Contents lists available at ScienceDirect



Journal of Safety Science and Resilience



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# Underground storage tank blowout analysis: Stability prediction using an artificial neural network

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## ARTICLE INFO

Keywords: Blowout Passive stability Trapdoor Stability factors Limit analysis

#### ABSTRACT

Most geotechnical stability research is linked to "active" failures, in which soil instability occurs due to soil selfweight and external surcharge applications. In contrast, research on passive failure is not common, as it is predominately caused by external loads that act against the soil self-weight. An earlier active trapdoor stability investigation using the Terzaghi's three stability factor approach was shown to be a feasible method for evaluating cohesive-frictional soil stability. Therefore, this technical note aims to expand "active" trapdoor research to assess drained circular trapdoor passive stability (blowout condition) in cohesive-frictional soil under axisymmetric conditions. Using numerical finite element limit analysis (FELA) simulations, soil cohesion, surcharge, and soil unit weight effects are considered using three stability factors ( $F_{cr}$ ,  $F_{sr}$ , and  $F_{\gamma}$ ), which are all associated with the cover-depth ratio and soil internal friction angle. Both upper-bound (UB) and lower-bound (LB) results are presented in design charts and tables, and the large dataset is further studied using an artificial neural network (ANN) as a predictive model to produce accurate design equations. The proposed passive trapdoor problem under axisymmetric conditions is significant when considering soil blowout stability owing to faulty underground storage tanks or pipelines with high internal pressures.

## 1. Introduction

The classical active trapdoor problem has been considered a fundamental geotechnical stability issue since the innovative study by Terzaghi [1]. As the word "active" suggests, active failures are primarily caused by soil self-weight and surface surcharge. Typical active failure problems include lateral earth pressure, and trapdoor, slope, and tunnel-heading stability.

In contrast, passive failures are related to excessive pressure acting opposite to the soil gravity direction. On occasion, they are called blowout or uplift failures, in which the internal pressure is much greater than the soil shear resistance and self-weight. Owing to the growing population and metropolitan infrastructure development expansion, the demand for subterranean sanitary systems such as various underground storage tanks (water, biogas, and fuel storage tanks) has increased dramatically over the past decades. The demand for underground facilities has highlighted soil stability importance, particularly in blowout stability evaluation.

Previous studies on buried anchor uplift capability in soils were conducted through experimentation by Meyerhof and Adams [2], Vesic [3], Meyerhof [4], and Das [5,6]. Vardoulakis et al. [7] conducted a sequence of physical experiments on cohesionless sand and provided analytical conclusions for both passive and active trapdoors. A wedge extending from a particular trapdoor to the ground surface was utilized to illustrate the passive situation. For computational studies, Koutsabeloulis and Griffiths [8] conducted several finite-element analyses on active and passive trapdoors in soils. Using the discontinuity layout optimization method in conjunction with upper-bound (UB) limit analysis, Smith [9] established a computer-based method for calculating the trapdoor load ratio in cohesionless soils. Martin [10] employed both UB and lower-bound (LB) techniques while applying a unique slip line procedure to estimate the genuine collapse load for undrained active and passive trapdoor stability problems. Wang et al. [11] investigated active and passive soil arching techniques for planar trapdoors in cohesive-frictional soils. No surcharge loading was considered, and complex load ratio normalization limited its practicability.

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https://doi.org/10.1016/j.jnlssr.2023.09.002

Received 16 July 2023; Received in revised form 18 September 2023; Accepted 18 September 2023 Available online 18 October 2023

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Shallow foundation load-bearing capacity has frequently been determined using three stability factors and the superposition technique, which are both widely known as Terzaghi's bearing capacity factors [12]. This approach has recently been recognized as an effective method for collapse load estimation and has been applied to various underground stability problems in cohesive-frictional soils [13–15]. The Terzaghi equation was modified to evaluate active failures, as shown in Eq. (1).

$$\sigma_t = -cF_c + \sigma_s F_s + \gamma DF_\gamma \tag{1}$$

In Eq. (1), the minimum support pressure ( $\sigma_t$ ) is determined by the mathematical formulation of three stability factors, namely the cohesion factor ( $F_c$ ), the surcharge factor ( $F_s$ ), and the unit weight factor ( $F_\gamma$ ). The primary design parameters are soil cohesion *c*, surcharge  $\sigma_s$ , soil unit weight  $\gamma$ , and tunnel diameter *D* [13]. The negative sign in the first term of Eq. (1) suggests that the cohesive strength works in opposition to the soil surcharge motions and soil unit weight.

It should be emphasized that by removing the negative sign in Eq. (1), a new equation can be created to assess passive failure (blowout/uplift failure). This is shown in Eq. (2).

$$\sigma_t = cF_c + \sigma_s F_s + \gamma DF_\gamma \tag{2}$$

According to Eq. (2), the stability factor can be calculated individually by adjusting certain parameters to zero, except for the parameter of interest. For example, in these calculations,  $\gamma = 0$  and  $\sigma_s = 0$  values were used to calculate  $\sigma_t = cF_c$ . The other two stability factors ( $F_s$  and  $F_\gamma$ ) can be calculated in a similar manner. Further details on the numerical operation are available in Shiau and Al-Asadi [13].

The main objective of this study is to broaden the stability solution for a trustworthy drained circular trapdoor evaluation in cohesivefrictional soil under axisymmetric conditions. The passive trapdoor problem is assumed to represent a soil blowout incident caused by a faulty subterranean storage tank under high internal pressure. Recently developed UB and LB finite element limit analysis (FELA) was employed to produce rigorous solutions for practical use. Using a large FELA result dataset, an artificial neural network (ANN) model was established to produce novel formulae for predicting the three stability factors. This study aims to provide accurate equations for predicting trapdoor blowout stability in cohesive-frictional soils under axisymmetric conditions. Novel formulae can improve working design speed compared with traditional methods, such as modeling or interpolating using a design chart. Practitioners can use novel formulae in MS Excel to immediately perform hundreds of tasks.



Fig. 1. A passive circular trapdoor in axisymmetry.



Fig. 2. A numerical model, boundary condition and adaptive mesh for  $F_{\gamma}$  analysis (H/D = 3).

#### 2. Problem statement and three stability factors

The problem definition for passive trapdoors in cohesive-frictional soil under axisymmetric conditions is illustrated in Fig. 1. The trapdoor has a diameter (*D*) and a cover depth (*H*) measured from the top surface of the ground with a uniform surface pressure ( $\sigma_s$ ). On the trapdoor surface, a uniform uplift pressure ( $\sigma_t$ ) was applied vertically in the opposite direction to the soil self-weight and surcharge loading. Three soil properties were used to represent the soil strength profile as the soil mass satisfied the Mohr-Coulomb yield criteria: drained cohesion (*c*), drained friction angle ( $\phi$ ), and soil unit weight ( $\gamma$ ). Note that this study proposes a perfectly ideal engineering case, which is a circular trapdoor in cohesive-frictional soil under axisymmetric conditions. This



