

# The TESS–Keck Survey. XIII. An Eccentric Hot Neptune with a Similar-mass Outer Companion around TOI-1272

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#### Abstract

We report the discovery of an eccentric hot Neptune and a non-transiting outer planet around TOI-1272. We identified the eccentricity of the inner planet, with an orbital period of 3.3 days and  $R_{p,b} = 4.1 \pm 0.2 R_{\oplus}$ , based on a mismatch between the observed transit duration and the expected duration for a circular orbit. Using ground-based radial velocity (RV) measurements from the HIRES instrument at the Keck Observatory, we measured the mass of TOI-1272b to be  $M_{p,b} = 25 \pm 2 M_{\oplus}$ . We also confirmed a high eccentricity of  $e_b = 0.34 \pm 0.06$ , placing TOI-1272b among the most eccentric well-characterized sub-Jovians. We used these RV measurements to also identify a non-transiting outer companion on an 8.7 day orbit with a similar mass of  $M_{p,c} \sin i = 27 \pm 3 M_{\oplus}$  and  $e_c \leq 0.35$ . Dynamically stable planet–planet interactions have likely allowed TOI-1272b to avoid tidal eccentricity decay

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despite the short circularization timescale expected for a close-in eccentric Neptune. TOI-1272b also maintains an envelope mass fraction of  $f_{env} \approx 11\%$  despite its high equilibrium temperature, implying that it may currently be undergoing photoevaporation. This planet joins a small population of short-period Neptune-like planets within the "Hot Neptune Desert" with a poorly understood formation pathway.

Unified Astronomy Thesaurus concepts: Exoplanets (498); Eccentricity (441); Hot Neptunes (754)

Supporting material: machine-readable table

#### 1. Introduction

The solar system consists of eight planets from three size categories: terrestrial (0.4–1.0  $R_{\oplus}$ ), ice giant (3.9–4.0  $R_{\oplus}$ ), and gas giant (9.5–11.2  $R_{\oplus}$ ). They are spread out across a 30 au radial expanse and, with the exception of Mercury, their orbits are nearly circular. All three of these solar system-based patterns (distributions of planet sizes, orbit spacing, and orbital eccentricity) are contradicted by known exoplanetary systems. The prime Kepler mission (Borucki et al. 2010) revealed that the most common exoplanet sizes are between those of Earth and Neptune (1.0–3.9  $R_{\oplus}$ ; super-Earths/mini-Neptunes) in addition to a significant population with sizes between those of Uranus and Saturn (4.0–9.4  $R_{\oplus}$ ; super-Neptunes or sub-Saturns). Moreover, planetary orbits interior to Mercury's orbit are common, as well as orbits with eccentricities of e > 0.1(>60% of known planets, NASA Exoplanet Archive 2022). Such broad demographics demonstrate a variety of possible outcomes to planet formation.

However, there are certain planet characteristics that are less common, even with observational biases accounted for. These include the dearth of extremely high-eccentricity planets at short orbital periods, the "gap" in planet radius between super-Earths and mini-Neptunes at P < 100 days (Fulton et al. 2017), and the paucity of short-period Neptunian planets (Mazeh et al. 2016). The latter was first proposed as a natural consequence of photoevaporation by planet characterization studies (Lopez & Fortney 2013; Owen & Wu 2013). The resulting "Hot Neptune Desert" implies that for intermediate-size planets of  $\sim 10-100$  $M_{\oplus}$  and  $\sim 2-6 R_{\oplus}$ , an inefficient formation pathway or an efficient mass loss mechanism sharply differentiates Neptunes from Jupiters at periods of  $\lesssim 5$  days. Owen & Lai (2018) proposed that the upper and lower boundaries of this sparse region of  $M_p$ -P and  $R_p$ -P parameter space can be mostly explained by limitations from either eccentricity decay of larger planets or photoevaporation of smaller planets. The handful of observations of atmosphere-stripped Neptunian cores in the desert further supports this hypothesis (e.g., TOI-849b; Armstrong et al. 2020), but many questions remain surrounding the formation pathways of such planets.

Eccentricity further complicates the long-term evolutionary history of sub-Jovians on compact orbits. To date, only eight planets with sizes of 2.0–6.0  $R_{\oplus}$  and  $M_p < 100 M_{\oplus}$  have been found to have well-constrained eccentricities of e > 0.2, the greatest outlier being Kepler-1656b at  $e \approx 0.84 \pm 0.01$  (Brady et al. 2018). Only two of these planets, however, have orbital periods of P < 5 days. Hot Jupiter-size planets tend to have longer tidal circularization timescales and more massive cores that can retain their H/He envelopes during close-in periastron passage, but hot sub-Jovians are more susceptible to eccentricity decay and atmospheric loss. Consequently, the population of hot, eccentric Neptunes with  $\gtrsim 10\%$  H/He envelope mass fraction is small, consisting only of a handful of planets including HAT-P-11b (Yee et al. 2018) and GJ 436b (Lanotte et al. 2014).

In this paper, we discuss TOI-1272b, the latest Neptune to join the sparse population of hot, eccentric sub-Jovians. Leveraging the "photoeccentric" methodology outlined by Dawson & Johnson (2012) and Kipping et al. (2012), we identified TOI-1272b as a candidate for high eccentricity based on a mismatch between the observed transit duration and the expected duration for a circular orbit. We used this technique as a pre-filter to vet for high-eccentricity candidates based on photometry alone, motivating follow-up radial velocity observations. Similar photometric modeling methods have been applied to Kepler target samples (Kane et al. 2012; Van Eylen & Albrecht 2015; Xie et al. 2016; Van Eylen et al. 2019), but those studies were not followed up by radial velocity campaigns. We present TOI-1272 as the second system from our photoeccentric pre-filter study of TOIs, in association with the planetary demographics work being carried out by the TESS-Keck Survey collaboration (TKS; Chontos et al. 2022).

We introduce the TOI-1272 system and discuss the transit profile modeling that we used to identify TOI-1272b as an eccentric planet candidate from photometry (Section 2). We also describe our follow-up radial velocity (RV) observations (Section 3) and analyze our spectroscopic measurements to characterize the properties of the host star, including stellar variability and age (Section 4). From our dense RV data set, we confirm the high eccentricity of TOI-1272b and detect the presence of a non-transiting outer planet (Section 5). Finally, we explore the long-term stability of this system through various dynamical criteria, which we use to further constrain our eccentricity measurements (Section 6). We also place this system in context within the Hot Neptune Desert (Section 7) and consider possible formation and evolution pathways for TOI-1272b and other hot Neptunes.

