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A study on truss bolt mechanism in controlling stability of underground excavation and cutter roof failure --Manuscript Draft--

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A study on truss bolt mechanism in controlling stability of underground excavation and cutter roof failure

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Abstract The truss bolt reinforcement system has been used in controlling the stability of underground excavations in severe ground conditions and cutter roof failure in layered rocks especially in coal mines. In spite of good application reports, working mechanism of this system is largely unknown and truss bolts are predominantly designed based on past experience and engineering judgement. In this study, the reinforcing effect of the truss bolt system on an underground excavation in layered rock is studied using non-linear finite element analysis. Different indicators are defined to evaluate the reinforcing effects of the truss bolt system. Using these indicators one can evaluate the effects of a reinforcing system on the deformation, loosened area, failure prevention, horizontal movement of the immediate layer, shear crack propagation and cutter roof failure of underground excavations. Effects of truss bolt on these indicators reveal the working mechanism of the truss bolt system. To illustrate the application of these indicators, a comparative study is conducted between three different truss bolt designs. It is shown that the design parameters of truss bolt systems, including tie-rod

span, length, and angle of the bolts can have significant effects on the reinforcing capability of the system.

Keywords Truss bolt · Reinforcement · FEM · Stability indicators · Underground excavation · Ground control

1 Introduction

Nowadays, rock bolt systems are being extensively used in mining and civil engineering applications. These systems are a dominant part of the New Austrian Tunneling Method (NATM) and can be used as both temporary and permanent support (Brady and Brown 2005; Karanam and Dasyapu 2005; Osgoui and Oreste 2007; Maghous et al 2012). The common use of rock bolts is because of their flexibility, ease of use and fast installation (Hoek and Brown 1980; Brady and Brown 2005). However, in severe ground conditions and especially in response to cutter roof failure, conventional rock bolt patterns could be inadequate and risky to use. In these circumstances, Peng and Tang (1984) suggest using a special configuration of rock bolts called Truss Bolt systems.

Truss bolt, in its simplest form, consists of two inclined members at two top corners and one horizontal member on the roof. A common truss bolt system, known as the Birmingham truss, consists of two long cable bolts which are connected at the middle of the roof. Horizontal tension is applied by means of a turnbuckle at the connection point of the cables at the roof and transferring a compression to the rock (Gambrell and Crane 1986). A schematic view of the Birmingham truss is shown in Fig. 1.

One of the advantages of truss bolt systems is the ability to control the cutter roof failure. Cutter roof is a

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1 common type of failure in laminated rock formations in
2 flat roof excavations. In this type of failure, shear cracks
3 propagate from the corners of the roof and as they reach
4 the first bedding plane, a huge block separates from the
5 roof (Su and Peng 1987). Very good responses of truss
6 bolt have been reported in places that systematic rock
7 bolt failed to prevent cutter roof (Stankus et al 1996).

8
9 The successful applications of truss bolt have led re-
10 searchers to develop different truss bolt systems which
11 resulted in several patents (White 1969; Wahab Khair
12 1984; Seegmiller and Reeves 1990). Alongside with these
13 developments, several researchers initiated studies to
14 understand the mechanism of the truss bolt system
15 and presented a number of practical design schemes.
16 A number of these works has been done by means of
17 photoelastic study during 1970s and 1980s (Gambrell
18 and Haynes 1970; Neall et al 1977, 1978; Gambrell and
19 Crane 1986). In design schemes for truss bolt systems,
20 Sheorey et al (1973) statistically studied the effects of
21 position and thickness of blocking points to find the op-
22 timum value of these parameters. Based on several field
23 investigations, Cox and Cox (1978) proposed their de-
24 sign method by considering suspension and reinforcing
25 effect of truss bolt system. Neall et al (1978) proposed a
26 theoretical design approach on the basis of beam build-
27 ing theory of reinforcement systems and tabular over-
28 burden load. Wahab Khair (1984) carried out lab exper-
29 iments to understand the effects of truss bolt on a sim-
30 ulated roof beam. Zhu and Young (1999) proposed an-
31 alytical based equations to calculate the required mini-
32 mum horizontal tension and length of tie-rod for single
33 and multiple truss bolt systems. Most recently, Liu et al
34 (2005) published an analytical based design procedure
35 on the basis of a number of simplifying assumptions.
36 Further to these studies, some field investigation and a
37 small number of numerical analyses are available in this
38 field (Seegmiller and Reeves 1990; O'Grady and Fuller
39 1992; Stankus et al 1996; Li et al 1999; Liu et al 2001;
40 Cox 2003; Ghabraie et al 2012).