**Fig. 3.**  $F_c$  vs.  $\phi$  (*LB* and *UB*) at various depth ratios (*H*/*D* = 0.5–10).

**Table 1** $F_c$  vs.  $\phi$  (*LB*) at various depth ratios (*H*/*D* = 0.5–10).

| $\phi$ | $H/D$ ( $F_c$ , 1 | LB)   |        |        |        |         |         |         |         |         |         |
|--------|-------------------|-------|--------|--------|--------|---------|---------|---------|---------|---------|---------|
|        | 0.5               | 1     | 2      | 3      | 4      | 5       | 6       | 7       | 8       | 9       | 10      |
| 0      | 1.964             | 3.935 | 7.159  | 9.108  | 10.470 | 11.521  | 12.362  | 13.074  | 13.685  | 14.218  | 14.704  |
| 1      | 1.980             | 4.002 | 7.472  | 9.684  | 11.278 | 12.512  | 13.537  | 14.398  | 15.156  | 15.822  | 16.425  |
| 2      | 1.997             | 4.070 | 7.796  | 10.284 | 12.126 | 13.591  | 14.808  | 15.858  | 16.790  | 17.615  | 18.360  |
| 3      | 2.014             | 4.137 | 8.124  | 10.912 | 13.030 | 14.742  | 16.188  | 17.471  | 18.596  | 19.589  | 20.536  |
| 4      | 2.031             | 4.205 | 8.453  | 11.566 | 13.998 | 15.986  | 17.700  | 19.231  | 20.576  | 21.834  | 22.973  |
| 5      | 2.048             | 4.273 | 8.790  | 12.239 | 14.999 | 17.323  | 19.324  | 21.146  | 22.773  | 24.290  | 25.679  |
| 6      | 2.065             | 4.340 | 9.123  | 12.935 | 16.060 | 18.737  | 21.117  | 23.236  | 25.193  | 26.989  | 28.671  |
| 7      | 2.082             | 4.408 | 9.451  | 13.660 | 17.200 | 20.258  | 23.002  | 25.502  | 27.789  | 29.986  | 31.973  |
| 8      | 2.099             | 4.477 | 9.787  | 14.410 | 18.373 | 21.853  | 25.024  | 27.964  | 30.685  | 33.224  | 35.629  |
| 9      | 2.116             | 4.547 | 10.120 | 15.167 | 19.583 | 23.553  | 27.209  | 30.612  | 33.806  | 36.812  | 39.676  |
| 10     | 2.113             | 4.616 | 10.451 | 15.945 | 20.837 | 25.358  | 29.539  | 33.488  | 37.136  | 40.729  | 44.133  |
| 11     | 2.150             | 4.686 | 10.775 | 16.733 | 22.158 | 27.242  | 31.938  | 36.525  | 40.842  | 44.912  | 48.923  |
| 12     | 2.166             | 4.756 | 11.084 | 17.544 | 23.581 | 29.214  | 34.569  | 39.750  | 44.751  | 49.502  | 54.113  |
| 13     | 2.185             | 4.825 | 11.402 | 18.360 | 24.951 | 31.268  | 37.374  | 43.255  | 48.941  | 54.429  | 59.850  |
| 14     | 2.202             | 4.896 | 11.709 | 19.191 | 26.408 | 33.400  | 40.173  | 46.870  | 53.395  | 59.707  | 65.994  |
| 15     | 2.220             | 4.969 | 12.010 | 20.006 | 27.887 | 35.658  | 43.274  | 50.704  | 58.115  | 65.368  | 72.573  |
| 16     | 2.239             | 5.040 | 12.297 | 20.851 | 29.434 | 37.966  | 46.375  | 54.863  | 63.235  | 71.496  | 79.642  |
| 17     | 2.256             | 5.111 | 12.595 | 21.677 | 30.949 | 40.366  | 49.757  | 59.082  | 68.490  | 77.761  | 87.078  |
| 18     | 2.274             | 5.185 | 12.896 | 22.512 | 32.568 | 42.790  | 53.210  | 63.601  | 74.237  | 84.651  | 95.173  |
| 19     | 2.293             | 5.262 | 13.193 | 23.336 | 34.143 | 45.322  | 56.625  | 68.169  | 79.929  | 91.739  | 103.756 |
| 20     | 2.311             | 5.337 | 13.499 | 24.151 | 35.716 | 47.879  | 60.288  | 73.028  | 86.104  | 99.371  | 112.719 |
| 21     | 2.330             | 5.414 | 13.807 | 24.947 | 37.350 | 50.490  | 63.963  | 78.128  | 92.398  | 107.211 | 122.329 |
| 22     | 2.348             | 5.490 | 14.113 | 25.737 | 39.021 | 53.065  | 68.010  | 83.360  | 99.141  | 115.532 | 132.283 |
| 23     | 2.368             | 5.570 | 14.432 | 26.511 | 40.562 | 55.745  | 71.885  | 88.618  | 106.047 | 124.059 | 142.521 |
| 24     | 2.387             | 5.649 | 14.750 | 27.255 | 42.229 | 58.520  | 75.706  | 94.198  | 113.143 | 132.912 | 153.504 |
| 25     | 2.407             | 5.730 | 15.074 | 28.004 | 43.769 | 61.183  | 79.925  | 99.620  | 120.537 | 142.039 | 164.454 |
| 26     | 2.428             | 5.811 | 15.405 | 28.744 | 45.356 | 63.869  | 84.015  | 105.320 | 127.755 | 151.694 | 176.172 |
| 27     | 2.449             | 5.892 | 15.735 | 29.502 | 46.841 | 66.613  | 88.183  | 111.193 | 135.550 | 161.214 | 188.127 |
| 28     | 2.470             | 5.977 | 16.071 | 30.282 | 48.402 | 69.287  | 92.187  | 117.020 | 143.367 | 171.000 | 200.244 |
| 29     | 2.491             | 6.065 | 16.424 | 31.059 | 49.851 | 71.885  | 96.272  | 122.999 | 151.255 | 181.313 | 213.135 |
| 30     | 2.509             | 6.153 | 16.772 | 31.866 | 51.366 | 74.453  | 100.617 | 128.781 | 159.101 | 191.585 | 225.787 |
| 31     | 2.534             | 6.240 | 17.130 | 32.672 | 52.775 | 77.172  | 104.523 | 134.709 | 167.289 | 202.202 | 239.122 |
| 32     | 2.557             | 6.332 | 17.501 | 33.502 | 54.335 | 79.783  | 108.640 | 140.839 | 174.900 | 212.000 | 252.180 |
| 33     | 2.580             | 6.428 | 17.872 | 34.338 | 55.807 | 82.180  | 112.598 | 146.468 | 183.402 | 223.233 | 265.238 |
| 34     | 2.603             | 6.517 | 18.240 | 35.144 | 57.358 | 84.670  | 116.492 | 152.281 | 191.288 | 233.378 | 279.121 |
| 35     | 2.626             | 6.606 | 18.666 | 36.087 | 58.910 | 87.125  | 120.372 | 158.201 | 199.123 | 244.362 | 292.083 |
| 36     | 2.651             | 6.715 | 19.053 | 37.010 | 60.559 | 89.451  | 124.079 | 163.774 | 206.587 | 254.672 | 305.855 |
| 37     | 2.678             | 6.822 | 19.474 | 37.915 | 62.070 | 92.196  | 128.083 | 169.262 | 215.009 | 265.334 | 319.522 |
| 38     | 2.701             | 6.926 | 19.875 | 38.816 | 63.903 | 94.941  | 131.651 | 174.683 | 223.010 | 275.104 | 332.344 |
| 39     | 2.731             | 7.028 | 20.327 | 39.768 | 65.666 | 97.678  | 135.691 | 180.059 | 229.777 | 286.062 | 344.910 |
| 40     | 2.757             | 7.139 | 20.784 | 40.823 | 67.331 | 100.431 | 139.833 | 185.654 | 237.495 | 295.811 | 357.836 |

Table 2

| 0.5         1         2         3         4         5         6         7         8         9           0         1.969         3.945         7.187         9.149         10.523         11.578         12.416         13.109         13.722         14.251           1         1.985         4.011         7.507         9.726         11.324         12.575         13.594         14.470         15.205         15.870           2         2.002         4.081         7.831         10.337         12.189         13.664         14.891         15.948         16.875         17.658 | 10<br>14.742<br>16.490<br>18.438<br>20.576<br>23.089<br>25.791<br>28.907<br>32.220<br>32.620 |
|--|--|
| 0         1.969         3.945         7.187         9.149         10.523         11.578         12.416         13.109         13.722         14.251           1         1.985         4.011         7.507         9.726         11.324         12.575         13.594         14.470         15.205         15.870           2         2.002         4.081         7.831         10.337         12.189         13.664         14.891         15.948         16.875         17.658   | 14.742<br>16.490<br>18.438<br>20.576<br>23.089<br>25.791<br>28.907<br>32.220                 |
| 1         1.985         4.011         7.507         9.726         11.324         12.575         13.594         14.470         15.205         15.870           2         2.002         4.081         7.831         10.337         12.189         13.664         14.891         15.948         16.875         17.658   | 16.490<br>18.438<br>20.576<br>23.089<br>25.791<br>28.907<br>32.220                           |
| 2 <b>2.002</b> 4.081 7.831 10.337 12.189 13.664 14.891 15.948 16.875 <b>17.658</b>   | 18.438<br>20.576<br>23.089<br>25.791<br>28.907<br>32.220                                     |
|  | 20.576<br>23.089<br>25.791<br>28.907<br>32.220   |
| 3 <b>2.019</b> 4.148 8.159 <i>10.970</i> 13.107 14.832 16.310 <i>17.575</i> 18.708 19.689  | 23.089<br>25.791<br>28.907<br>32.220   |
| 4 2.036 4.216 8.494 11.628 14.074 16.097 <b>17.839</b> 19.360 20.713 21.936  | 25.791<br>28.907<br>32.220   |
| 5 2.053 4.283 8.827 <b>12.310</b> 15.096 17.444 19.490 21.308 22.952 24.456  | 28.907<br>32.220   |
| 6 2.070 4.353 9.165 13.013 16.171 18.894 21.256 23.430 25.362 27.226   | 32.220   |
| 7 2.087 4.422 9.501 13.746 17.313 20.421 23.206 25.732 28.040 30.218   | 06.006   |
| 8 <b>2.104</b> 4.489 <b>9.840</b> 14.499 18.489 <b>22.054</b> 25.272 28.234 30.964 33.574  | 36.026   |
| 9 2.121 4.558 <b>10.169</b> 15.268 19.741 <b>23.779 27.476 30.926</b> 34.156 37.172  | 40.088   |
| 10 2.138 <b>4.629</b> 10.499 16.057 21.025 25.597 29.845 33.814 37.585 41.167  | 44.587   |
| 11 2.156 4.699 10.827 16.845 22.366 27.505 32.324 36.907 41.264 45.432   | 49.462   |
| 12 <b>2.173 4.768</b> 11.148 17.662 23.750 29.503 34.960 40.218 45.270 <b>50.108</b>   | 54.830   |
| 13 2.191 4.839 <b>11.459</b> 18.495 25.186 31.599 37.766 <b>43.731</b> 49.515 55.075   | 60.626   |
| 14 2.208 <b>4.910</b> 11.766 19.316 26.654 33.784 <b>40.685</b> 47.452 54.059 60.479   | 66.796   |
| 15 2.226 4.982 12.063 20.156 28.159 36.042 43.783 51.334 58.874 66.292   | 73.580   |
| 16 2.244 5.054 12.357 21.007 29.693 38.384 46.977 55.546 64.013 72.389   | 80.785   |
| 17 2.262 5.129 12.658 21.836 31.271 <b>40.794</b> 50.321 59.867 69.383 78.954  | 88.437   |
| 18 2.281 <b>5.202</b> 12.952 22.690 <b>32.865</b> 43.259 53.809 <b>64.434</b> 75.134 85.849  | 96.612   |
| 19 <b>2.299</b> 5.277 13.258 23.510 34.472 45.796 57.381 69.163 81.077 <b>93.128</b>   | 105.301  |
| 20 2.318 5.352 13.559 <b>24.320</b> 36.073 <b>48.377</b> 61.106 <b>74.019</b> 87.335 100.774   | 114.473  |
| 21 2.337 5.429 13.870 <b>25.126</b> 37.731 51.044 64.895 79.230 93.886 108.778   | 124.008  |
| 22 <b>2.356 5.508 14.178</b> 25.918 39.356 53.706 68.773 84.403 100.602 117.165  | 134.183  |
| 23 2.376 5.586 <b>14.500</b> 26.687 40.962 56.405 72.761 89.881 <b>107.664</b> 125.870   | 144.801  |
| 24 2.396 5.666 14.821 27.454 <b>42.584</b> 59.118 76.881 95.470 114.845 134.956  | 155.711  |
| 25 2.416 5.747 15.145 28.193 44.186 <b>61.858 80.943</b> 101.016 <b>122.308</b> 144.271  | 167.210  |
| 26 2.436 5.829 15.476 28.933 45.784 64.749 85.079 106.926 129.844 154.003  | 179.185  |
| 27 2.457 5.914 15.818 29.699 47.323 67.341 89.302 112.828 137.772 163.887  | 191.411  |
| 28 2.478 <b>5.999 16.162</b> 30.477 48.844 70.097 93.474 118.756 145.519 174.091   | 204.030  |
| 29 2.500 6.086 16.510 <b>31.264</b> 50.324 <b>72.781</b> 97.749 124.767 153.448 184.393  | 216.911  |
| 30 2.522 6.175 16.862 32.067 51.851 75.486 101.801 130.744 161.907 195.291   | 229.957  |
| 31 2.544 6.265 17.232 32.898 53.304 78.064 106.010 136.702 170.072 205.490   | 243.052  |
| 32 <b>2.567</b> 6.358 17.602 33.740 54.739 80.593 <b>110.140</b> 142.743 178.302 215.244   | 256.147  |
| 33 2.591 6.452 17.979 34.584 56.306 83.107 114.070 148.314 186.619 226.911   | 270.652  |
| 34 2.614 6.549 18.369 35.469 57.858 85.630 118.097 154.479 194.621 237.810   | 284,499  |
| 35 2.639 6.647 18.764 36.382 <b>59.472</b> 88.114 122.002 160.324 202.763 248.522  | 298.453  |
| 36 2.664 6.749 19.172 <b>37.323 61.102</b> 90.804 125.901 <b>165.892</b> 210.542 259.126   | 311.584  |
| 37 2.690 <b>6.853</b> 19.594 38.266 62.806 93.451 129.726 171.763 218.017 269.666  | 325,475  |
| 38 2.716 6.960 20.130 39.230 64.518 96.045 133.597 177.250 225.924 280.215   | 338.310  |
| 39 2.734 7.070 20.460 40.187 66.303 98.804 137.599 182.781 233.903 290.505   | 352.229  |
| 40 2.772 7.182 20.911 <b>41.215</b> 68.092 101.658 141.705 188.353 241.510 300.483   | 365.296  |



