm{~K}$, we find a slightly lower
luminosity, $\log L / \mathrm{L}_{\odot} \approx 1.03$. From the same scaling relationship we obtain $\nu_{\max } \approx 1130 \mu \mathrm{~Hz}$, which is still significantly lower than observed. We conclude that it would be difficult to understand the location of the high frequencies if they are due to solar-like pulsations in star A.

If the high frequencies are a result of solar-like oscillations in either star B or C, their real amplitudes must be about 10 times larger or about 50 ppm , owing to the presence of the A companion which is 10 times more luminous. There is a strong correlation between amplitude and $\nu_{\text {max }}$ in Kepler stars with solar-like oscillations (Huber et al. 2011). The expected amplitude for $v_{\max } \approx 1450 \mu \mathrm{~Hz}$ is only 2 ppm , which is far lower than the inferred value of about 50 ppm . On this basis alone, it is clear that the high-frequency modes are most unlikely to be solar-like oscillations in one of the two faint companion stars.

The stellar parameters for B and C are even more uncertain than for A, but they do seem to be quite similar to the Sun. However, $v_{\max }=3300 \mu \mathrm{~Hz}$ in the Sun is much larger than observed in KIC 4840675. If we use the parameters in Table 2 for components B and C, the tight scaling relationship between $\Delta v$ and $v_{\max }$ (Stello et al. 2009) results in values for $v_{\text {max }}$ that are even larger than that of the Sun. We conclude that although spectroscopy indicates that the two faint companions are similar to the Sun, the expected frequency and large separation are very different from the observed values. This, together with the fact that the observed amplitude of the presumed solar-like oscillations would be at least an order of magnitude larger than expected, rules out solar-like oscillations in B and C as an explanation for the high frequencies.

It is, of course, possible that solar-like oscillations are present in B and C but, if so, they are not visible in the Kepler data. From the $v_{\text {max }}$-amplitude relationship of Huber et al. (2011), the expected amplitudes would be less than 10 ppm for $\nu_{\text {max }}>1000 \mu \mathrm{~Hz}$. The presence of the A companion, which is 10 times more luminous than B or C, would reduce the observed amplitudes to less than 1 ppm and render any such modes undetectable.

Let us now turn to the possibility that the high frequencies are caused by roAp-like pulsations. Star A is not an Ap star, so they cannot be described as roAp pulsations, but any mechanism which suppresses convection could, in principle, lead to the excitation of high-frequency oscillations through the opacity mechanism working on the H ionization region. In the presence of a strong magnetic field, convection is expected to be suppressed in the magnetic polar regions, rendering high-frequency modes overstable in the region of the HR diagram where roAp stars are observed (Cunha 2002).

To test this possibility, we used non-adiabatic models with and without suppression of envelope convection. A non-local, timedependent mixing-length formalism was used (Gough 1977). In the models with envelope convection, no high radial order, highfrequency modes are excited. When convection is suppressed, both low radial order and high radial order modes are excited. In fact, the region of frequencies in which modes are found to be excited is similar to the region of the high frequencies in KIC 4840675. In addition, this model has a large separation similar to the observed separation between the high-frequency triplets. Despite this, the large rotational velocity derived for the A component makes this star very different from all other roAp stars known (and a faster rotator than any Ap stars known to date), making this scenario rather unlikely.

Finally, we always need to bear in mind that there might be a faint star in the system which may be responsible for the high-frequency oscillations. Pulsating white dwarfs, such as ZZCet or V777 Her stars, have frequencies in the observed range as do subdwarf B stars
(sdB stars). Observations in the far-ultraviolet (UV) may be able to detect the presence of a white dwarf in the system, but unfortunately the star was not observed in the Galaxy Evolution Explorer (GALEX) survey (http://galex.stsci.edu/GR6/). The luminosity of a white dwarf is about $10^{-2}-10^{-3} \mathrm{~L} \odot$ while the total luminosity of the three components in the KIC 4840675 system is about $12 \mathrm{~L} \odot$. Therefore the amplitude of the white dwarf pulsations would be about $10^{3}-10^{4}$ larger in the absence of the three components, or about $0.5-5.0 \mathrm{mmag}$, which is well within the observed range of ZZ Cet or V777 Her stars.
In conclusion, none of the three stars in the system is an obvious candidate for the origin of the high-frequency oscillations. While it is possible that the high frequencies could arise in an unobserved white dwarf companion, this remains a pure conjecture until the putative white dwarf is observed. Until then, the nature of the high frequencies must remain unresolved.