41
42 Despite these efforts in understanding the truss bolt
43 mechanism, the complicated effects of truss bolts on
44 load distribution around an underground excavation is
45 still largely unknown (Liu et al 2005; Ghabraie et al
46 2012). This lack of knowledge forces engineers to con-
47 sider large safety factors while using these schemes.

48
49 Understanding the mechanism of truss bolt system
50 on reinforcing the rock around an underground excava-
51 tion is the most important and the first step in obtain-
52 ing a practical, reliable and easy to use design scheme.
53 This paper is focused on understanding the mechanism
54 of truss bolt systems on stability of underground ex-
55 cavations and preventing cutter roof failure. For this
56 purpose, numerical modelling techniques are used in or-
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der to capture the complicated behaviour of truss bolt
systems. Once a comprehensive numerical model is es-
tablished, one can repeat numerous tests for varying
input parameters at relatively little extra cost.

In this paper, the finite element method (FEM) has
been used for numerical modelling, using ABAQUS as
the software package (ABAQUS 2010). An underground
excavation, containing bedding planes, several rock lay-
ers and an installed truss bolt system has been mod-
elled. For the purpose of evaluating the effects of truss
bolt on stability of an underground excavation, a num-
ber of stability indicators have been introduced. Us-
ing these indicators, the effects of truss bolt system on
reinforcing an underground excavation and preventing
the cutter roof failure have been studied. Three regu-
lar truss bolt pattern have been modelled to study the
effects of different parameters of the system. These pat-
terns have been chosen from several case studies in the
literature and adjusted to the dimensions of the model
in this study. Using the stability indicators and study-
ing the effects of each truss bolt pattern on the stability
of an underground excavation, mechanism and effects
of different design parameters have been derived. Re-
sults showed that depending on the pattern of truss
bolt system, areas of reinforcing effect around an exca-
vation change dramatically. A long span truss bolt with
short inclined bolts results in reinforcing the top side
areas of the tunnel while a short span truss bolt with
long inclined bolts produce an arch shape reinforced
area above the roof. In conclusion, truss bolt creates a
trapezoid reinforced area above the roof and between
inclined bolts in which an arch shape area is the major
area of reinforcement.

2 Preliminary Understanding of Truss Bolt Behaviour

Previous studies have pointed out that the effect of re-
inforcement on the rock material is to apply the con-
fining pressure, suspend unstable blocks and increase
the strength properties of rock (Lang 1961; Lang and
Bischoff 1984; Huang et al 2002; Li 2006). Among these,
applying the confining pressure is the most important
effect which is the basis of the systematic rock bolt pat-
terns (Li 2006). The applied compressive force tightens
the rock fragments together alongside with increasing
the strength characteristics of rock by increasing the
mean stress and decreasing the deviatoric stress. Any
prestressed rock bolt compresses and reinforces the rock
in its vicinity. In a systematic rock bolt pattern, the
bolts are placed close enough such that their reinforced
area overlaps and a compressed area is produced. This
area acts like a beam and carries the load to the sides

1 of the excavation (Lang and Bischoff 1982; Roy and
2 Rajagopalan 1997; Li 2006).