**Fig. 4.**  $F_s$  vs.  $\phi$  (*LB* and *UB*) at various depth ratios (*H*/*D* = 0.5–10).

study aims to simulate an idealized blowout stage when a hole occurs in a pipe, causing hydraulic pressure to be exerted on the soil layer above. The hole was circular (Fig. 1), and the soil above it was cohesivefrictional. The hydraulic pressure was set as uniform. The results of this study can be used in practical engineering to evaluate the uplift pressure due to the scenario in which the pipeline burst-related ground stability is under blowout conditions.

To calculate the passive internal trapdoor pressure ( $\sigma_i$ ) in cohesivefrictional soil under a blowout situation, Eq. (2) was employed. In this equation, the total compressive blowout pressure is equal to the cohesion, surcharge, and unit weight contributions. Noting similarity with the Terzaghi's bearing capacity approach, the respective factors for cohesion, surcharge, and unit weight are denoted as  $F_c$ ,  $F_s$ , and  $F_\gamma$ . Unlike the Terzaghi's bearing capacity factors, these three factors are functions of both the soil friction angle and soil cover depth ratio (H/D). The variation in these two parameters results in various outcomes for the three stability factors, and this relationship can be expressed as shown in Eq. (3):

$$F_c, F_s, F_\gamma = f\left(\phi, \frac{H}{D}\right) \tag{3}$$

where  $F_c$ , denotes the drained cohesion factor;  $F_s$ , denotes the surcharge factor;  $F_{\gamma}$ , denotes the soil unit weight factor; H/D, is the soil cover-depth ratio;  $\phi$ , is the soil internal friction angle.

FELA is a prominent technique used to solve a wide range of

**Table 3** $F_s$  vs.  $\phi$  (*LB*) at various depth ratios (*H*/*D* = 0.5–10).

| $\phi$ | H/D (F <sub>S</sub> , 1 | LB)   |        |        |        |        |         |         |         |         |         |
|--------|-------------------------|-------|--------|--------|--------|--------|---------|---------|---------|---------|---------|
|        | 0.5                     | 1     | 2      | 3      | 4      | 5      | 6       | 7       | 8       | 9       | 10      |
| 0      | 1.002                   | 1.004 | 1.007  | 1.009  | 1.010  | 1.012  | 1.012   | 1.013   | 1.014   | 1.015   | 1.016   |
| 1      | 1.037                   | 1.074 | 1.138  | 1.179  | 1.208  | 1.231  | 1.250   | 1.266   | 1.280   | 1.292   | 1.303   |
| 2      | 1.072                   | 1.146 | 1.280  | 1.369  | 1.436  | 1.488  | 1.532   | 1.570   | 1.603   | 1.633   | 1.660   |
| 3      | 1.108                   | 1.221 | 1.434  | 1.583  | 1.696  | 1.788  | 1.865   | 1.933   | 1.994   | 2.047   | 2.097   |
| 4      | 1.144                   | 1.298 | 1.599  | 1.820  | 1.992  | 2.134  | 2.257   | 2.364   | 2.459   | 2.549   | 2.630   |
| 5      | 1.181                   | 1.378 | 1.777  | 2.083  | 2.328  | 2.532  | 2.713   | 2.871   | 3.016   | 3.148   | 3.267   |
| 6      | 1.219                   | 1.461 | 1.968  | 2.373  | 2.706  | 2.988  | 3.240   | 3.466   | 3.627   | 3.863   | 4.044   |
| 7      | 1.258                   | 1.546 | 2.171  | 2.692  | 3.128  | 3.505  | 3.849   | 4.157   | 4.440   | 4.712   | 4.960   |
| 8      | 1.297                   | 1.634 | 2.386  | 3.040  | 3.597  | 4.095  | 4.541   | 4.957   | 5.347   | 5.707   | 6.046   |
| 9      | 1.337                   | 1.725 | 2.610  | 3.416  | 4.123  | 4.755  | 5.339   | 5.879   | 6.389   | 6.870   | 7.326   |
| 10     | 1.378                   | 1.818 | 2.852  | 3.828  | 4.698  | 5.494  | 6.241   | 6.928   | 7.588   | 8.225   | 8.819   |
| 11     | 1.420                   | 1.915 | 3.103  | 4.270  | 5.337  | 6.318  | 7.251   | 8.134   | 8.971   | 9.769   | 10.563  |
| 12     | 1.463                   | 2.016 | 3.368  | 4.744  | 6.030  | 7.240  | 8.395   | 9.488   | 10.553  | 11.571  | 12.567  |
| 13     | 1.507                   | 2.119 | 3.643  | 5.258  | 6.796  | 8.254  | 9.667   | 11.025  | 12.341  | 13.630  | 14.860  |
| 14     | 1.550                   | 2.226 | 3.931  | 5.805  | 7.611  | 9.367  | 11.065  | 12.736  | 14.359  | 15.945  | 17.515  |
| 15     | 1.597                   | 2.336 | 4.230  | 6.387  | 8.506  | 10.595 | 12.643  | 14.658  | 16.647  | 18.580  | 20.521  |
| 16     | 1.644                   | 2.450 | 4.538  | 6.998  | 9.479  | 11.932 | 14.337  | 16.777  | 19.203  | 21.549  | 23.886  |
| 17     | 1.692                   | 2.569 | 4.862  | 7.650  | 10.518 | 13.374 | 16.253  | 19.113  | 21.963  | 24.872  | 27.725  |
| 18     | 1.741                   | 2.690 | 5.202  | 8.337  | 11.610 | 14.995 | 18.307  | 21.729  | 25.144  | 28.584  | 32.031  |
| 19     | 1.792                   | 2.817 | 5.557  | 9.053  | 12.782 | 16.638 | 20.582  | 24.583  | 28.648  | 32.663  | 36.818  |
| 20     | 1.844                   | 2.948 | 5.925  | 9.811  | 14.039 | 18.464 | 23.000  | 27.651  | 32.426  | 37.235  | 42.129  |
| 21     | 1.897                   | 3.084 | 6.313  | 10.601 | 15.395 | 20.432 | 25.630  | 31.076  | 36.566  | 42.271  | 48.002  |
| 22     | 1.951                   | 3.224 | 6.716  | 11.424 | 16.802 | 22.498 | 28.494  | 34.733  | 41.173  | 47.725  | 54.484  |
| 23     | 2.007                   | 3.369 | 7.139  | 12.275 | 18.280 | 24.727 | 31.576  | 38.744  | 46.119  | 53.737  | 61.615  |
| 24     | 2.066                   | 3.519 | 7.582  | 13.163 | 19.799 | 27.100 | 34.839  | 42.990  | 51.509  | 60.388  | 69.183  |
| 25     | 2.125                   | 3.676 | 8.044  | 14.091 | 21.458 | 29.595 | 38.376  | 47.591  | 57.345  | 67.340  | 77.791  |
| 26     | 2.187                   | 3.840 | 8.527  | 15.049 | 23.166 | 32.243 | 42.007  | 52.541  | 63.473  | 75.169  | 87.094  |
| 27     | 2.250                   | 4.008 | 9.036  | 16.063 | 24.914 | 34.998 | 46.025  | 57.755  | 70.272  | 83.233  | 97.133  |
| 28     | 2.315                   | 4.185 | 9.565  | 17.118 | 26.781 | 37.922 | 50.077  | 63.253  | 77.268  | 92.291  | 107.803 |
| 29     | 2.382                   | 4.368 | 10.116 | 18.252 | 28.708 | 40.970 | 54.522  | 69.240  | 85.057  | 101.712 | 119.100 |
| 30     | 2.453                   | 4.558 | 10.704 | 19.423 | 30.720 | 44.091 | 59.142  | 75.445  | 92.983  | 111.844 | 131.644 |
| 31     | 2.525                   | 4.757 | 11.315 | 20.671 | 32.766 | 47.458 | 64.005  | 82.075  | 101.648 | 122.645 | 144.660 |
| 32     | 2.600                   | 4.965 | 11.957 | 21.972 | 34.961 | 50.838 | 69.018  | 88.919  | 110.614 | 133.999 | 158.739 |
| 33     | 2.677                   | 5.180 | 12.631 | 23.348 | 37.265 | 54.449 | 74.227  | 96.227  | 120.153 | 146.095 | 173.555 |
| 34     | 2.758                   | 5.406 | 13.332 | 24.769 | 39.728 | 58.211 | 79.620  | 103.779 | 130.418 | 159.104 | 189.677 |
| 35     | 2.841                   | 5.640 | 14.082 | 26.268 | 42.334 | 62.108 | 85.504  | 111.816 | 140.696 | 171.902 | 206.236 |
| 36     | 2.928                   | 5.886 | 14.852 | 27.877 | 44.977 | 66.260 | 91.441  | 120.241 | 151.658 | 185.727 | 223.410 |
| 37     | 3.020                   | 6.148 | 15.691 | 29.615 | 47.934 | 70.593 | 97.426  | 128.785 | 162.781 | 201.272 | 241.787 |
| 38     | 3.115                   | 6.418 | 16.565 | 31.408 | 50.969 | 75.255 | 104.169 | 137.728 | 174.701 | 216.861 | 261.168 |
| 39     | 3.240                   | 6.699 | 17.473 | 33.321 | 54.212 | 79.873 | 111.121 | 147.108 | 187.488 | 232.440 | 281.027 |
| 40     | 3.317                   | 7.003 | 18.454 | 35.319 | 57.598 | 85.280 | 118.265 | 157.128 | 200.385 | 249.389 | 302.188 |