# 2. TOI-1272b: A High-eccentricity Candidate

# 2.1. Photometry

TOI-1272 was observed by TESS with 2 minute cadence photometry in sectors 15, 16, and 22 between UT 2019 October 10 and 2020 May 11. The time-series photometry was processed by the TESS Science Processing Operations Center pipeline (SPOC; Jenkins et al. 2016), which first detected the periodic transit signal of TOI-1272b with a wavelet-based, noise-compensating matched filter (Jenkins 2002; Jenkins et al. 2010). An initial limb-darkened transit model fit was performed (Li et al. 2019) and the signature passed a suite of diagnostic tests described by Twicken et al. (2018), leading to the selection of this target as a TESS Object of Interest (TOI).

We accessed the pre-search data conditioning simple aperture photometry (PDC-SAP; Stumpe et al. 2012, 2014; Smith et al. 2012) through the Mikulski Archive for Space Telescopes (MAST), stitching together the light curves from individual TESS sectors into a single time series using Lightkurve (Lightkurve Collaboration et al. 2018). We performed outlier rejection, normalization, and detrending of the full light curve following the procedures outlined in MacDougall et al. (2021). We then searched for transits using a box least squares (BLS; Kovács et al. 2002) transit search to recover the same planetary signal detected by SPOC with signal-to-noise ratio (S/N) = 23.3. We subtracted the known transits and applied the BLS search again but identified no additional periodic transit events.

To confirm that the observed transit events were on target and not the result of a background source, we referenced additional ground-based time-series photometry taken for TOI-1272. Independent observations were collected with MuS-CAT2 (Narita et al. 2019) at a pixel scale of 0."44 in g, r, i, and  $z_s$  filters on UT 2020 February 28 and again ~1 year later with MuSCAT (Narita et al. 2015) at a pixel scale of 0."36 in g, r, and  $z_s$  filters on UT 2021 May 8. These detections confirmed that the expected transit was on target and presented no evidence of nearby eclipsing binaries. This target has one neighbor listed in Gaia Data Release 2 (DR2) within 30". At a separation of 8."45 and  $\Delta G = 5.93$ , the neighbor contributes <1% dilution to the light curve, which was already corrected for in the photometric data products that we used.

## 2.2. Photometric Transit Model

We characterized the planetary transit signal using a photometric light-curve model to determine whether TOI-1272b was a candidate for high eccentricity. We made this determination by comparing the planet's observed transit duration (*T*; mid-ingress to mid-egress) to the expected duration for a circular orbit  $T_{\rm circ}$ . The ratio of these two values can be used to assess the orbital geometry of a transiting planet through the geometric relation for transit duration given by Winn (2010):

$$T = \left(\frac{R_*P}{\pi a}\sqrt{1-b^2}\right) \frac{\sqrt{1-e^2}}{1+e\sin\omega}.$$
 (1)

Given the known period P = 3.316 days, fixed b = 0, and the stellar characterization from Section 4.1, TOI-1272b would have a transit duration of  $T_{\rm circ} = 0.094 \pm 0.004$  days if it were on a circular orbit. The observed transit, however, had a duration that was nearly 40% shorter than this at  $T_{\rm obs} \approx 0.06$ days. The short transit duration suggests either a higheccentricity orbit transiting near periastron or an orbit with a high impact parameter, motivating our follow-up analysis to constrain the true eccentricity.

To characterize the transit properties of TOI-1272b more precisely, we fit the available TESS photometry with the exoplanet package (Foreman-Mackey et al. 2021). The exoplanet package uses a Hamiltonian Monte Carlo algorithm that is a generalization of the No U-Turn Sampling method (Hoffman & Gelman 2014; Betancourt 2016). We used this model to generate samples from the posterior probability density for the parameters  $\{P, t_0, R_p/R_*, b, \rho_*, \sqrt{e} \sin \omega, \sqrt{e} \cos \omega, \mu, u, v\}$ , conditioned on the observed TESS light curve. Here,  $\mu$  is the mean out-of-transit stellar flux and  $\{u, v\}$ are quadratic limb-darkening parameters. The model used here follows that of MacDougall et al. (2021).

We applied weakly informative priors to each of the 10 model parameters, similar to those used by Sandford & Kipping (2017). In particular, the prior used on our parameterization of eccentricity and argument of periastron



**Figure 1.** Top: transit models drawn from parameter posterior distributions (orange; 50 samples) for phase-folded TESS photometry of TOI-1272b. Expected transit shape for a circular orbit is shown in blue, modeled using median posterior distribution values for all other model parameters. Details regarding fitting procedure are discussed in Section 2.2. Bottom: residuals to our maximum a posteriori model.

 $\{\sqrt{e} \sin \omega, \sqrt{e} \cos \omega\}$  was uniform on both parameters, not accounting for transit probability or other astrophysically motivated considerations. Also, our prior on  $\rho_*$  was based on the stellar characterization discussed in Section 4.1. We fit the photometry of TOI-1272 with this model using 6000 tuning steps and 4000 sampling steps over four parallel chains. Figure 1 shows the final transit model sampled from the posteriors.

An independent fit to the MuSCAT2 transit photometry of TOI-1272b was performed and used to verify the results of our transit fit to the full TESS photometry (Figure 2). The raw MuSCAT2 data were reduced by the MuSCAT2 pipeline (Parviainen et al. 2019), which performed standard image calibration and aperture photometry, and modeled the instrumental systematics present in the data while simultaneously fitting a transit model to the light curve. We also applied our own transit model to the detrended MuSCAT2 photometry, achieving consistent posterior constraints on all transit parameters. The same process was repeated for independent transit photometry from MuSCAT, producing similar results.

## 2.3. Eccentricity Constraints from Photometry

The photometrically constrained eccentricity posterior distribution that we measured for TOI-1272b from { $\sqrt{e} \sin \omega$ ,  $\sqrt{e} \cos \omega$ } was consistent with our high-eccentricity hypothesis, yielding a 1 $\sigma$  range of e = 0.18-0.60 and an  $\omega$  suggestive of a transit near periastron. The individual posterior distributions of e and  $\omega$  are shown in Figure 3, along with their joint 2D posterior.

We do note, however, that our impact parameter distribution remains loosely constrained, with a  $1\sigma$  range of b = 0.19-0.73, peaking in density toward the upper end of this range (Figure 3). The similarly loose constraints on both *e* and  $\omega$ implied that our photometric characterization of the orbital



**Figure 2.** Transit photometry for two independent single transits measured by the MuSCAT2 and MuSCAT instruments, plotted with 10 minute binning and photometric fits by the corresponding instrument pipeline. Horizontal dashed lines indicate the expected transit depth. Top: combined photometry from MuSCAT2 g, r, i, and  $z_s$  bands, observed on UT 2020 February 28. Bottom: photometry from MuSCAT g, r, and z bands, observed on UT 2021 April 8.

geometry was complicated by  $e-\omega-b$  degeneracy, as can be seen in the 2D joint posterior distributions in Figure 3. Nevertheless, the potential for a high eccentricity combined with the expected Neptune-like size of the planet and its short orbital period made TOI-1272b a prime target for follow-up radial velocity observations.