3
4 In truss bolt systems, the applied tension in the mid-
5 dle of the tie-rod creates areas of compression around
6 the tunnel. The preliminary understanding of the load
7 distribution around truss bolt is shown in Fig. 2. Re-
8 sults of the early photoelastic analysis and physical
9 modelling also confirmed the presence of a compressive
10 force which demolished the shear stress at the mid-
11 dle of the roof (Gambrell and Haynes 1970; Gambrell
12 and Crane 1986). Also, the two inclined members of
13 the truss system are able to create a compressive area
14 above the abutments. Reinforcing this area could be
15 very effective in controlling the horizontal movement of
16 rock layers in the areas prone to the cutter roof failure
17 (Stankus et al 1996).

21 3 Numerical Model

22
23 A typical underground excavation in a coal seam with
24 thickness of 2 m has been modelled. The tunnel is as-
25 sumed to be long enough to satisfy plain strain as-
26 sumptions. The model contains four bedding planes,
27 two above and two beneath the tunnel.

28
29 Slipping or sticking behaviour of bedding planes are
30 governed by the Coulomb friction model

$$31 \tau = \mu p \quad (1)$$

32
33 In this equation, τ is shear stress, μ is the coefficient of
34 friction on the plane of weakness ($\mu = \tan \phi$) and p is
35 the contact pressure. In this model, no penetration is al-
36 lowed and pressure can be mobilized if two surfaces are
37 in contact. The responses of the model and the bedding
38 surfaces have been verified with the analytical solutions
39 proposed by Brady and Brown (2005).

40
41 An elastic-perfectly plastic material model has been
42 used to model the intact rock material and the Mohr-
43 Coulomb yield function has been adopted as the failure
44 criterion. The model is capable of capturing separation
45 and slipping along the bedding planes. This material
46 behaviour has been verified by the analytical solution
47 proposed by Hoek et al (1998).

48
49 The pretensioned rock bolts (inclined bolts and hor-
50 izontal tie-rod) have been modelled by using preten-
51 sioned one dimensional truss elements. Inclined bolts
52 have been anchored by tightening the end node of the
53 rock bolt element to the rock (no separation is allowed).
54 By increasing deformation in rock around the tunnel,
55 because of the relative displacement of two ends of the
56 bolt elements, the amount of stress in truss elements
57 increases. This extra load on the reinforcement system
58 may exceed the ultimate strength of bolts (Hoek et al
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1998). To prevent this, the maximum allowable preten-
sion is chosen at 60% of the ultimate tensile strength
of the bolts. Strength parameters of bolts are shown in
Table 1.

Truss bolt patterns Three different typical truss bolt
patterns have been considered. These patterns are cho-
sen based on the proposed designs by several researchers
(Cox and Cox 1978; Liu et al 2005; Ghabraie et al 2012).
Design parameters in these models have been adjusted
to the dimensions of the tunnel in this study. These
parameters are shown in Fig. 1 and Table 2.

4 Stability Indicators

The behaviour of the rock after installing reinforcement
needs to be measured via defining some performance
indicators. For the scope of this study, these indicators
should be able to evaluate the reinforcing effect of the
truss bolt system, roof deflection and effects of truss
bolt on preventing cutter roof failure.

4.1 Reinforced Arch

After excavating a tunnel, redistribution of the in-situ
stress forms a pressurized arch above the tunnel. This
arch is stable and can carry the load to the sides of
the tunnel. The rock material beneath this arch is con-
sidered as loosened material (Fig. 3). This phenomenon
can be observed in almost all types of coherent rock for-
mations (Li 2006) and is proved by experience as well
as numerical analysis (Bergman and Bjurström 1984;
Huang et al 2002). Position of this arch changes dras-
tically by changing the in-situ stress distribution. High
horizontal in-situ stress is favourable in forming a closer
natural arch to the roof, i.e. smaller loosened area. It
should be noted, however, that extensive horizontal in-
situ stress has negative effects on cutter roof failure and
also causes stability problems in pillars.