#### Table 4

| $\phi$ | H/D (F <sub>S</sub> , l | UB)   |        |        |        |        |         |         |         |         |         |
|--------|-------------------------|-------|--------|--------|--------|--------|---------|---------|---------|---------|---------|
|        | 0.5                     | 1     | 2      | 3      | 4      | 5      | 6       | 7       | 8       | 9       | 10      |
| 0      | 1.002                   | 1.004 | 1.007  | 1.009  | 1.010  | 1.012  | 1.012   | 1.013   | 1.014   | 1.015   | 1.016   |
| 1      | 1.037                   | 1.074 | 1.139  | 1.180  | 1.209  | 1.232  | 1.251   | 1.267   | 1.280   | 1.293   | 1.304   |
| 2      | 1.072                   | 1.147 | 1.281  | 1.371  | 1.438  | 1.491  | 1.535   | 1.573   | 1.606   | 1.636   | 1.663   |
| 3      | 1.108                   | 1.222 | 1.436  | 1.586  | 1.700  | 1.793  | 1.871   | 1.939   | 2.000   | 2.054   | 2.103   |
| 4      | 1.144                   | 1.299 | 1.602  | 1.825  | 1.998  | 2.142  | 2.265   | 2.374   | 2.470   | 2.558   | 2.641   |
| 5      | 1.182                   | 1.379 | 1.781  | 2.089  | 2.336  | 2.544  | 2.726   | 2.887   | 3.032   | 3.165   | 3.289   |
| 6      | 1.220                   | 1.462 | 1.973  | 2.381  | 2.716  | 3.004  | 3.259   | 3.487   | 3.695   | 3.890   | 4.068   |
| 7      | 1.258                   | 1.547 | 2.177  | 2.702  | 3.143  | 3.527  | 3.874   | 4.187   | 4.473   | 4.745   | 4.990   |
| 8      | 1.298                   | 1.635 | 2.393  | 3.052  | 3.619  | 4.120  | 4.577   | 4.996   | 5.387   | 5.754   | 6.095   |
| 9      | 1.338                   | 1.727 | 2.622  | 3.433  | 4.147  | 4.790  | 5.380   | 5.925   | 6.440   | 6.928   | 7.393   |
| 10     | 1.379                   | 1.821 | 2.863  | 3.847  | 4.729  | 5.535  | 6.291   | 6.997   | 7.660   | 8.295   | 8.911   |
| 11     | 1.421                   | 1.918 | 3.116  | 4.294  | 5.372  | 6.375  | 7.318   | 8.212   | 9.058   | 9.878   | 10.666  |
| 12     | 1.464                   | 2.019 | 3.381  | 4.774  | 6.075  | 7.302  | 8.470   | 9.583   | 10.663  | 11.691  | 12.689  |
| 13     | 1.508                   | 2.122 | 3.658  | 5.288  | 6.841  | 8.327  | 9.758   | 11.136  | 12.472  | 13.771  | 15.055  |
| 14     | 1.553                   | 2.229 | 3.947  | 5.838  | 7.675  | 9.457  | 11.186  | 12.875  | 14.532  | 16.142  | 17.698  |
| 15     | 1.599                   | 2.340 | 4.245  | 6.426  | 8.576  | 10.686 | 12.769  | 14.814  | 16.831  | 18.814  | 20.766  |
| 16     | 1.646                   | 2.455 | 4.558  | 7.044  | 9.547  | 12.046 | 14.520  | 16.977  | 19.410  | 21.791  | 24.212  |
| 17     | 1.694                   | 2.573 | 4.881  | 7.702  | 10.592 | 13.505 | 16.438  | 19.363  | 22.271  | 25.187  | 28.067  |
| 18     | 1.743                   | 2.696 | 5.223  | 8.393  | 11.709 | 15.105 | 18.536  | 21.976  | 25.448  | 28.928  | 32.426  |
| 19     | 1.794                   | 2.823 | 5.577  | 9.119  | 12.908 | 16.814 | 20.813  | 24.878  | 28.944  | 33.091  | 37.307  |
| 20     | 1.846                   | 2.954 | 5.951  | 9.879  | 14.173 | 18.672 | 23.308  | 28.029  | 32.849  | 37.740  | 42.657  |
| 21     | 1.900                   | 3.090 | 6.337  | 10.673 | 15.520 | 20.655 | 25.987  | 31.478  | 37.104  | 42.787  | 48.701  |
| 22     | 1.954                   | 3.231 | 6.744  | 11.504 | 16.950 | 22.767 | 28.871  | 35.200  | 41.707  | 48.382  | 55.155  |
| 23     | 2.011                   | 3.377 | 7.168  | 12.359 | 18.447 | 25.023 | 31.973  | 39.217  | 46.766  | 54.495  | 62.523  |
| 24     | 2.069                   | 3.529 | 7.613  | 13.252 | 20.014 | 27.418 | 35.298  | 43.560  | 52.193  | 61.160  | 70.430  |
| 25     | 2.129                   | 3.686 | 8.079  | 14.179 | 21.663 | 29.925 | 38.831  | 48.231  | 58.082  | 68.370  | 79.059  |
| 26     | 2.191                   | 3.850 | 8.566  | 15.143 | 23.381 | 32.634 | 42.616  | 53.246  | 64.417  | 76.176  | 88.511  |
| 27     | 2.255                   | 4.019 | 9.075  | 16.169 | 25,168 | 35,422 | 46.591  | 58,566  | 71.353  | 84.586  | 98.542  |
| 28     | 2.320                   | 4.196 | 9.610  | 17.237 | 27.032 | 38.373 | 50.833  | 64.221  | 78,596  | 93.655  | 109.661 |
| 29     | 2.388                   | 4.380 | 10.170 | 18.364 | 28,956 | 41.443 | 55.296  | 70.295  | 86.234  | 103.400 | 121.162 |
| 30     | 2.458                   | 4.572 | 10.756 | 19.557 | 30.993 | 44.671 | 59.936  | 76.542  | 94.479  | 113.669 | 133.797 |
| 31     | 2.531                   | 4,772 | 11.370 | 20.880 | 33.094 | 48.008 | 64.868  | 83.255  | 103.365 | 124.601 | 147.222 |
| 32     | 2,607                   | 4,980 | 12.015 | 22,118 | 35,299 | 51,485 | 69.972  | 90.361  | 112.637 | 136.487 | 161.925 |
| 33     | 2.685                   | 5.196 | 12.695 | 23.501 | 37.630 | 55.099 | 75.287  | 97.690  | 122.288 | 148.501 | 176.997 |
| 34     | 2.766                   | 5.423 | 13.407 | 24,981 | 40.164 | 58.836 | 80.853  | 105.382 | 132.395 | 161.527 | 193.068 |
| 35     | 2.850                   | 5.661 | 14 159 | 26.511 | 42.737 | 62.894 | 86 603  | 113.438 | 143,136 | 175.324 | 210 009 |
| 36     | 2.938                   | 5.981 | 14.950 | 28,141 | 45.470 | 66,994 | 92.612  | 121.832 | 154.196 | 189.434 | 227.185 |
| 37     | 3.030                   | 6.171 | 15.786 | 29.848 | 48.378 | 71.524 | 98.871  | 130.545 | 165.856 | 204.478 | 246.235 |
| 38     | 3.125                   | 6.444 | 16.663 | 31.662 | 51,472 | 76.111 | 105.564 | 139.759 | 177.939 | 220.063 | 266.187 |
| 39     | 3 224                   | 6.732 | 17.592 | 33,609 | 54 764 | 81,110 | 112,609 | 149,176 | 190.694 | 236.396 | 286 687 |
| 40     | 3.328                   | 7.034 | 18 564 | 35.635 | 58,220 | 86 403 | 120.111 | 159.229 | 203 856 | 253.377 | 307.655 |
|        | 0.010                   | /     | 10.007 | 00.000 | 00.220 | 001,00 |         | 10,100  | 200.000 | 2001077 | 007.000 |



**Fig. 5.**  $F_{\gamma}$  vs.  $\phi$  (*LB* and *UB*) at various depth ratios (*H*/*D* = 0.5–10).

geotechnical stability problems. This is an effective approach for computing the limit load with a precise upper-lower bound solution. Sloan [16] discussed the historical development of FELA for assessing soil stability, starting from the earliest FELA initiatives that employed linear programming [17,18] up to the most recent important advancements that used non-linear programming [19–21]. OptumG2 is the most recently developed FELA program. This software has been used effectively to solve several stability problems in geotechnical engineering [22–24]. It was used to perform a parametric analysis in this study to establish UB and LB solutions for the drained passive circular trapdoor. Within OptumG2, the UB elements have three nodes that provide an unidentified velocity linear approximation, whereas the LB elements have three nodes that provide an unidentified stress linear approximation with stress discontinuity possibilities at the overlaying triangular edges. A perfectly plastic Mohr-Coulomb material was utilized in combination with a flow rule to replicate the solid components that constitute the drained soil. Further details on the FELA formulation can be found in Shiau and Al-Asadi [13].