## 3. Spectroscopic Follow-up

We obtained a high-S/N template spectrum of TOI-1272 with the HIRES instrument at the Keck Observatory (Vogt et al. 1994) on UT 2020 June 11 with an S/N of 282 pixel<sup>-1</sup> at 5000 Å. We also collected 62 spectra of TOI-1272 between UT 2020 February 5 and UT 2021 November 27 (Table 1). On average, the observations had a spectral resolution of R = 50,000, using a median exposure time of 900 s at 5500 Å. Along with the RVs, we also measured the stellar activity S-index S<sub>HK</sub> for all 62 Keck/HIRES observations using the observed strengths of the Ca II H and K lines in our spectra, following the methods of Isaacson & Fischer (2010).

For the RV observations, a heated cell of gaseous iodine was included along the light path just behind the entrance slit of the spectrometer, imprinting a dense forest of molecular absorption lines onto the observed stellar spectrum (Marcy & Butler 1992). These lines served as a wavelength reference for measuring the relative Doppler shift of each spectrum and tracking variations in the instrument profile using the standard forward-modeling procedures of the California Planet Search (Howard et al. 2010).

#### 4. Stellar Characterization

#### 4.1. Bulk Properties

Following the procedures outlined by MacDougall et al. (2021), we characterized the bulk properties of TOI-1272 by first inferring  $T_{\rm eff}$  and [Fe/H] from our Keck/HIRES template spectrum using SpecMatch-Synth (Petigura et al. 2017). We then modeled the stellar mass, radius, surface gravity,



**Figure 3.** Corner plot of exoplanet model posteriors for TOI-1272b, showing the effects of  $e^{-\omega-b}$  degeneracy on our transit fit. The best-fit value for eccentricity is given by  $e = 0.40^{+0.20}_{-0.22}$ . The argument of periastron  $\omega$  remained loosely constrained about 90°, suggesting a transit near periastron.

 Table 1

 Radial Velocity Measurements

Time (BJD)	$\frac{\text{RV}}{(\text{m s}^{-1})}$	RV Unc. $(m s^{-1})$	$S_{\rm HK}$
2,458,885.021035	11.00	1.68	0.315
2,458,904.925436	-0.66	1.55	0.277
2,458,911.896259	4.05	1.88	0.290
2,458,999.786695	4.78	1.51	0.304
2,459,003.840909	20.53	1.42	0.309
2,459,006.852128	-1.18	1.60	0.300
2,459,010.867973	4.47	1.55	0.294
2,459,024.775924	-3.86	1.58	0.300
2,459,024.829972	-3.96	1.36	0.295
2,459,024.883105	-6.08	1.70	0.302

**Note.** Only the first 10 Keck/HIRES RVs are displayed in this table. A complete list has been made available online.  $S_{HK}$  values were measured using procedures from Isaacson & Fischer (2010) with standard uncertainties of 0.001.

(This table is available in its entirety in machine-readable form.)

density, and age via stellar isochrone fitting with isoclassify (Berger et al. 2020; Huber et al. 2017). We report these values and their associated uncertainties in Table 2, accounting for small corrections due to model grid uncertainties discussed by Tayar et al. (2020). We note that the properties derived with isoclassify rely on Two Micron All Sky Survey (2MASS) *K*-band magnitude and Gaia parallax, also reported in Table 2. The properties that we measured were consistent with those reported to ExoFOP-TESS from two spectra obtained with the TRES instrument at the Whipple Observatory, analyzed using the Stellar Parameter Classification (SPC) tool (Buchhave et al. 2012, 2014).

Table 2		
TOI-1272 System Properties		

Parameter	Value	Notes
Stellar		
RA (deg)	199.1966	А
Dec (deg)	49.86104	А
$\pi$ (mas)	$7.24\pm0.021$	А
$m_G$	$9.6844 \pm 0.0004$	А
$m_K$	$9.70\pm0.02$	В
$T_{\rm eff}$ (K)	$4985 \pm 121$	С
[Fe/H] (dex)	$0.17\pm0.06$	С
$\log(g)$	$4.55\pm0.10$	С
$M_*~(M_{\odot})$	$0.851\pm0.049$	С
$R_* (R_{\odot})$	$0.788 \pm 0.033$	С
$\rho_* ({\rm g}{\rm cm}^{-3})$	$2.453 \pm 0.343$	С
age (Gyr)	$3.65_{-0.98}^{+4.17}$	D
$P_{*,\rm rot}$ (days)	$28.3\pm0.6$	Е
S <sub>HK</sub>	0.331	F
$\log R'_{\rm HK}$	-4.705	F
и	$0.39\pm0.05$	G
ν	$0.09\pm0.05$	G
$\mu$ (ppm)	$-4.3\pm36.2$	Н
$\gamma (m s^{-1})$	$0.7\pm0.7$	Н
$\sigma_{\rm jit}~({\rm m~s}^{-1})$	$5.6\pm0.6$	Н
Planet b		
P (days)	$3.31599 \pm 0.00002$	Н
$T_c$ (BJD – 2,457,000)	$1713.0253 \pm 0.0006$	Н
b	$0.45_{-0.21}^{+0.15}$	Н
$R_p (R_{\oplus})$	$4.14 \pm 0.21$	Н
$M_p(M_{\oplus})$	$24.6 \pm 2.3$	Н
$\rho_p (g \text{ cm}^{-3})$	$1.9\pm0.3$	Н
$K ({\rm m}{\rm s}^{-1})$	$12.6 \pm 1.1$	Н
a (au)	$0.0412 \pm 0.0008$	Н
e	$0.338\substack{+0.056\\-0.062}$	Н
$\omega$ (deg)	$123.6 \pm 11.5$	Н
$T_{\rm eq}$ (K)	$961\pm32$	Ι
Planet c		
P (days)	$8.689 \pm 0.008$	Н
$T_c$ (BJD – 2,457,000)	$1885.34 \pm 0.48$	Н
$M_p \sin i (M_{\oplus})$	$26.7 \pm 3.1$	Н
$K \text{ (m s}^{-1})$	$9.4 \pm 1.0$	Н
a (au)	$0.0783 \pm 0.0014$	Н
e	≲0.35	J
$\omega$ (deg)	$-80.8^{+97.4}_{-57.3}$	Н
$T_{\rm eq}$ (K)	$697 \pm 23$	I
r <sub>eq</sub> (ix)	$077 \pm 23$	1

Note. A: Gaia DR2, epoch J2015.5 (Gaia Collaboration et al. 2018); B: 2MASS (Skrutskie et al. 2006); C: derived with isoclassify; D: derived with stardate (Angus et al. 2019a); E: derived with TESS-SIP (Hedges et al. 2020); F: measured from Keck/HIRES template; G: derived with LDTK (Parviainen & Aigrain 2015); H: constrained from joint RV-photometry model with juliet (Espinoza et al. 2018; Kreidberg 2015; Fulton et al. 2018; Speagle 2020); I: calculated from other parameters assuming albedo  $\alpha = 0.3$ ; J: dynamically constrained with rebound (Rein & Liu 2012).