Usually, the natural arch is positioned far above the
tunnel and the loosened area beneath it should be stabi-
lized (Li 2006). This can be achieved by either removing
or reinforcing the loosened rock. In coal mines, however,
where the shape of the tunnel is normally governed by
the shape of the coal layer, removing the loosened rock
is not an option and a suitable reinforcement system
should be designed (Fig. 3).

Choosing parameters of the reinforcement systems
to carry the load of the loosened area, without consid-
ering reinforcing effects of the system, normally results
in overdesign parameters. The load of the loosened area
can be used as only to achieve an upper limit (ultimate

capacity) for the parameters of the reinforcement system (Cox and Cox 1978). To have a safe and economic design, the reinforcing effect of truss bolt on the loosened rock area should be taken into account. By applying a new load distribution around the tunnel, truss bolt system reinforces the loosened area and repositions the natural roof arch which results in smaller loosened area (Ghabraie et al 2012).

For specifying the position of the reinforced arch, Huang et al (2002) used the concept of invert stress cone to find the natural arch position around an underground excavation. In their model the thickness of the arch has been governed by the direction of principal stresses. According to Huang et al (2002), reinforced arch is the area in which principal stresses are not in vertical or horizontal direction except on the apex of the arch. Another approach to specify the position of reinforced arch is to use the vertical deformation of the rock above the roof. In this approach, the reinforced arch is defined by the points with the closest amount of vertical deformation to a certain fraction of the maximum vertical displacement of the tunnel roof. This fraction is the amount of displacement which predicts the stable/unstable rock. This condition can be expressed as (Ghabraie et al 2012)

$$|d_i - (n \times d_{max})| = \text{Minimum} \quad (2)$$

where d_i is the vertical displacement at points above the roof in FE mesh, d_{max} is the maximum vertical displacement on roof and n is a fraction between 0 and 1. In this approach, $n \times d_{max}$ is a threshold (a certain amount of displacement) which predicts the area of the loosened rock. Areas with less deformation than this threshold are considered to be stable and vice versa. The fraction (n) can be chosen with respect to the sensitivity of the tunnel to displacement and can be different from case to case. In this study, $n = 50\%$ has been chosen which implies that areas with less than 50% of the maximum displacement on the roof are loosened area. The output of this method is a line which connects all the points resulting from Eq. 2. It should be noted that this approach does not necessarily predict the actual area of loosened rock and is only used to define a basis for comparing different designs.

Using $n = 50\%$, the position of the reinforced arch and area of the loosened rock for different truss bolt patterns have been derived. These results are shown in Fig. 4. It can be seen that truss bolt system repositions the reinforced arch and reduces the area of loosened rock around a tunnel under hydrostatic in-situ stress. These results highlight the importance of the position and the angle of the inclined bolts. The truss pattern with short span and wide angled inclined bolts (pattern

3) shows the best result. One reason is that the major area of the loosened rock is above the middle of the roof and this pattern has better coverage on this area compared to the other truss bolt patterns. On the other hand, pattern 1, which has a bigger span, has a small effect on the area above the middle of the roof but shows a good response on the areas near the corners. This is because in this pattern the inclined bolts are closer to the corners of the roof.

4.2 Stress Safety Margin (SSM)

The Mohr-Coulomb failure criterion is frequently used for modelling rock material (Jing 2003). In this criterion, if the Mohr's circle corresponding to the stress condition at a point in rock material touches the Mohr-Coulomb failure envelope, rock yields and the elastic solution is no longer valid. By increasing stress on the surrounding rock around an excavation, more points will undergo failure and the tunnel would collapse. The area beneath the failure envelope represents elastic behaviour of rock with no failure and can be considered as safe. The failure in Mohr-Coulomb failure criterion is a function of two key parameters: a) radius of Mohr's circle $(\sigma_1 - \sigma_3)/2$ and b) position of centre of the circle $(\sigma_1 + \sigma_3)/2$. Failure is happened by increasing radius of the circle or/and decreasing the amount of $\sigma_1 + \sigma_3$. Fig. 5 shows two possible Mohr's circles for these two paths of failure. It can be seen that the possibility of failure by decreasing radius of the circle is always more than failure by decreasing the amount of $\sigma_1 + \sigma_3$ ($x_c > x_r/\sin\phi$). Hence, the shortest distance to failure is x_r where x_r equal to zero represents failure. Now the stress safety margin can be defined based on this parameter. The mathematical expression for x_r can be derived as (Ghabraie et al 2008)