Fig. 2 shows a typical numerical model, boundary condition, and adaptive mesh for  $F_{\gamma}$  analysis (H/D = 3). The drained passive circular trapdoor was placed under axisymmetric conditions, where the axial symmetry line was set on the left soil domain border. The model required only half of the circular trapdoor, owing to the axisymmetric assumption. The boundary conditions for the FELA analysis were set as follows: the two vertical borders were set as roller supports with no vertical motion restriction; the horizontal border (model base) was set as

Table 5 $F_{\gamma}$  vs.  $\phi$  (*LB*) at various depth ratios (*H*/*D* = 0.5–10).

| $\phi$ | $H/D(F_{p} LB)$ |       |        |        |        |         |         |         |         |         |          |  |
|--------|-----------------|-------|--------|--------|--------|---------|---------|---------|---------|---------|----------|--|
|        | 0.5             | 1     | 2      | 3      | 4      | 5       | 6       | 7       | 8       | 9       | 10       |  |
| 0      | 0.501           | 1.004 | 2.014  | 3.026  | 4.040  | 5.055   | 6.074   | 7.094   | 8.112   | 9.128   | 10.160   |  |
| 1      | 0.510           | 1.090 | 2.158  | 3.335  | 4.552  | 5.790   | 7.059   | 8.340   | 9.632   | 10.935  | 12.260   |  |
| 2      | 0.519           | 1.076 | 2.308  | 3.668  | 5.112  | 6.615   | 8.169   | 9.769   | 11.392  | 13.022  | 14.730   |  |
| 3      | 0.528           | 1.113 | 2.466  | 4.025  | 5.728  | 7.530   | 9.436   | 11.408  | 13.408  | 15.522  | 17.690   |  |
| 4      | 0.537           | 1.150 | 2.628  | 4.412  | 6.400  | 8.555   | 10.852  | 13.277  | 15.792  | 18.399  | 21.130   |  |
| 5      | 0.546           | 1.189 | 2.800  | 4.823  | 7.140  | 9.690   | 12.461  | 15.399  | 18.488  | 21.727  | 25.140   |  |
| 6      | 0.556           | 1.229 | 2.976  | 5.261  | 7.944  | 10.950  | 14.250  | 17.801  | 21.568  | 25.549  | 29.770   |  |
| 7      | 0.565           | 1.270 | 3.162  | 5.726  | 8.812  | 12.335  | 16.242  | 20.497  | 25.056  | 29.919  | 35.100   |  |
| 8      | 0.575           | 1.311 | 3.354  | 6.218  | 9.752  | 13.845  | 18.451  | 23.536  | 29.008  | 34.901  | 41.210   |  |
| 9      | 0.584           | 1.354 | 3.554  | 6.743  | 10.764 | 15.505  | 20.888  | 26.905  | 33.488  | 40.567  | 48.140   |  |
| 10     | 0.594           | 1.398 | 3.760  | 7.292  | 11.860 | 17.310  | 23.601  | 30.679  | 38.424  | 46.942  | 56.120   |  |
| 11     | 0.604           | 1.443 | 3.976  | 7.867  | 13.008 | 19.260  | 26.561  | 34.811  | 43.968  | 54.056  | 65.110   |  |
| 12     | 0.615           | 1.489 | 4.202  | 8.473  | 14.256 | 21.390  | 29.760  | 39.426  | 50.136  | 61.951  | 75.150   |  |
| 13     | 0.625           | 1.537 | 4.434  | 9.106  | 15.580 | 23.605  | 33.295  | 44.419  | 56.952  | 70.881  | 86.480   |  |
| 14     | 0.636           | 1.585 | 4.674  | 9.757  | 16.964 | 26.085  | 37.119  | 49.888  | 64.552  | 80.782  | 99.840   |  |
| 15     | 0.647           | 1.635 | 4.926  | 10.444 | 18.432 | 28.705  | 41.255  | 55.966  | 72.640  | 91.691  | 112.690  |  |
| 16     | 0.658           | 1.687 | 5.188  | 11.155 | 19.984 | 31.470  | 45.702  | 62.437  | 81.664  | 103.633 | 128.230  |  |
| 17     | 0.669           | 1.739 | 5.462  | 11.905 | 21.616 | 34.445  | 50.408  | 69.447  | 91.528  | 117.005 | 144.950  |  |
| 18     | 0.680           | 1.794 | 5.740  | 12.678 | 23.312 | 37.575  | 55.486  | 77.080  | 102.208 | 131.259 | 164.110  |  |
| 19     | 0.692           | 1.850 | 6.038  | 13.509 | 25.088 | 40.875  | 60.846  | 85.147  | 113.520 | 146.664 | 184.030  |  |
| 20     | 0.704           | 1.907 | 6.340  | 14.352 | 26.944 | 44.365  | 66.693  | 94.034  | 125.960 | 163.426 | 206.440  |  |
| 21     | 0.716           | 1.967 | 6.660  | 15.237 | 28.912 | 48.080  | 72.725  | 103.214 | 139.080 | 181.942 | 230.560  |  |
| 22     | 0.729           | 2.028 | 6.988  | 16.179 | 30.884 | 51.885  | 79.280  | 113.347 | 153.664 | 201.439 | 256.310  |  |
| 23     | 0.741           | 2.091 | 7.328  | 17.163 | 33.008 | 55.925  | 85.930  | 123.655 | 169.032 | 222.716 | 283.930  |  |
| 24     | 0.755           | 2.156 | 7.694  | 18.176 | 35.204 | 60.130  | 93.175  | 134.818 | 185.416 | 245.207 | 314.250  |  |
| 25     | 0.768           | 2.223 | 8.058  | 19.226 | 37.548 | 64.520  | 100.444 | 146.541 | 202.488 | 269.056 | 346.720  |  |
| 26     | 0.782           | 2.295 | 8.450  | 20.360 | 39.912 | 69.040  | 108.649 | 159.223 | 220.576 | 294.155 | 381.760  |  |
| 27     | 0.796           | 2.366 | 8.858  | 21.533 | 42.500 | 73.775  | 116.609 | 171.863 | 240.112 | 321.124 | 418.490  |  |
| 28     | 0.811           | 2.440 | 9.270  | 22.753 | 45.168 | 78.635  | 124.676 | 185.658 | 259.648 | 350.764 | 455.790  |  |
| 29     | 0.826           | 2.520 | 9.712  | 24.022 | 47.960 | 83.840  | 133.667 | 199.951 | 280.080 | 373.022 | 498.290  |  |
| 30     | 0.841           | 2.597 | 10.172 | 25.390 | 50.892 | 89.365  | 143.157 | 214.839 | 303.440 | 411.879 | 542.580  |  |
| 31     | 0.858           | 2.681 | 10.658 | 26.791 | 53.968 | 95.145  | 153.139 | 229.867 | 326.672 | 444.874 | 589.000  |  |
| 32     | 0.874           | 2.768 | 11.160 | 28.275 | 57.520 | 101.200 | 163.187 | 245.707 | 350.848 | 480.036 | 636.610  |  |
| 33     | 0.891           | 2.861 | 11.678 | 29.823 | 60.620 | 107.570 | 173.697 | 262.101 | 375.472 | 515.791 | 685.270  |  |
| 34     | 0.909           | 2.954 | 12.212 | 31.443 | 64.260 | 114.400 | 185.312 | 280.700 | 403.312 | 554.685 | 739.550  |  |
| 35     | 0.927           | 3.048 | 12.808 | 33.173 | 68.148 | 121.115 | 197.419 | 298.193 | 430.140 | 593.498 | 793.520  |  |
| 36     | 0.946           | 3.152 | 13.404 | 35.012 | 72.104 | 128.830 | 209.178 | 317.276 | 456.968 | 635.414 | 851.110  |  |
| 37     | 0.967           | 3.258 | 14.034 | 36.899 | 76.256 | 136.805 | 223.061 | 339.713 | 488.632 | 675.405 | 907.160  |  |
| 38     | 0.988           | 3.367 | 14.710 | 38.869 | 80.928 | 145.410 | 237.155 | 360.462 | 521.176 | 722.248 | 969.910  |  |
| 39     | 1.009           | 3.485 | 15.436 | 41.050 | 85.244 | 153.955 | 252.281 | 384.433 | 555.240 | 769.847 | 1036.530 |  |
| 40     | 1.031           | 3.609 | 16.170 | 43.224 | 90.572 | 163.845 | 268.055 | 408.810 | 592.816 | 821.493 | 1107.800 |  |