#### 4.2. Variability and Rotation

To properly detrend our RV data and interpret any planetary signals, we first needed to characterize the intrinsic stellar variability for TOI-1272. We measured stellar variability from the TESS 2 minute cadence SAP photometry where TOI-1272 was observed in three sectors, one of which partially overlapped with our RV observation baseline. Upon removing data that were flagged as being of poor quality,  $\geq 5\sigma$  outliers, or part of the TOI-1272b transit events, we measured the stellar

variability period from the trimmed SAP light curve using the TESS-SIP algorithm (Hedges et al. 2020). This systematicsinsensitive Lomb–Scargle periodogram (Angus et al. 2016) yielded a clear variability signal at  $28.3 \pm 0.6$  days, likely associated with stellar rotation. The corrected TESS-SIP light curve, Lomb–Scargle periodogram, and phase-folded light curve with a sinusoidal fit are shown in Figure 4.

The stellar variability observed in the TESS photometry of TOI-1272 also allowed us to derive the expected stellar activity-driven variability in our RV measurements using the FF' method (Aigrain et al. 2012). This method uses the lightcurve flux (F), its derivative (F'), an estimate of relative spot coverage ( $f \sim 0.005$  in this work), and a simple spot model to simulate activity-induced RV variability. We estimated that this stellar activity would produce an RV variability signal with semiamplitude  $K \approx 5.0$  m s<sup>-1</sup>, assuming a sinusoidal signal. Given the partial overlap of our RV baseline with that of the TESS photometry, we used this RV variability estimate as the foundation for our consideration of activity-driven RV signals in Section 5.2. By doing so, we implicitly assumed that the variability signal in the region of overlap could be extrapolated out to the entire data set. Based on the measured value of log(g)and the observed values of activity metrics  $S_{\rm HK}$  and  $\log R'_{\rm HK}$ , moderate stellar activity-driven RV jitter was also expected for TOI-1272 based on the classifications presented in Luhn et al. (2020),  $\sigma_{\rm jit} \gtrsim 2.5$  m s<sup>-1</sup>, consistent with our photometry-only estimate.

As a final consideration of stellar variability, we searched for periodic, activity-driven signals in the  $S_{\rm HK}$  data series for TOI-1272 using a Lomb–Scargle periodogram. We identified a significant 28.5 day signal, consistent with our stellar variability measurement from TESS-SIP (Figure 5). We also detected additional sub-significant  $S_{\rm HK}$  variability signals that did not correspond to any known sources. We consider the impact that activity may have on our RV measurements when constructing our RV-only model in Section 5.

## 4.3. Age

Given the short orbital period of TOI-1272b and the possibility of a high-eccentricity orbit, the age constraints for this system were valuable for interpreting the tidal circularization timescale of the transiting planet. Our isochrone fit using isoclassify yielded a poorly constrained age estimate of  $\sim$ 1–7 Gyr. This was consistent with a first-order analytical estimate of the age of TOI-1272, 3.1 Gyr, based on  $G_{\rm BP} - G_{\rm RP}$  color and stellar rotation period via gyrochronology (Angus et al. 2019b).

We took this analysis a step further by using stardate (Angus et al. 2019a) to combine stellar isochrone modeling with gyrochronology to precisely measure the stellar age. Running the stardate Markov Chain Monte Carlo (MCMC) sampler for  $10^5$  draws, we measured an age of  $3.65^{+4.17}_{-0.98}$  Gyr. While this age range remained broad and consistent with our isoclassify measurement, the increased median value and reduced uncertainty from stardate provided us with better constraints on the lower bound of the age of this system.

#### 5. Keplerian Modeling

## 5.1. RV Detection of Planets b and c

We searched for periodic signals in our RV data using the RVSearch pipeline (Rosenthal et al. 2021). We set Gaussian



Figure 4. Top: TESS light curve of TOI-1272 from sectors 15, 16, and 22. The gray points show the original TESS SAP light curve and the black points show the TESS-SIP corrected light curve that is used to extract the variability period. The vertical dashed lines mark the gaps between TESS sectors. Bottom left: Lomb-Scargle periodogram of the TESS-SIP corrected light curve. The orbital period and transit depth from the TOI catalog are listed at the top of the panel. Bottom right: phase-folded light curve based on the most significant period detected from the periodogram. The gray points show the TESS-SIP corrected photometry, the black points show the binned data, and the red curve is a sinusoidal fit to the phase-folded light curve. The period, amplitude, and their associated uncertainties from the best-fit sinusoidal function are listed at the top of the panel.



**Figure 5.** Lomb–Scargle periodogram search of TOI-1272  $S_{HK}$  data, identifying a significant 28.5 day variability signal consistent with the suspected stellar rotation period.

priors on the period  $P_b$  and time of conjunction  $T_{c,b}$  of the 3.3 day planetary signal known from photometry. We then used RVSearch to iteratively search the RV data for additional Keplerian signals across the period range from 2 to 4000 days. This search yielded an eccentric Keplerian fit with  $K \approx 12.6$  m

s<sup>-1</sup> at the known period and an outer 8.7 day Keplerian fit with  $K \approx 9.4 \text{ m s}^{-1}$  (Figure 6). Both signals surpassed our significance threshold, with false-alarm probabilities (FAPs) measured by RVSearch FAP  $\approx 10^{-4}$  and  $10^{-5}$ , respectively.

We corroborated the significance of the 8.7 day signal by performing an independent search of the RV data set using an  $l_1$ periodogram (Hara et al. 2017), which minimizes the aliasing seen in a general Lomb-Scargle periodogram by evaluating all frequencies simultaneously rather than iteratively. We implemented our  $l_1$  periodogram with jitter  $\sigma = 5.0 \text{ m s}^{-1}$ , correlation time  $\tau = 0$ , and maximum frequency 1.5 cycles/day across the period range from 1.1 to 1000 days. Both the 3.3 and 8.7 day signals were clearly detected by this  $l_1$  periodogram search, with consistent FAP values of  $\sim 10^{-4}$  and  $\sim 10^{-5}$ , respectively. Given the significance of the 8.7 day period and the lack of a corresponding signal in either the  $S_{\rm HK}$  activity data or photometric time series (see Section 4.2), we concluded that this Keplerian signal was of planetary origin. A close inspection of the phase-folded and detrended TESS photometry at the RVconstrained period and time of conjunction for the outer RV signal showed no evidence for a corresponding transit event.