$$x_r = c \cos(\phi) + \left(\frac{\sigma_1 + \sigma_3}{2}\right) \sin(\phi) - \left(\frac{\sigma_1 - \sigma_3}{2}\right) \quad (3)$$

Using a dimensionless expression of this factor makes it easier to compare the results of several models. This will be achieved by the following equation

$$\text{SSM} = \frac{r + x_r}{r} \quad (4)$$

In this equation, SSM equal to one represents failure and plastic behaviour of rock while SSM greater than one means elastic behaviour of rock and safe Mohr's circle. Figs. 6 to 8 show contours of SSM difference before and after installing the three truss bolt patterns around a tunnel under hydrostatic stress distribution ($\text{SSM}_{\text{before}} - \text{SSM}_{\text{after}}$). By this definition, negative values represent areas in which truss bolt has favourable effect. The green line in these graphs shows the line in

1 which truss bolt does not have any significant effect on
 2 the value of SSM around the tunnel. This line demon-
 3 strates the border of favourable and unfavourable ef-
 4 fects of truss bolt. It can be seen that truss bolt effec-
 5 tively increases the value of SSM around the roof and
 6 abutments of tunnel.
 7

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 9 Comparing the three truss bolt patterns reveals that
 10 short tie-rod, wide angle of inclination and long inclined
 11 bolts (pattern 3) results in better effect on the area
 12 above the roof but less favourable effect on the rib area.
 13 On the other hand, in patterns 1 and 2, the most effec-
 14 tive areas around truss bolt are near inclined bolts. This
 15 makes truss bolt patterns 1 and 2 capable of reinforcing
 16 the area above the walls of the excavation (rib area).
 17 The length of inclined bolts, in current design schemes,
 18 is a function of the required load carrying capacity of
 19 the reinforcement systems. Inclined bolts should be long
 20 enough to ensure sufficient length of anchorage in the
 21 safe area (behind the rib line) to provide enough ca-
 22 pacity to the truss bolt system (Cox 2003; Liu et al
 23 2005). Figs. 6 to 8 show that the length of inclined bolts
 24 even changes the load distribution around the truss bolt
 25 where long inclined bolts (Fig. 8), in comparison with
 26 short inclined bolts (Figs. 6 and 7), are not able to pro-
 27 duce a highly reinforced area around inclined members.
 28 On the other hand, failure in providing enough length
 29 of anchorage results in failure of the truss bolt system.
 30 Consequently, the required length of anchorage to carry
 31 the applied load on truss bolt system can be always used
 32 to find the lower limit for the length of inclined bolts
 33 while this length can be adjusted with respect to the
 34 required amount of reinforcing effect near corners of the
 35 roof.
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39 Fig. 9 shows a different illustration of effects of pat-
 40 tern 3 on SSM around the tunnel. Contour lines in this
 41 figure have been chosen to represent three different ar-
 42 eas, namely, major reinforced area (less than -0.03),
 43 minor reinforced area (between -0.03 and 0) and un-
 44 favourable area (greater than 0). It can be seen that
 45 the major reinforced area approximately fits in an arch
 46 shape above the roof while the minor reinforced area
 47 is more like a trapezoid area which is located above
 48 the roof and between the inclined bolts. In other pat-
 49 terns the major reinforced area can be seen around the
 50 inclined members (Figs. 6 and 7). However, load dis-
 51 tribution around these patterns also shows arch shape
 52 borders. The applied horizontal tension at tie-rod can
 53 be well transferred to the rock at blocking points and by
 54 lateral behaviour of inclined bolts. This load produces
 55 an arch shape compressive area above the roof. The re-
 56 inforced areas in Figs. 6 to 9 match the compressive
 57 areas of Fig. 2.
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On the other hand, the horizontal tension in the
 tie-rod places the area behind inclined bolts in tension.
 This unfavourable area is mostly located on sides of
 the tunnel and can cause stability problems, especially
 when the side rock is relatively weak. In this case, in-
 stalling truss bolt can shear the side rock which causes
 rock sliding in this area. Individual rock bolts can be
 used to stabilise this area.