## 7 LOW FREQUENCIES

Since the advent of Kepler we know that $\delta$ Sct stars nearly always have low frequencies. This is a general feature in all A-F stars and not only in $\delta$ Sct variables. Because low frequencies occur in the hottest A-type stars, they cannot be attributed to $\gamma$ Dor pulsations. The convective blocking instability which is thought to drive $\gamma$ Dor pulsations cannot act in these hot stars because they lack a substantial superficial convective zone.
We have already mentioned that KIC 4840675 has a prominent peak at $f_{19}=2.649 \mathrm{~d}^{-1}$ which may be the rotational frequency of star A. There are a number of significant peaks at harmonics of $f_{19}$, indicating that this low frequency variation is non-sinusoidal and therefore consistent with rotational modulation. For low frequencies, the LC data are very useful because they cover a much longer period, as shown by the observational log in Table 5. Again we use the uncalibrated LC data and have adjusted trends and jumps between data sets by visual inspection. The periodograms of individual LC data sets show that $f_{19}$ and its harmonics undergo large amplitude variations.

We can extract the shape of the light curve for each quarter by removing all significant frequencies except those relating to $f_{19}$ and its harmonics. Fig. 10 shows the resulting phase curves. It is clear from Fig. 10 that the amplitude variation in the periodogram is actually a variation in the light-curve shape with time. Note that for Q7-Q9 there is an additional bump at phase $\phi=0.6$ which is not present at earlier times. On the other hand for Q3 and Q4 the bump is at $\phi=0.3$. One might even interpret the sequence of light curves as a stationary curve with a travelling bump. Balona (2011)

Table 5. Log of Kepler LC observations for KIC 4840675. The Kepler quarter name, the start and ending truncated Julian day, the duration and the number of data points, $N$, are shown.

| Quarter | Julian day | Days | $N$ |
| :--- | :--- | :--- | :--- |
| Q0 | $54953.5-54963.2$ | 9.7 | 476 |
| Q1 | $54964.5-54998.0$ | 33.5 | 1639 |
| Q2 | $55002.5-55091.5$ | 88.9 | 4194 |
| Q3 | $55093.2-55182.5$ | 89.2 | 4228 |
| Q4 | $55185.4-55275.2$ | 89.8 | 4159 |
| Q5 | $55276.5-55371.2$ | 94.7 | 4538 |
| Q7 | $55463.2-55552.5$ | 89.4 | 4295 |
| Q8 | $55568.4-55635.3$ | 66.9 | 3143 |
| Q9 | $55641.5-55738.9$ | 97.4 | 4703 |



Figure 10. The light curve of LC data phased with frequency $f_{19}=$ $2.649 \mathrm{~d}^{-1}$. All frequencies except for $f_{19}$ and its harmonics have been removed. The epoch of phase zero is BJD 54950.00.
finds that about 8 per cent of Kepler A-type stars manifest clear travelling bumps in the low frequency variation similar to those found in migrating starspots in cool stars.
We know from statistical studies of large numbers of Kepler A-F stars that the dominant low frequency is a measure of the rotational velocity of the star (Balona 2011). Therefore it is reasonable to assume that $f_{19}$ represents a rotational frequency, presumably of the bright A component. The projected rotational velocity of star A implies that the equatorial velocity $v_{\mathrm{e}}>220 \mathrm{~km} \mathrm{~s}^{-1}$. If we assume $f_{19}$ to be the rotational frequency, we can derive a lower bound for the stellar radius $R>1.63 \mathrm{R}_{\odot}$. From its effective temperature of 7400 K , we obtain a lower bound for the luminosity $\log L_{\mathrm{A}} / \mathrm{L}_{\odot}>$ 0.86 , which is in agreement from the estimate based on the spectroscopic parameters (Table 2).
The above arguments show that it is reasonable to suppose that $f_{19}$ is the rotational frequency. In that case, the light curve of Fig. 10 strongly indicates that the photosphere of star A has a non-uniform brightness distribution, possibly as a result of starspots or corotating
obscurations. It would seem that the spots or obscurations migrate or change intensity on a time-scale of months. There are other indications for surface patches in A stars (Balona 2011) which might suggest a partial explanation for low frequencies in A stars.

## 8 FREQUENCY MODULATION IN A BINARY

If one of the components of a binary system is a pulsating star, the pulsation frequency is Doppler shifted due to the orbital motion. As a result, the periodogram shows additional frequency components. Shibahashi \& Kurtz (2012) have derived general expressions for these components which enable the orbital parameters to be extracted in the same way as traditional methods using the radial velocities. In the case of a relatively rapidly rotating $\delta$ Sct star such as KIC 4840675, the photometric derivation of the mass function is more precise than is possible with spectroscopic radial velocities.

For two stars with masses $m_{1}$ and $m_{2}$ in a circular orbit with inclination $i$, Shibahashi \& Kurtz (2012) show that the frequency modulation results in the appearance of two sidelobes spaced by the orbital frequency. They show that the mass function,
$f\left(m_{1}, m_{2}, \sin i\right)=\frac{m_{2}^{3} \sin ^{3} i}{\left(m_{1}+m_{2}\right)^{2}}$,
can be expressed as
$f\left(m_{1}, m_{2}, \sin i\right)=\left(\frac{A_{+1}+A_{-1}}{A_{0}}\right)^{3} \frac{P_{\text {pul }}^{3}}{P_{\text {orb }}^{2}} \frac{c^{3}}{2 \pi G}$,
where $A_{+1}, A_{-1}$ and $A_{0}$ refer to the amplitudes of the components of the frequency triplet, $A_{0}$ being the amplitude of the central component. $P_{\text {pul }}$ and $P_{\text {orb }}$ are the pulsation and orbital periods, respectively, $G$ is the gravitational constant and $c$ the speed of light.