**Figure 6.** Iterative Keplerian periodogram search of TOI-1272 RV data using RVSearch. We confirmed the 3.3 day transiting planet (top panel) and identified a significant 8.7 day period with no corresponding transits (middle panel).  $\Delta$ BIC was used to discriminate between models with additional Keplerians over a grid of periods (Bayesian information criterion; Schwarz 1978), corresponding to a significance threshold of FAP = 0.001 at the yellow dashed horizontal line. The bottom panel shows a sub-significant signal at a 14.1 day period, likely corresponding to  $P_{\rm rot}/2$ .

# 5.2. Additional RV Signals

While we did not identify any additional signals in our RV data that met our significance criteria, we did detect a subsignificant Keplerian signal at a 14.1 day period using both RVSearch and an  $l_1$  periodogram search. This signal persisted throughout our entire observing baseline and was detectable in the residuals to a preliminary two-planet RV fit with Keplerian modeling code RadVel (Fulton et al. 2018). We concluded that this signal was the first harmonic ( $P_{\rm rot}/2$ ) of the 28.3 day stellar rotation as measured from the  $S_{\rm HK}$  time series and TESS photometry. The  $P_{\rm rot}/2$  harmonic of a star's rotation period is known to induce strong periodic activity signatures such as this in RV time-series data (Boisse et al. 2011).

Preliminary RV modeling revealed no other RV signals and insignificant detections of a trend and curvature in our RV time series, providing no evidence of further companions. We also found an estimated RV jitter of  $\sigma \approx 5.5$  m s<sup>-1</sup>. This jitter measurement was consistent with both our *FF'* estimate of RV variability and the RV semiamplitude of the marginal 14.1 day signal ( $K = 4 \pm 1$  m s<sup>-1</sup>). Given the low significance of this additional signal and its sub-jitter amplitude, we chose to consider only the two planetary signals in our final RV models. We therefore interpreted the spectroscopic data for TOI-1272 to reveal two planetary signals (3.3 days and 8.7 days), with a sub-significant activity signal driven by stellar rotation ( $P_{rot}/2 \approx 14.1$  days).

## 5.3. RV-only Model

We performed a two-planet fit to the RV time series for TOI-1272 using RadVel, a Python package used to characterize planets from Keplerian RV signals by applying maximum a posteriori model fitting and parameter estimation via MCMC (Fulton et al. 2018). Our model consisted of two planetary Keplerian signals with periods of 3.3 and 8.7 days. We modeled the data by fitting the following free parameters for both planets:  $P, T_c, K, \sqrt{e} \cos \omega$ , and  $\sqrt{e} \sin \omega$ . Our model also included RV offset  $\gamma$  and RV jitter term  $\sigma$  to account for astrophysical white noise and instrumental uncertainty. The best-fit RV-only RadVel model confirmed the existence of two eccentric sub-Jovian mass planets orbiting TOI-1272, and we used these results to inform the priors for a joint RV– photometry model.

## 5.4. Joint RV-Photometry Model

We obtained the most precise planet parameters for the TOI-1272 system by performing global RV-photometry modeling using juliet (Espinoza et al. 2018), a robust tool for modeling both transiting and non-transiting exoplanets. We used juliet to jointly fit the radial velocities through RadVel and the transit photometry through batman (Kreidberg 2015), with proper handling of limb-darkening coefficients (Kipping 2013). Estimation and comparison of Bayesian evidences and posteriors was performed directly by the dynamic nested sampling package dynesty (Speagle 2020), one of several such tools offered through the juliet interface. Unlike the Monte Carlo algorithm used in our initial transit-only analysis, nested sampling algorithms break up complex posterior distributions into simpler nested slices, sampling from each slice individually then recombining the weighted results to reconstruct the complete posterior. This method becomes more efficient in the higher-dimensional posterior spaces of joint models.

We directly fit for each transit and Keplerian property with priors informed from our previous photometry-only and RVonly models. For the final global model, we fit for photometryonly properties { $R_p/R_*$ , b,  $\rho_*$ ,  $\mu$ , u, v}, joint properties { $P_b$ ,  $t_{0,b}$ ,  $\sqrt{e_b} \sin \omega_b$ ,  $\sqrt{e_b} \cos \omega_b$ }, and RV-only properties { $P_c$ ,  $t_{0,c}$ ,  $\sqrt{e_c} \sin \omega_c$ ,  $\sqrt{e_c} \cos \omega_c$ ,  $K_b$ ,  $K_c$ ,  $\gamma$ ,  $\sigma$ }. Our final measurements are included in Table 2 and the corresponding maximum a posteriori RV model is shown in Figure 7.

In summary, we measured mass constraints for TOI-1272 b and c at significance levels  $\sim 11\sigma$  and  $\sim 9\sigma$ , respectively,

reflecting the strengths of the two periodogram signals discussed in Section 5.1. We also measured a high eccentricity of  $e_b = 0.34 \pm 0.06$  for TOI-1272b, consistent within  $1\sigma$  with our photometry-only eccentricity constraint from Section 2.3. The eccentricity of the outer planet was loosely constrained to  $e_c = 0.12^{+0.1}_{-0.08}$ . We note, however, that a model fit with  $e_c = 0$  performed nearly identically to the eccentric model, suggesting that the eccentricity of TOI-1272c is only marginally significant. We discuss these constraints on eccentricity further in Section 6.1. Our global model also served to minimize degeneracies between e,  $\omega$ , and b and allowed us to obtain more precise b and  $R_{p,b}$  values than with our photometry-only model. Our loose posterior constraint on impact parameter from Figure 3 was improved to  $b = 0.45^{+0.15}_{-0.21}$ , subsequently yielding our final radius measurement of  $R_{p,b} = 4.14 \pm 0.21 R_{\oplus}$ .

## 6. System Dynamics

## 6.1. Eccentricity Constraints from Stability Requirements

Despite the compact architecture of the TOI-1272 system, both planets had moderate RV-constrained eccentricities that were inconsistent with zero to  $\sim 5\sigma$  and  $\sim 1\sigma$  significance, respectively. Such excited dynamics put TOI-1272 b and c at risk of dynamical instability if orbit crossing were to occur:

$$\frac{a_c(1-e_c)}{a_b(1+e_b)} > 1.$$
 (2)

Given our RV-constrained measurements of eccentricity and orbital separation in this system, we found the left-hand side of the above equation to be  $1.22 \pm 0.15$ , or  $<2\sigma$  from the orbit-crossing threshold. We note, however, that our confidence in long-term orbital stability based on this value is highly sensitive to our eccentricity uncertainties. Assuming a fixed true value of  $e_c = 0.05$ , this system would be firmly out of reach of geometric orbit crossing given its current configuration.