Table 6

| $F_{\gamma}$ vs. $\phi$ ( <i>UB</i> ) at various depth ratios ( <i>H</i> / <i>D</i> = 0.5) | 5–10). |
|--|--------|
|--|--------|

| $\phi$ | $H/D (F_{\gamma}, l)$ | UB)   |        |        |        |         |         |         |         |         |          |
|--------|-----------------------|-------|--------|--------|--------|---------|---------|---------|---------|---------|----------|
|        | 0.5                   | 1     | 2      | 3      | 4      | 5       | 6       | 7       | 8       | 9       | 10       |
| 0      | 0.501                 | 1.004 | 2.014  | 3.026  | 4.040  | 5.055   | 6.074   | 7.094   | 8.112   | 9.128   | 10.160   |
| 1      | 0.510                 | 1.039 | 2.158  | 3.335  | 4.552  | 5.790   | 7.059   | 8.340   | 9.632   | 10.935  | 12.260   |
| 2      | 0.519                 | 1.076 | 2.310  | 3.671  | 5.116  | 6.620   | 8.175   | 9.776   | 11.408  | 13.049  | 14.760   |
| 3      | 0.528                 | 1.113 | 2.468  | 4.031  | 5.732  | 7.545   | 9.442   | 11.415  | 13.440  | 15.549  | 17.990   |
| 4      | 0.537                 | 1.151 | 2.632  | 4.415  | 6.412  | 8.575   | 10.870  | 13.298  | 15.816  | 18.435  | 21.150   |
| 5      | 0.546                 | 1.190 | 2.802  | 4.829  | 7.156  | 9.715   | 12.497  | 15.448  | 18.536  | 21.790  | 25.190   |
| 6      | 0.556                 | 1.230 | 2.980  | 5.270  | 7.968  | 10.990  | 14.304  | 17.864  | 21.616  | 25.656  | 29.880   |
| 7      | 0.565                 | 1.271 | 3.166  | 5.741  | 8.488  | 12.385  | 16.333  | 20.609  | 25.184  | 30.054  | 35.250   |
| 8      | 0.575                 | 1.312 | 3.358  | 6.239  | 9.792  | 13.920  | 18.571  | 23.662  | 29.208  | 35.117  | 41.480   |
| 9      | 0.585                 | 1.355 | 3.560  | 6.764  | 10.812 | 15.595  | 21.044  | 27.087  | 33.664  | 40.809  | 48.550   |
| 10     | 0.595                 | 1.399 | 3.768  | 7.316  | 11.912 | 17.420  | 23.752  | 30.903  | 38.736  | 47.284  | 56.510   |
| 11     | 0.605                 | 1.444 | 3.984  | 7.900  | 13.088 | 19.390  | 26.771  | 35.084  | 44.376  | 54.550  | 65.580   |
| 12     | 0.615                 | 1.491 | 4.210  | 8.506  | 14.336 | 21.535  | 30.024  | 39.769  | 50.640  | 62.644  | 75.780   |
| 13     | 0.626                 | 1.538 | 4.444  | 9.145  | 15.668 | 23.835  | 33.601  | 44.846  | 57.592  | 71.673  | 87.240   |
| 14     | 0.636                 | 1.587 | 4.688  | 9.808  | 17.076 | 26.305  | 37.419  | 50.448  | 65.184  | 81.736  | 100.040  |
| 15     | 0.647                 | 1.637 | 4.940  | 10.492 | 18.572 | 28.955  | 41.603  | 56.499  | 73.528  | 92.725  | 113.910  |
| 16     | 0.658                 | 1.689 | 5.204  | 11.209 | 20.124 | 31.775  | 46.092  | 63.130  | 82.768  | 104.982 | 129.920  |
| 17     | 0.669                 | 1.742 | 5.476  | 11.953 | 21.776 | 34.770  | 50.936  | 70.266  | 92.768  | 118.103 | 147.180  |
| 18     | 0.681                 | 1.797 | 5.758  | 12.753 | 23.508 | 37.935  | 56.086  | 77.983  | 103.576 | 132.887 | 166.080  |
| 19     | 0.693                 | 1.853 | 6.054  | 13.572 | 25.292 | 41.280  | 61.615  | 86.176  | 115.320 | 148.741 | 186.940  |
| 20     | 0.705                 | 1.911 | 6.360  | 14.433 | 27.172 | 44.815  | 67.455  | 95.161  | 127.936 | 165.926 | 209.500  |
| 21     | 0.717                 | 1.970 | 6.680  | 15.333 | 29.120 | 48.540  | 73.649  | 104.629 | 141.448 | 184.406 | 233.930  |
| 22     | 0.730                 | 2.032 | 7.010  | 16.269 | 31.144 | 52.400  | 80.168  | 114.643 | 156.032 | 204.406 | 260.500  |
| 23     | 0.743                 | 2.095 | 7.358  | 17.256 | 33.268 | 56.505  | 87.101  | 125.385 | 171.560 | 225.791 | 289.050  |
| 24     | 0.756                 | 2.161 | 7.718  | 18.284 | 35.472 | 60.725  | 94.346  | 136.856 | 187.944 | 248.849 | 319.780  |
| 25     | 0.769                 | 2.229 | 8.092  | 19.358 | 37.796 | 65.160  | 101.921 | 148.606 | 205.568 | 273.174 | 352.680  |
| 26     | 0.783                 | 2.299 | 8.482  | 20.492 | 40.276 | 69.700  | 109.850 | 161.176 | 224.400 | 299.164 | 387.630  |
| 27     | 0.797                 | 2.372 | 8.890  | 21.662 | 42.812 | 74.455  | 118.247 | 174.307 | 243.672 | 326.978 | 425.050  |
| 28     | 0.812                 | 2.447 | 9.316  | 22.906 | 45.524 | 79.490  | 126.675 | 188.179 | 264.240 | 356.520 | 464.880  |
| 29     | 0.828                 | 2.525 | 9.760  | 24.193 | 48.360 | 84.765  | 135.678 | 202.535 | 286.056 | 386.808 | 507.320  |
| 30     | 0.843                 | 2.606 | 10.222 | 25.555 | 51.376 | 90.280  | 145.144 | 217.612 | 308.880 | 418.597 | 551.870  |
| 31     | 0.859                 | 2.690 | 10.708 | 26.986 | 54.496 | 96.140  | 154.916 | 233.074 | 331.936 | 453.966 | 598.410  |
| 32     | 0.876                 | 2.777 | 11.214 | 28.482 | 57.760 | 102.280 | 165.192 | 249.622 | 356.280 | 488.237 | 647.140  |
| 33     | 0.893                 | 2.868 | 11.744 | 30.054 | 61.252 | 108.765 | 176.224 | 266.513 | 381.928 | 525.063 | 699.320  |
| 34     | 0.911                 | 2.963 | 12.302 | 31.710 | 64.856 | 115.680 | 187.659 | 284.300 | 409.032 | 563.121 | 752.620  |
| 35     | 0.930                 | 3.061 | 12.888 | 33.452 | 68.788 | 122.880 | 193.619 | 303.088 | 436.784 | 604.191 | 807.420  |
| 36     | 0.949                 | 3.164 | 13.496 | 35.282 | 72.856 | 130.525 | 212.551 | 323.081 | 466.080 | 645.207 | 866.560  |
| 37     | 0.969                 | 3.272 | 14.144 | 37.217 | 77.140 | 138.605 | 226.044 | 344.433 | 497.248 | 688.957 | 926.520  |
| 38     | 0.990                 | 3.384 | 14.820 | 39.256 | 81.672 | 147.110 | 240.516 | 366.513 | 529.728 | 735.845 | 989.990  |
| 39     | 1.011                 | 3.501 | 15.536 | 41.416 | 86.508 | 156.175 | 255.732 | 390.399 | 564.840 | 785.000 | 1056.190 |
| 40     | 1.034                 | 3.625 | 16.284 | 43.680 | 91.572 | 165.775 | 271.957 | 415.511 | 601.976 | 836.745 | 1127.550 |



**Fig. 6.** Current study comparison with that of Shiau et al. [26] (LB and UB) at various depth ratios (H/D = 0.5-10) with  $\phi = 0^{\circ}$ .

a fixed support where both vertical and horizontal motion were restricted; lastly, the top ground surface was set as a free surface without restriction. Note that regarding the roller support stress boundary conditions, shear stresses are constrained to zero, whereas normal stresses are unconstrained. For a fixed support at the bottom boundary, both shear and normal stresses were constrained to zero. Model domain dimensions were determined to be sufficiently large to guarantee that the soil motions were accurately localized within the specified domain.

Moreover, the FELA program incorporates an adaptive mesh refinement feature, which was created by Ciria et al. [25], to mitigate errors and enhance finding accuracy. Adaptive meshing technique application, in which the number of elements is automatically increased in zones with large plastic shear strains, considerably improves simulation computational performance. To minimize the confining discrepancies between the UB and LB solutions, a load multiplier technique and adaptive mesh refinement were implemented [16].

As shown in Fig. 2, automated mesh adaptivity was conducted to compute the circular trapdoor drained passive stability UB and LB solutions. The sensitivity zone gradient allows for direct intense plastic shearing strain regional observation. Three adaptive iteration stages were used in all the studies as suggested in the software, ensuring that this value was adequate to generate a reliable outcome. The initial 3000-component mesh was gradually increased to a final 5000-component



Fig. 7. ANN model structure.

mesh over three iteration rounds.

## 3. Results and discussion

A series of parametric studies regarding the LB and UB analysis three stability factors  $F_c$ ,  $F_s$ , and  $F_\gamma$  were conducted using two dimensionless parameters, namely the cover-depth ratio (*H*/*D*) and drained frictional angle ( $\phi$ ). The selected parameters covered the *H*/*D* = 0.5–10 and  $\phi$  = 0–40 ranges, respectively.

Cohesion factor  $F_c$ , results for the H/D and  $\phi$  value ranges are shown in Fig. 3. Both UB and LB results are shown in the Figure. The confidence level with the produced results has been substantially increased by the fact that UB and LB results can bracket the ``true'' solutions within 1 %. It is recommended that future solutions using various techniques be compared with the results obtained in this study. In general, a non-linear relationship between  $F_c$  and  $\phi$  was observed, where the greater the  $\phi$ , the larger is the  $F_c$ . A larger gradient showing a strong rate of increase was also observed in the  $\phi = 30-40$  range. In addition, regarding the shallow trapdoor, the variation in  $\phi$  had little effect on  $F_c$  values. This can be explained by understanding material arching, particularly in deep trapdoors. There is insufficient length in shallow trapdoors for material arching to develop. The complete  $F_c$  result list is provided in Tables 1 and 2.

Regarding the surcharge factor  $F_s$ , numerical results on the drained frictional angle  $\phi$  effects in the H/D = 0.5-10 range are shown in Fig. 4. Similar to  $F_c$  (Fig. 3), a non-linear relationship between  $F_s$  and  $\phi$  was observed. For frictionless soils ( $\phi = 0$ ) under undrained conditions,  $F_s$  was exactly 1 for all H/D values. As H/D increased (trapdoor depth

increased), the soil arching phenomenon began to increase, especially when  $\phi$  increased from 10 to 40. However, negligible effects were reported at shallow depths such as H/D = 0.5, and 1, as shown in the Figure. The complete  $F_s$  result list is provided in Tables 3 and 4.