4.3 Cutter Roof

Cutter roof failure happens when shear cracks around
 the corners of the roof propagate towards the immedi-
 ate roof layer and reach a plane of weakness, resulting
 in separation of a massive unstable block (Su and Peng
 1987). This separation applies a huge load on the rein-
 forcement system that usually exceeds the load carry-
 ing ability of regular systems and the whole block drops
 into the excavated area. In some cases, re-opening and
 stabilizing a site after cutter roof failure has no efficient
 solution and the site would be abandoned (Su and Peng
 1987). Various researchers had done field investigations
 and modellings to understand the mechanism of cutter
 roof failure (Su and Peng 1987; Altounyan and Taljaard
 2001; Gadde and Peng 2005; Coggan et al 2012). In
 these works the main controlling parameters for cutter
 roof failure are mentioned as entry width, in-situ stress
 condition, propagation of shear cracks, relative stiff-
 ness between immediate roof layer and coal, geological
 anomalies, separation of bedding, horizontal movement
 of rock layers and gas pressure. The mechanism of truss
 bolt on preventing cutter roof failure can be studied by
 monitoring horizontal movement of the immediate roof
 layer and shear crack propagation in models under high
 horizontal or vertical in-situ stresses.

4.3.1 Slip on the First Bedding Plane

In numerical modelling, slip on the first bedding plane
 can be determined by monitoring the relative displace-
 ment of bedding surfaces. This parameter can be in-
 terpreted as the relative horizontal movement of the
 immediate rock layer.

Figs. 10 and 11 show the relative horizontal dis-
 placement between surfaces of the first bedding plane
 before and after installing truss bolt on two different
 in-situ stress distributions (high vertical $\sigma_v = 2\sigma_h$ and
 high horizontal $\sigma_v = 1/2\sigma_h$ stresses). These figures
 show that the truss bolt reduces the amount of hori-
 zontal movement in the immediate rock layer in both
 models.

A closer look at Fig. 10 reveals that, in high verti-
 cal in-situ stress the major area of slip before installing

truss bolt is approximately located above the roof. This slippage approaches zero near the rib area (radial distance of 2 m). After installing different truss bolt patterns, pattern 3 shows the best response which is due to the location of the inclined bolts that pass through the major area of the slip. By increasing the length of the tie-rod, the effectiveness of truss bolt reduces dramatically and pattern 1 shows small effect on this factor.

In contrast, when the horizontal in-situ stress is high, the slippage on the first bedding plane reaches a peak above the roof and extends to almost 1.5 times of the span of the opening (radial distance of 4 m) and smoothly approaches zero after this distance (Fig. 11). To prevent the cutter roof failure, horizontal displacement, especially above and behind the rib area, need to be controlled. Fig. 11 shows that for the area above the tunnel short span truss bolt has the best effect (similar to results of high vertical in-situ stress, Fig. 10). However, for the area around corners of the roof (radial distance of 2 m) pattern 2 shows the best results. In this area pattern 1 and 2 are more successful than pattern 3 due to having inclined bolts passing through this area. Also, angle of inclined bolts in pattern 2 is another reason for effective application of this pattern where 45° inclined bolts produce a larger horizontal component than 60° for the same amount of pretension. This component is in the opposite direction to the horizontal in-situ stress and reduces the effect of this stress.