With the ambiguity in our orbit-crossing stability result, we also calculated the dynamical stability of the TOI-1272 system according to the stricter criterion from Petrovich (2015):

$$\frac{a_c(1-e_c)}{a_b(1+e_b)} - 2.4(\max\left(\mu_b,\,\mu_c\right))^{1/3} \left(\frac{a_c}{a_b}\right)^{1/2} > 1.15, \quad (3)$$

where  $\mu$  is  $M_p/M_*$ , drawn from our joint model results. This threshold marks an estimated empirical boundary in two-planet system stability, determined by applying a support vector machine algorithm to a large number of numerical integrations. Planet–planet interactions resulting in the ejection of a planet into the star or out of the system were considered by Petrovich (2015) in developing this criterion.

Systems that satisfy the condition in Equation (3) are expected to maintain dynamical stability for integrations out to at least  $10^8$  orbits of the inner planet. When computed for this system, we measured the left-hand side of Equation (3) to be  $1.1 \pm 0.15$ , or  $<1\sigma$  below the stated stability threshold of 1.15. Similar to the orbit-crossing criterion, TOI-1272 straddles the stability boundary for the Petrovich (2015) empirical threshold. We again note that a fixed outer planet eccentricity of  $e_c = 0.05$  would promote the long-term stability of the TOI-1272 system according this stability criterion.

We followed up these inconclusive analytical predictions of long-term stability with a full *N*-body treatment of the stability



**Figure 7.** (a) Best-fit radial velocity model (blue) for Keck/HIRES RV measurements (black) using Radvel (Fulton et al. 2018) in a joint RV-photometry model via juliet (Espinoza et al. 2018), with corresponding residuals shown below. (b), (c) Phase-folded views of the best-fit RV model for TOI-1272 b and c, with binned points shown in red.

of the TOI-1272 system. Drawing initial conditions from our RV-photometry model posteriors, we ran  $10^4$  N-body simulations with rebound (Rein & Liu 2012) for ~ $10^6$  orbits of the inner planet. We restricted the initialized eccentricities of our simulations to avoid starting on crossing orbits, and we considered a simulation to be "unstable" after an orbit-crossing event or close dynamical encounter. Overall, ~81% of simulations remained "stable" for the entirety of our integration time, suggesting that the eccentricities and masses measured from our RV model were largely consistent with a stable architecture on moderate timescales (Figure 8). Our rebound simulations also showed that stable configurations of this system exhibit Laplace–Lagrange oscillations in eccentricity with a secular timescale on the order of ~ $10^2$  yr.

While our  $e_b$  posterior remained mostly unchanged by this *N*-body model, our stability constraints on  $e_c$  allowed us to



**Figure 8.** Distribution of initialized  $e_b - e_c$  values for all rebound simulations of the TOI-1272 system. Green-blue contours show regions with the highest density of stable configurations (simulations lasting  $10^6$  orbits of the inner planet).

determine an upper bound of  $e_c \leq 0.35$ . Upon this redefinition of  $e_c$ , we inferred that the true eccentricity of TOI-1272c was likely in the lower tail of the acceptable range. Given that a RadVel model with  $e_c = 0$  performed nearly equivalently to the nonzero eccentricity model (Section 5.4), this interpretation is consistent with our RV-only analysis.

## 6.2. No Evidence for TTVs

Along with our *N*-body integration, we also used rebound to model the transit-timing variations (TTVs) expected to be observed in this system over a similar baseline to our TESS photometry (~215 days). We estimated a TTV O-C rms of  $0.3 \pm 0.3$  minutes, below our threshold of sensitivity for individual transits. We verified this empirically by modeling the TESS photometry with exoplanet, similar to Section 2.3 but this time including TTVs as an additional model parameter. From this fit, we measured a TTV O-C rms of  $2 \pm 2$  minutes, consistent with the estimate from rebound.

With the additional photometric observations from MuS-CAT, we extended our TTV search to a total photometric baseline of ~600 days. A fit to the single transit measured by MuSCAT yielded a transit mid-point of BJD – 2,457,000 = 2313.223, only ~3 minutes off from the predicted mid-point of 2313.221  $\pm$  0.003 and within the ~5 minute uncertainty of this prediction. The extended photometric baseline demonstrated again that the TTVs in this system are negligible, within ~1 $\sigma$  of showing no evidence for TTVs.

The lack of TTVs was also consistent with the nonresonant orbital period ratio between TOI-1272 b and c:  $P_c/P_b \approx 2.62$ . This period ratio is outside of the resonant width of any strong resonances, lying most closely to the 3:1 second-order mean motion resonance, with a ~14% difference in ratio. However, we cannot rule out the possibility of past planet migration leading to resonance-crossing, which could have played a role in the planet–planet excitation of  $e_b$  discussed briefly in Section 7.3.

## 6.3. Strong Tidal Eccentricity Decay

The age measurement of TOI-1272 from Section 4.3 is valuable when considering the potential tidal eccentricity decay of TOI-1272b. According to Millholland et al. (2020), which draws from Leconte et al. (2010), the timescale of orbital circularization due to tidal eccentricity damping for an eccentric orbit is given by

$$\tau_e = \frac{4}{99} \left(\frac{Q'}{n}\right) \left(\frac{M_P}{M_*}\right) \left(\frac{a}{R_P}\right)^5 \\ \times \left(\Omega_e(e)\cos\epsilon\left(\frac{\omega_{\rm eq}}{n}\right) - \frac{18}{11}N_e(e)\right)^{-1}.$$
 (4)

Here, the mean motion is given by  $n = \sqrt{GM_*/a^3}$  and the reduced tidal quality factor Q' can be rewritten as  $Q' = 3Q/2k_2$ , with specific dissipation function Q and tidal Love number  $k_2$  (Murray & Dermott 1999; Mardling & Lin 2004). We defined  $\omega_{eq}$  as the spin rotation frequency of TOI-1272b at equilibrium, which we found to be  $3 \pm 0.5$  day<sup>-1</sup> following the procedure outlined in Millholland et al. (2020). We assumed the obliquity  $\epsilon$  to be 0°. We have also introduced functions of eccentricity  $\Omega_e(e)$  and  $N_e(e)$  given by

$$\Omega_e(e) = \frac{1 + \frac{3}{2}e^2 + \frac{1}{8}e^4}{(1 - e^2)^5}$$
(5)

$$N_e(e) = \frac{1 + \frac{15}{4}e^2 + \frac{15}{8}e^4 + \frac{5}{64}e^6}{(1 - e^2)^{13/2}}.$$
 (6)

A typical Neptune-like planet is generally assumed to have a tidal quality factor of  $Q' \approx 10^5$ , but the true value is highly uncertain. Assuming this fixed value for Q' and drawing the other parameters in Equation (4) from our previous analysis, we estimated a circularization timescale of  $\tau_e \approx 0.21 \pm 0.09$  Gyr. This nominal value of  $\tau_e$  is  $>3\sigma$  below our age measurement of  $3.65^{+4.17}_{-0.98}$  Gyr, suggesting that TOI-1272b has experienced significant eccentricity decay due to tides. This is not reflected in the anomalously high eccentricity that we measured, suggesting that another mechanism must be driving the excited state of this system. We note, however, that Q' is highly uncertain and  $\tau_e \propto Q'$ , so a tidal quality factor of  $2 \times 10^6$  would make  $\tau_e$  consistent with the age of the system.