Finally, Fig. 5 shows the drained frictional angle  $\phi$  effects on  $F_{\gamma}$  at the various depth ratios (H/D = 0.5-10). Similar trends with  $F_c$  and  $F_s$  (see Figs. 3 and 4) were observed in this "passive" study. The deeper the trapdoor, the greater are the  $F_{\gamma}$  values. Moreover, the non-linear increasing  $F_{\gamma}$  values were most pronounced at greater depth ratios (H/D). The minimum 0.5  $F_{\gamma}$  value was obtained at  $\phi = 0$  and H/D = 0.5. The complete  $F_{\gamma}$  result list is provided in Tables 5 and 6.

However, to confirm the FELA results obtained in this study, a comparison was made with those of Shiau et al. [26]. In their study, a passive trapdoor three-dimensional stability factor was provided. The cohesion factor ( $F_c$ ) results were compared with those of the selected  $\phi = 0$  and H/D = 0.5-10 cases in the current study. Specifically, the two investigations exhibited excellent agreement for both the UB and LB solutions, as illustrated in Fig. 6, demonstrating that the proposed stability solutions are accurate and reliable.

## A simple example

An underground circular cavity in an urban area with a 100 kPa surcharge loading ( $\sigma_s = 100$  kPa) had a 2 m width *B* (or diameter *D*) and a 16 m cover depth (*H*). The soil was found to have a (c = 17 kPa) cohesion with a 16 kN/m<sup>3</sup> unit weight. The internal friction angle was set at 30°. The critical inner blowout pressure was determined using three stability factors.

Solution: For H/B = 8 and  $\phi = 30$ , Tables 1, 3, and 5 provide the LB values;  $F_c = 159.101$ ,  $F_s = 92.983$ , and  $F_\gamma = 303.440$ . Substituting all the parameters into Eq. (2),  $\sigma_t$  was calculated as 21,713.09 kPa. The actual computer analysis using these parameters gives a 21,944.08 kPa value, which is extremely close to that of the tabular solution. Thus, the tabular approach is both reliable and convenient, with differences within 1 %, suggesting that practical engineers can use it with confidence.

#### 4. ANN predictive model

Over previous years, several machine learning approaches have been developed and can be classified into four groups: neuron-based (ANN, ANFIS(adaptive-network-based fuzzy inference systems)), kernel-based (SVM (support vector machine), KNEA (kernel-based non-linear extension of Arps decline)), tree-based (M5Tree, XGBoost), and curve-based (MARS(multivariate adaptive regression splines)) models. Although the XGBoost or MARS models are considered better machine learning approaches [27–29], ANN is generally recognized as a productive statistical learning method for addressing regression and classification problems and providing explicit predictive equations. For instance, it has been extensively utilized in various fields of study, from construction management to structural analysis [30,31]. Geotechnology has played a vital role in predicting soil and structural comportment, such as slope stability [32], ring foundation uplift resistance [33], and pipeline pull-out capacity [34]. Thus, the ANN model was adopted in this study.

A typical ANN framework in which numerous layered nodes are simultaneously manipulated is shown in Fig. 7. The input layer is for the

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| nput | parameter | statistical | properties | for set | training, | testing, | and | validation |
|------|-----------|-------------|------------|---------|-----------|----------|-----|------------|
|      |           |             |            |         |           |          |     |            |

| Variable | Training | set |       |       | Testing s | Testing set |       |       |     | Validation set |       |       |  |
|----------|----------|-----|-------|-------|-----------|-------------|-------|-------|-----|----------------|-------|-------|--|
|          | Min      | Max | Mean  | SD    | Min       | Max         | Mean  | SD    | Min | Max            | Mean  | SD    |  |
| φ        | 0.0      | 40  | 20.39 | 11.72 | 0.0       | 40          | 20.43 | 11.70 | 0.0 | 40             | 17.78 | 12.21 |  |
| H/D      | 0.5      | 10  | 5.03  | 3.09  | 0.5       | 10          | 4.71  | 3.06  | 0.5 | 10             | 5.46  | 3.09  |  |

\*Note: SD, standard deviation.



Fig. 8. Convergency study – MSE and  $R^2$  versus the number of hidden neurons.

unprocessed dataset, whereas the hidden layers obtain all computations that need to be performed. Finally, the output layer generates the model predictions [35].

As the process began, a coincidental value was assigned to individual neuron weights and biases. These values were then modified after each iteration to improve model performance. In addition, the procedure included a comparison between the desired objective and the actual result as well as the loss value calculation. At each hidden node, the activation functions translated the weighted inputs and biases into values to be used in the following layer. Owing to its robust capacity to accelerate the training process, the hyperbolic tangent transfer function shown in Eq. (4) was chosen to calculate the hidden layer output. In addition, a wide variety of techniques, such as Levenberg–Marquardt (LM), stochastic gradient descent, and Bayesian regularization, were introduced for ANN optimization. As recommended in [36,37], the LM algorithm was employed to adjust the weight and bias numbers.

$$tansig(x) = tanh(x) = \frac{2}{1 + e^{-2x}} - 1$$
 (4)

Prediction = 
$$\sum_{i=1}^{N_h} W^{2,i} \operatorname{tansig}\left(\sum_{j=1}^J W^{1,i} x^j + b^{1,i}\right) + b^{2,i}$$
 (5)

All the results from the FELA method were used to construct the ANN models. The input parameters comprise the drained friction angle  $\phi$  and soil cover depth ratio H/D, whereas the output features comprise the LB and UB solution three stability factors  $F_c$ ,  $F_s$ , and  $F_\gamma$ . The ANN model analysis encompassed 451 design cases that corresponded to H/D depth ratios at (0.5, 1.0, 2.0, 3.0, 4.0, 6.0, 7.0, 8.0, 9.0, and 10.0) and  $\phi$  ranging from 0 to 40 (totaling 41 cases). Notably, 70 % of the data are used for the training set, 15 % for the validation set, and 15 % for the test

set. Specifically, all data for training ANN are listed in Tables 1–6, in which the bold numbers represent the test set, and the italicized numbers are used for validation. The four statistical data properties in each set, comprising boundaries, mean, and standard deviation, are listed in Table 7, revealing the two input parameter approximate values in the three groups.

The number of nodes effect in a model hidden layer is an important consideration when selecting an optimal ANN model. The mean squared error (MSE) and coefficient of determination ( $R^2$ ) were used to assess optimal ANN model effectiveness [38]. The relationships between the number of hidden neurons,  $R^2$ , and MSE for training (70 % of the data), validation (15 % of the data), testing (15 % of the data), and all (100 % of the data) are illustrated in Fig. 8. The numerical results showed a noticeable increase in  $R^2$  and a dramatic decrease in MSE when the number of hidden nodes was increased to seven. Thereafter, they remained approximately constant, despite slight fluctuations. Therefore, seven neurons were used in all analyses. The corresponding values for the seven neurons are  $R^2 = 0.99998$  and MSE = 0.47030.

The optimal model weight and bias values, as listed in Table 8, were used to develop accurate equations to estimate the three stability factors (UB and LB). The hyperbolic tangent function Eqs. (4) and (5) was applied to construct the forecasting function that considers the  $\phi$  and H/D input parameters. The formulae for calculating  $F_{cs}$ ,  $F_{ss}$ , and  $F_{\gamma}$  (LB and UB) are shown in Eqs. (6)–(11).

$$F_{c,LB} = 1.1767N_1 + 2.7713N_2 + 12.9184N_3 + 10.0937N_4 - 5.0884N_5 - 1.6165N_6 + 2.9652N_7 + 0.6282$$
(6)

| Neuron | Input variab. | les     |         | Output  |         |         |         |         |         |        |        |        |        |        |        |
|--------|---------------|---------|---------|---------|---------|---------|---------|---------|---------|--------|--------|--------|--------|--------|--------|
|        | $W^1$         |         | $b^1$   | $W^2$   |         |         |         |         |         | $b^2$  |        |        |        |        |        |
|        | φ             | D/H     |         | F       |         |         |         |         |         |        |        |        |        |        |        |
| 1      | 1.1786        | 0.9919  | -2.8154 | 1.1767  | 1.1934  | 2.1949  | 2.2006  | 2.8602  | 2.8631  | 0.6282 | 0.6403 | 1.7572 | 1.7615 | 2.1109 | 2.1130 |
| 2      | 0.3020        | 0.8066  | -0.7231 | 2.7714  | 2.7494  | 3.4828  | 3.4682  | 1.4415  | 1.4243  |        |        |        |        |        |        |
| 3      | -0.7221       | 0.2695  | 0.8450  | 12.9185 | 12.9753 | 1.7379  | 1.8026  | 10.6803 | 10.7605 |        |        |        |        |        |        |
| 4      | 0.6964        | -0.0273 | -0.6421 | 10.0937 | 10.1077 | 4.4450  | 4.4866  | 7.9057  | 7.9666  |        |        |        |        |        |        |
| 5      | -0.7325       | 0.4543  | 1.0060  | -5.0885 | -5.1286 | 0.6800  | 0.6495  | -4.5930 | -4.6255 |        |        |        |        |        |        |
| 6      | 0.1593        | 0.9393  | -0.8591 | -1.6165 | -1.6025 | -2.0105 | -1.9972 | -0.6669 | -0.6506 |        |        |        |        |        |        |
| 7      | -0.5917       | -0.3726 | 0.3939  | 2.9653  | 2.9590  | 2.9360  | 2.9439  | 2.3473  | 2.3605  |        |        |        |        |        |        |
|        |               |         |         |         |         |         |         |         |         |        |        |        |        |        |        |

Optimal ANN model weight and bias values (seven neurons).