For the highest amplitude mode in KIC 4840675, $f_{1}$, we have $A_{0}=1.37 \mathrm{mmag}$ (see Table 3). We do not detect any equally spaced sidelobes with amplitudes greater than $10 \mu \mathrm{mag}$, which is a conservative upper estimate of the detection limit. Therefore we can place firm upper limits on $A_{-1}, A_{+1} \leq 0.01 \mathrm{mmag}$. We thus have

$$
\frac{A_{+1}+A_{-1}}{A_{0}}=\left(\frac{2 \pi G}{c^{3}}\right)^{1 / 3} \frac{m_{2} \sin i}{\left(m_{1}+m_{2}\right)^{2 / 3}} \frac{P_{\mathrm{or}}^{2 / 3}}{P_{\mathrm{pul}}}<0.01
$$

Assuming that $m_{1}=1.7 \mathrm{M}_{\odot}$ for the A star and $m_{2}=2 \mathrm{M}_{\odot}$ for the sum of the masses of the two other components, we find for $P_{\text {orb }}=10 \mathrm{~d}$ and $i=90^{\circ}$ that $A_{+1}+A_{-1} / A_{0}=0.06 \sin i$. From the lack of any frequency triplets about $f_{1}$ we can thus rule out all but the smallest of inclinations $\left(i<14^{\circ}\right)$. For longer orbital periods, up to the length of the data set of nearly 800 d , the constraint is much more stringent. For an orbital period of 500 d , for example $\left(A_{+1}+\right.$ $\left.A_{-1}\right) / A_{0}=0.78 \sin i$. In this case it is possible to detect the sidelobes in the mode of highest amplitude for $i>1^{\circ}$.

In general, A stars with orbital periods less than 10 d have synchronous orbits and $v \sin i<100 \mathrm{~km} \mathrm{~s}^{-1}$. The lack of sidelobes to the main frequency in KIC 4840675 thus precludes a short orbital period. As long as the orbit of star A about the other two stars is not nearly face-on, the orbital period must be longer than the length of the data set ( 785 d ). Given the same constraints on orbital period and inclination, one can rule out a roAp star in the system in addition to the three known components. In any case, such a star would be relatively luminous and easily detected in the spectrum.

## 9 CONCLUSIONS

We show that KIC 4840675 is composed of at least three stars. The brightest component is a rapidly rotating main-sequence A star
which is also a $\delta$ Sct variable. The other two stars are similar to the Sun. The most unusual feature of this stellar system is the presence of three independent pulsation modes with frequencies of 118, 124 and $129 \mathrm{~d}^{-1}$. These frequencies are much higher than observed in any other $\delta$ Sct star and cannot be explained by the same mechanism which drives the $\delta$ Sct pulsations.

We considered two possible mechanisms: solar-like modes excited by convection or self-excited modes of the roAp type. The frequency pattern does not resemble the comb-like structure seen in other stars with solar-like oscillations. Moreover, the mode lifetime appears to be longer than expected. We find that the observed high frequencies and implied large separation cannot be matched for solar-like modes in star A. Furthermore, their amplitudes are far too high to be attributed to solar-like oscillations in stars B and C. In this case, too, the frequencies and large separation do not match their expected values. We thus conclude that the high frequencies cannot be due to solar-like oscillations in any of the three stars.

In spite of the fact that star A cannot be an Ap star, we found that models of roAp pulsation do agree quite well with the observed frequencies and frequency spacing. Unless a strong magnetic field is detected in this star, the possibility that this is a new type of roAp-like variable is difficult to accept at this stage. Since none of the three stars seems obvious candidates for the high frequencies, the only alternative is to attribute the origin of these frequencies to an unseen compact companion. However, until such time that the compact companion is detected, this must remain a conjecture.

We find several low frequencies in the light curve which is typical of all A-F stars when observed with high photometric precision. It has been shown that the dominant low frequency in A-F stars is probably the rotational frequency (Balona 2011). Indeed, the dominant low frequency in KIC 4840675 has several harmonics which supports rotational modulation rather than a pulsation. Furthermore, the frequency is consistent with the expected rotational frequency of the star. The light curve changes from season to season, suggesting migrating starspots or spots which change intensity with time.

Further progress in locating the origin of the high frequencies could be made if photometry in the far-UV were available. This might reveal the presence of a compact companion. Until then, KIC 4840675 remains a puzzle and a challenge to our understanding of stellar pulsations.

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