Continuing with the assumption of  $Q' \approx 10^5$ , we estimated the initial eccentricity that would have been needed for TOI-1272b to reach its currently observed  $e_b$  after 3.65 Gyr of tidal eccentricity decay. Assuming constant Q' and  $\tau_e$ , we followed the procedures of Correia et al. (2020) to derive the required post-formation eccentricity of  $e_b \approx 0.8$ . Without a significant restructuring of the TOI-1272 system architecture, however, such a high eccentricity would not have allowed for a stable companion at the orbital separation of TOI-1272c. Ruling out this "hot-start" scenario, we are left to consider whether the anomalously high eccentricity of the inner planet is due to an underestimated Q' or excitation by some other dynamical mechanism. We discuss such formation and evolution scenarios further in Section 7.3.



**Figure 9.** Hot Neptune Desert in  $R_p$ -P and  $M_p$ -P parameter space, where Neptune-like is defined as  $M_p < 100 M_{\oplus}$  and  $R_p = 2.0-6.0 R_{\oplus}$ . Data drawn from the NASA Exoplanet Archive (Akeson et al. 2013; NASA Exoplanet Archive 2022). TOI-1272 b and c are depicted as a green point (both panels) and a blue point (left panel), respectively. Relations dictating the upper and lower boundaries of the Hot Neptune Desert from Mazeh et al. (2016) are shown as black dashed lines. Left: mass-period distribution of all planets, with Neptune-like planets shown in red. Right: radius-period distribution of all planets, with Neptune-like planets shown in red and the  $R_p = 2 R_{\oplus}$  limit shown as a black dotted line.

## 7. Context in the Hot Neptune Desert

#### 7.1. Bulk Density and Core-envelope Fraction

TOI-1272b is a Neptune-like planet for which we measured a mass of 24.6  $\pm$  2.3  $M_{\oplus}$  and a radius of 4.1  $\pm$  0.2  $R_{\oplus}$ , yielding a density of 1.9  $\pm$  0.3 g cm<sup>-3</sup>. This system also contains a similar-mass outer companion ( $M_p \sin i = 26.7 \pm 3.1 M_{\oplus}$ ) that is not transiting. Planets in this size and mass range have been reported frequently in the literature; only a few of them also fall within the Hot Neptune Desert (Mazeh et al. 2016; Owen & Lai 2018). At moderate planet sizes ( $\sim$ 2–6  $R_{\oplus}$ ;  $M_p \leq$  100  $M_{\oplus}$ ) and low orbital separations ( $P \leq$  5 days), a relative paucity of planets has been observed.

The triangular regions of  $R_p-P$  and  $M_p-P$  parameter space shown in Figure 9 highlight this phenomenon, as defined by Mazeh et al. (2016). TOI-1272b can be seen here among the small subset of Neptunes that fall within this otherwise sparse parameter space. Some notable inhabitants of the Hot Neptune Desert include GJ 436b (Lanotte et al. 2014) and HAT-P-11b (Yee et al. 2018) along with more recent finds from TESS photometry including LP 714-47b (Dreizler et al. 2020) and TOI-132b (Díaz et al. 2020). While the the exact mechanism responsible for clearing out this  $R_p$ -P and  $M_p$ -P region remains unknown, some models support a combination of photoevaporation and tidal disruption following high-eccentricity migration (Mazeh et al. 2016; Lundkvist et al. 2016; Owen & Lai 2018).

Planets within the Hot Neptune Desert range from dense, atmosphere-poor mini-Neptunes to atmosphere-rich, "puffy" super-Neptunes. TOI-1272b lies in the middle of this spectrum, with an elevated density relative to the upper end of the Weiss & Marcy (2014) relation. We used a two-component composition model to determine the relative abundances of solid core and gaseous envelope for this dense Neptune, following the procedure of MacDougall et al. (2021). We interpolated over a 4D grid of stellar and planetary properties to derive the expected envelope mass fraction for TOI-1272b using the Lopez & Fortney (2014) planet structure models. Assuming an Earth-like core composition and a solar-composition H/He envelope, we estimated  $f_{\rm env} = 10.9\% \pm 2.0\%$  and a core mass of  $21.9 \pm 2.0 \ M_{\oplus}$ . Given the strong stellar irradiance experienced by this planet, with  $T_{\rm eq} \approx 960$  K (assuming albedo  $\alpha = 0.3$ ), TOI-1272b could have begun as a more atmosphererich Neptune similar to GJ 3470b (Kosiarek et al. 2019) and experienced subsequent atmosphere loss. TOI-1272b may then serve as a strong candidate for follow-up atmospheric observations, following the treatment of similar targets like those discussed by Crossfield & Kreidberg (2017).

The outer companion in this system, TOI-1272c, likely falls into the same size category as TOI-1272b, with  $M_{\rm p,c}$  sin  $i = 27.4 \pm 3.2 \ M_{\oplus}$ . However, since no transit was detected in TESS photometry, we were unable to make any claims regarding its density or composition. One might suppose that a sufficiently low-radius planet on an 8.7 day orbit could produce a transit signal below the detection threshold of S/N  $\approx$  7.1. Assuming a transit duration of  $T_{14} \approx 0.15$  days and the same noise properties as the TOI-1272b transit, this would require  $R_{\rm p,c} \lesssim 2.3 \ R_{\oplus}$  and  $\rho_{\rm p,c} \gtrsim 12.0 \ {\rm g \ cm^{-3}}$ . While this density is not entirely unreasonable (see, e.g., Kepler-411b; Sun et al. 2019), it is unlikely given the known sample of similar planets.

#### 7.2. Eccentricities

The eccentricity distribution of hot Neptunes was discussed in depth by Correia et al. (2020), who noted that such planets exhibit elevated eccentricities despite being on compact orbits. We reconsidered this claim using a more recent set of confirmed planet data from the NASA Exoplanet Archive (Akeson et al. 2013; NASA Exoplanet Archive 2022), including TOI-1272b in our sample. We considered Neptunes to have radii ~2–6  $R_{\oplus}$  and "hot" planets to have P < 5 days. Constraining our sample to only planets with eccentricity uncertainties less than 0.1 (Figure 10), we found that hot Neptunes (N = 17) displayed a broader eccentricity distribution than their longer-period counterparts (N = 75). We verified the distinction between the two distributions using a Kolmogorov– Smirnov (KS) test, finding  $p \approx 0.008$ . TOI-1272b contributed to this significant trend among hot Neptunes.