Table 8

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$$F_{c,UB} = 1.1934N_1 + 2.7494N_2 + 12.9753N_3 + 10.1077N_4 - 5.1286N_5 - 1.6025N_6 + 2.9590N_7 + 0.6403$$
(7)

$$F_{s,LB} = 2.1949N_1 + 3.4828N_2 + 1.7379N_3 + 4.4450N_4 + 0.6800N_5 - 2.0105N_6 + 2.9360N_7 + 1.7572$$
(8)

$$F_{s,UB} = 2.2006N_1 + 3.4682N_2 + 1.8026N_3 + 4.4866N_4 + 0.6495N_5 - 1.9972N_6 + 2.9439N_7 + 1.7615$$
(9)

$$F_{\gamma,LB} = 2.8602N_1 + 1.4415N_2 + 10.6803N_3 + 7.9057N_4 - 4.5930N_5 - 0.6669N_6 + 2.3473N_7 + 2.1109$$
(10)

$$F_{\gamma,UB} = 2.8631N_1 + 1.4243N_2 + 10.7605N_3 + 7.9666N_4 - 4.6255N_5 - 0.6506N_6 + 2.3605N_7 + 2.1130$$
(11)

where:

$$N_{1} = \operatorname{tansig}\left(1.1786\phi + 0.9919\frac{H}{D} - 2.8154\right)$$

$$N_{2} = \operatorname{tansig}\left(0.3020\phi + 0.8066\frac{H}{D} - 0.7231\right)$$

$$N_{3} = \operatorname{tansig}\left(-0.7221\phi + 0.2695\frac{H}{D} + 0.8450\right)$$

$$N_{4} = \operatorname{tansig}\left(0.6964\phi - 0.0273\frac{H}{D} - 0.6421\right)$$

$$N_{5} = \operatorname{tansig}\left(-0.7325\phi + 0.4543\frac{H}{D} + 1.0060\right)$$

$$N_{6} = \operatorname{tansig}\left(0.1593\phi + 0.9393\frac{H}{D} - 0.8591\right)$$

$$N_{7} = \operatorname{tansig}\left(-0.5917\phi - 0.3726\frac{H}{D} + 0.3939\right)$$

To validate the prediction model, Fig. 9 compares the stability factors obtained from the FELA method to those predicted by the ANN model in Eqs. (6)–(11). The three subfigures represent  $F_c$ ,  $F_s$ , and  $F_\gamma$  (LB and UB), respectively. In this Figure, the data points cluster more closely along the line y = x if the values obtained from the numerical approach and ANN predictor are in agreement. It is clear that the ANN model accuracy is proven by noting all data points on the centerline. This theory is supported by an  $R^2$  value of approximately 1.0, suggesting a high confidence level when using the seven-neuron model. Notably, this novel formula approximates the parameter values within the range provided, as previously detailed. Consequently, the results may be unreliable if the input values are outside this range.

Moreover, these proposed equations would be more persuasive if applied to input variables that did not appear in the previous set. Consequently, an additional dataset with 20  $\phi$  and H/D pairs, as shown in Table 9, was analyzed, and their FELA results are listed in Table 10. Thereafter, the  $R^2$  and MSE values were obtained based on the FELA results and ANN predictions described in Fig. 10. More specifically, the ANN model showed remarkable accuracy and the ability to make predictions using the new data, as indicated by its low MSE values of 0.4420 and 0.4399 for  $F_c$ , 0.5501 and 0.5852 for  $F_s$  and 0.7949 and 0.7322 for  $F_\gamma$  in the UB and LB solutions, respectively. The high  $R^2$  values in all cases (approximately 0.9998), emphasize the strong correlation between the ANN predictions and actual values. This underscores ANN model reliability and accuracy in predicting the results for an additional dataset within the training data range.

Garson's modified equation [39,40] was adopted to further assess

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Fig. 9. Comparisons between FELA results and ANN predictions.

Table 9The two input variable range with 20 additional cases.

| Parameter | Range of values                                  |
|-----------|--|
| φ<br>Η/D  | 5.5, 15.5, 25.5, 35.5<br>1.5, 2.5, 5.5, 7.5, 8.5 |
|           |  |

$$I_{j} = \frac{\sum_{m=1}^{m=N_{h}} \left( \frac{|w_{jm}^{jh}|}{\sum_{k=1}^{k=N_{h}} |w_{km}^{ih}|} \times |w_{mn}^{ho}| \right)}{\sum_{k=1}^{k=N_{h}} \left[ \sum_{m=1}^{m=N_{h}} \left( |w_{km}^{ih}| / \sum_{k=1}^{k=N_{h}} |w_{km}^{ih}| \right) \times |w_{mn}^{ho}| \right]}$$
(12)

the input parameter ( $\phi$  and H/D) effects on the stability factors. This is shown in Eq. (12), in which the optimal model weight and bias matrices are used for the assessment.

where  $I_j$  is the  $j_{th}$  input variable relative importance,  $N_i$  and  $N_h$  are the number of input and hidden neurons, respectively, W is the connection weight, and the superscripts *i*, *h*, and *o* are the input, hidden, and output layers, respectively, whereas the subscripts *k*, *m*, and *n* are the input, hidden, and output neurons, respectively.

The weight assigned to each input variable reflects its relative importance in calculating the output value. The greater the weight, the higher the influence. The results of this study, as presented by the relative importance index, are shown in Fig. 11. The results show that  $\phi$ 

**Table 10**  $F_c$ ,  $F_s$  and  $F_\gamma$  for 20 additional cases with various depth ratios (H/D = 1.5, 2.5, 5.5, 7.5, 8.5).

| ¢ | 5   | H/D | $F_{c}$ , LB | $F_c$ , UB | F <sub>s</sub> , LB | F <sub>s</sub> , UB | F <sub>7</sub> , LB | $F_{\gamma}$ , UB |
|---|-----|-----|--------------|------------|---------------------|---------------------|---------------------|-------------------|
| 5 | i.5 | 1.5 | 6.303        | 6.818      | 1.655               | 1.657               | 2.104               | 2.105             |
| 5 | .5  | 2.5 | 10.883       | 10.930     | 2.049               | 2.052               | 4.177               | 4.182             |
| 5 | .5  | 5.5 | 19.294       | 19.400     | 2.858               | 2.868               | 11.976              | 13.020            |
| 5 | .5  | 7.5 | 23.461       | 23.610     | 3.163               | 3.177               | 18.566              | 18.633            |
| 5 | .5  | 8.5 | 24.541       | 24.718     | 3.363               | 3.381               | 21.126              | 23.213            |
| 1 | 5.5 | 1.5 | 8.422        | 8.443      | 3.337               | 3.345               | 3.272               | 3.276             |
| 1 | 5.5 | 2.5 | 16.299       | 16.404     | 5.521               | 5.540               | 7.980               | 8.008             |
| 1 | 5.5 | 5.5 | 41.341       | 41.723     | 12.462              | 12.587              | 35.226              | 36.660            |
| 1 | 5.5 | 7.5 | 56.963       | 57.912     | 15.930              | 17.098              | 67.394              | 68.516            |
| 1 | 5.5 | 8.5 | 64.827       | 65.710     | 18.563              | 18.780              | 85.820              | 88.663            |
| 2 | 5.5 | 1.5 | 11.187       | 11.216     | 5.891               | 5.945               | 4.998               | 4.919             |
| 2 | 5.5 | 2.5 | 22.357       | 22.147     | 11.240              | 12.899              | 13.717              | 13.740            |
| 2 | 5.5 | 5.5 | 71.108       | 72.134     | 35.055              | 36.013              | 83.379              | 86.079            |
| 2 | 5.5 | 7.5 | 112.920      | 114.912    | 54.489              | 55.882              | 180.148             | 182.328           |
| 2 | 5.5 | 8.5 | 135.289      | 137.575    | 64.864              | 67.919              | 244.520             | 248.005           |
| 3 | 5.5 | 1.5 | 12.246       | 12.305     | 8.724               | 10.444              | 7.312               | 7.342             |
| 3 | 5.5 | 2.5 | 26.937       | 27.159     | 20.266              | 21.340              | 21.625              | 22.829            |
| 3 | 5.5 | 5.5 | 104.975      | 106.233    | 77.139              | 77.427              | 159.418             | 163.367           |
| 3 | 5.5 | 7.5 | 180.980      | 183.594    | 129.404             | 133.518             | 370.553             | 379.591           |
| 3 | 5.5 | 8.5 | 225.833      | 230.410    | 160.460             | 165.963             | 521.192             | 533.716           |



Fig. 10. Comparisons between FELA results and ANN predictions with 20 additional cases.



Fig. 11. The two input variables ( $\phi$  and H/D) relative importance index.

is the most critical parameter, with a 55.46 % relative importance index, compared to 44.54 % for the *H/D* ratio. It is crucial that neither  $\phi$  nor the *H/D* ratio should be ignored in practical analyses, because of the high importance index values.

#### 5. Conclusion

This study successfully examined passive circular trapdoor blowout stability using axisymmetry. This problem is analogous to an underground hydrogen storage simulation under extreme blowout pressures. Three conventional stability factors were investigated using the principle of superposition and UB and LB FELA. A series of parametric results for studying the cover-depth ratio and soil internal friction angle effects were presented using design charts and tables, which can be further used to determine the critical blowout pressures under various design conditions. An example was provided to demonstrate how practical solutions can be obtained for drained passive circular trapdoors in cohesivefrictional soil.

The investigation was continued using the latest ANN approach to provide a predictive model using a large FELA result dataset. It was concluded that the optimal ANN model could provide an accurate three stability factor prediction and evaluate the critical blowout pressure final prediction given the input parameters in the investigated ranges. Therefore, this study is of practical significance to the underground engineering community.

## **Ethics Statement**

Not applicable because this work does not involve the use of animal or human subjects.

### **Declaration of Competing Interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

#### Data availability

The datasets used and/or analyzed in the current study are available from the corresponding author upon reasonable request.

#### Acknowledgment

We acknowledge Ho Chi Minh City University of Technology (HCMUT), VNU-HCM for supporting this study.

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