**Figure 10.** Eccentricity distribution of planets with eccentricity uncertainties of  $\sigma_e < 0.1$ , comparing shorter-period planets (blue) against longer-period planets (orange). The lines show kernel density estimation fits to the data of the corresponding color. Top: Jupiter-like planets (>6  $R_{\oplus}$ ). Bottom: Neptune-like planets (2–6  $R_{\oplus}$ ), including TOI-1272b (dashed gray line).

On the other hand, planets with radii >6  $R_{\oplus}$  showed the opposite trend, as can also be seen in Figure 10, verified by a KS test with  $p \ll 0.01$ . In this radius range, 66 planets had P < 5 days and 88 had  $P \ge 5$  days. We did not consider planets with radii <2  $R_{\oplus}$  in this analysis due to the low sample size of such planets with eccentricity uncertainties <0.1. However, a cursory examination of this small subset suggested similar eccentricity distributions between shorter- and longer-period planets in this size range.

While these findings are statistically significant based on KS tests given the current data, several confounding factors led us to determine that these eccentricity trends are suggestive rather than definitive at this time. These factors include the small sample size of hot Neptunes, the reliability of the data reported by the NASA Exoplanet Archive, and potential observational biases. Nonetheless, the possible disagreement between the eccentricity trend for hot Neptunes and that for hot Jupiters is an active area of research. The low eccentricities of hot Jupiters were consistent with the rapid tidal circularization timescales expected at lower semimajor axes. Conversely, hot Neptunes seem more likely to violate the rule.

A nominal empirically derived periastron distance of  $r_{\text{peri}} \approx 0.03$  au is often used to approximate the boundary of rapid tidal eccentricity decay, shown in Figure 11. Here, we see that only a small subset of well-characterized planets inhabit the high-eccentricity area of parameter space beyond this boundary, including TOI-1272b and a few other eccentric hot Neptunes. The well-studied planet GJ 436b is among these Neptunes with orbits that disagree with tidal circularization, making it a near-twin to TOI-1272b based on mass, radius, eccentricity, and period.

## 7.3. A Unique Formation and Evolution Pathway

The sparsity of the Hot Neptune Desert along with the counterintuitive trend in hot Neptune eccentricities suggests a unique evolutionary pathway for hot planets within the



**Figure 11.** Eccentricity distribution of planets with  $\sigma_e < 0.1$  (Neptune-like in red, other known planets in gray) as a function of orbital separation, showing TOI-1272 b and c in green and blue, respectively. A periastron distance of 0.03 au is shown as an empirical threshold for rapid tidal eccentricity decay. Three eccentric Neptunes are labeled for reference (Kepler-1656b; TOI-269b, Cointepas et al. 2021; GJ 436b).

Neptune size regime. Several studies have sought to explain the dearth of planets within the "desert" region of  $M_p$ -P and  $R_p-P$  parameter space. The leading hypothesis suggests a combination of photoevaporation (Owen & Wu 2013; Owen & Lai 2018) and high-eccentricity migration (Mazeh et al. 2016; Matsakos & Königl 2016). Interestingly, photoevaporation is also cited as a possible mechanism for maintaining nonzero eccentricities among hot Neptunes (Correia et al. 2020), along with planet-planet excitation (see, e.g., Jurić & Tremaine 2008; Chiang & Laughlin 2013) or an eccentric Kozai–Lidov (EKL) effect from a distant giant companion (Naoz 2016). The persisting eccentricities of some hot Neptunes could also simply be a result of Q' values underestimated by an order of magnitude or more, which would make them inconsistent with the Q' values measured for Neptune and Uranus through interior modeling.

An underestimated Q' could certainly be the case for TOI-1272b, contributing to a longer  $\tau_e$  and slower rate of eccentricity decay. TOI-1272b may also be undergoing significant photoevaporation given its  $f_{env}$  and close-in  $r_{peri}$ , contributing to both its location in the middle of the Hot Neptune Desert and its high eccentricity. However, TOI-1272b differs from the plausible formation and evolution pathways of other hot Neptunes due to the presence of a stable, nearby outer companion. Both high-eccentricity migration and perturbations from a distant companion through EKL effects are complicated by the presence of the mildly eccentric companion on an 8.7 day orbit. Such excitation mechanisms would have likely caused an orbit-crossing event and subsequent ejection of one or both planets.

Instead, we propose that, along with photoevaporation, TOI-1272b has experienced minor planet–planet excitation events with TOI-1272c, possibly involving close approaches or resonance-crossing events during migration (Ford & Rasio 2008). These events could have contributed to both the high eccentricity and possible inward migration of TOI-1272b into the Hot Neptune Desert region of parameter space, similar to the proposed evolution of mini-Neptune HIP-97166b (MacDougall et al. 2021). The elevated eccentricity of the inner planet may then persist in spite of strong tidal forces through Laplace–Lagrange oscillations that continue to force the eccentricity, as seen in our dynamical simulations mentioned in Section 6.1. However, additional considerations such as the relative inclination of the two planets may be necessary for a more detailed description of the dynamical evolution of this system.

## 8. Summary and Conclusions

In this work, we introduced a newly discovered planet within the Hot Neptune Desert around TOI-1272 with a 3.3 day orbital period. We predicted that this planet might have a high eccentricity based on a mismatch between the observed transit duration and the expected duration for a circular orbit upon modeling three sectors of transit photometry from TESS. We confirmed this high eccentricity with follow-up RV measurements and verified its stability through dynamical constraints, yielding  $e_b = 0.34 \pm 0.06$ . We also identified a non-transiting outer companion on an 8.7 day orbit, placing a limit on its eccentricity of  $e_c \lesssim 0.35$ . TOI-1272b is now one of only a handful of close-in Neptunes with a well-constrained high eccentricity. The high eccentricity of this inner planet persists in spite of strong tidal forces, likely as a result of either underestimated tidal quality factors for close-in exo-Neptunes or stable dynamical interactions with the outer planet that continue to pump the eccentricity. Nonetheless, the discovery of TOI-1272 b and c has boosted the sample size of a small and poorly understood class of planets, contributing to ongoing studies of hot Neptunes and eccentric short-period planets.

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Facilities: TESS, Keck/HIRES, MuSCAT, MuSCAT2

Software: We made use of the following publicly available Python modules: exoplanet (Foreman-Mackey et al. 2021), PyMC3 (Salvatier et al. 2016), theano (The Theano Development Team et al. 2016), LDTK (Parviainen & Aigrain 2015), RadVel (Fulton et al. 2018), RVSearch (Rosenthal et al. 2021), astropy (Astropy Collaboration et al. 2013, 2018), isoclassify (Huber et al. 2017), lightkurve (Lightkurve Collaboration et al. 2018), matplotlib (Hunter 2007), numpy (Harris et al. 2020), scipy (Virtanen et al. 2019a), TESS-SIP (Hedges et al. 2020), SpecMatch-Synth (Petigura et al. 2017), and pandas (McKinney 2010).

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