4.3.2 Shear Crack Propagation

One of the main limitations of FEM is in modelling fracture growth (Jing 2003). Capturing crack propagation is only possible by employing relatively new methods such as enriched FEM and generalized FEM (Duarte et al 2000; Deb and Das 2011). Using these techniques in a comprehensive model of underground excavation with complex geometry involves significant computational costs. This problem becomes more complicated when the model contains pretensioned elements (rock bolts) and geological features such as bedding planes.

Based on the Mohr-Coulomb failure criterion, shear failure can happen under compressive stresses when the maximum shear stress reaches the critical value defined by the Mohr-Coulomb yield function. After shear failure the rock behaviour could be assumed to be plastic. This failure could thus be captured using an elastic-plastic material model in FEA. Hence the yielded areas resulted from elastic-plastic FEA, provided that the stresses are compressive, could be assumed to represent the shear crack propagation. However, if the failure occurs in tension, due to the separation in material, the

post failure behaviour could not be captured appropriately using an elastic-plastic FEA.

To monitor the effects of truss bolt on cutter roof, progressive failure (shear crack propagation) around the tunnel is modelled using a simplified interactive approach. For this purpose, the model is solved with elastic-plastic material model once and then the most likely area to yield is found with respect to the Mohr-Coulomb yield function and SSM factor (Eq. 4).

As discussed in Section 4.2 changes in radius of Mohr's circle is always smaller than the required change in the amount of pressure to satisfy the failure criterion ($x_r < x_c$). From Eq. 4, SSM equal to one ($x_r = 0$) denotes failure (Fig. 5). Increasing load in rock material results in changing the radius of Mohr's circle and causes an increase in the number of failure points in rock. Modelling this progressive failure in rock is possible by gradually increasing values of x_r and finding the yielded points for the new stress condition corresponding to the new x_r . This approach is essentially a linear extrapolation which helps us estimate shear crack propagation.

The increase in the amount of x_r can be defined through several increments (I_n) where

$$\text{SSM} - 1 = I_n \quad (5)$$

In this equation $\text{SSM} = 1$ represents yielding. By replacing the definition of SSM in Eq. 5, different increments can be derived as

$$I_n = \frac{x_r}{r} \quad (6)$$

This equation identifies the locations where rock will undergo shear failure at increment I_n . I_n equal to zero interprets $x_r = 0$ which shows the area of the failure under current loading condition. Increasing the amount of I_n shows propagation of yielded as loads increase. It should be noted that the resulting yielded areas for different increments do not necessarily mean that these areas are yielded but shows the pattern of potentially yielded area (shear cracked area) in different time spans after excavation.

With respect to the definition of cutter roof by (Su and Peng 1987), when shear cracks reach the plane of weakness, cutter roof happens. Four different increments have been chosen to represent the shear cracks just after excavation ($I_n = 0$) to cutter roof failure (when shear cracks reach the plane of weakness). Two different in-situ stress distributions have been modelled. Results showed that when the horizontal in-situ stress is high ($\sigma_v = 1/2\sigma_h$) shear cracks tend to propagate with a sharp angle to the roof of the opening. Various markers in Fig. 12 show yielded points for different increments. Different increments are shown by different colours. The hypothetical lines in this figure show

1 the areas of yielded rock for different increments. As it
2 can be seen, at the final increment ($I_n = 0.015$) shear
3 cracks reach the plane of weakness and the cutter roof
4 happens. Similarly, using the same method for a tun-
5 nel under high vertical in-situ stress ($\sigma_v = 2\sigma_h$), the
6 pattern of shear crack propagation can be obtained as
7 shown in Fig. 13. Comparing these two figures illus-
8 trates that the angle of shear crack propagation and
9 shape of the unstable block is deeply related to the con-
10 dition of the in-situ stress. In high vertical in-situ stress,
11 shear cracks propagate at an approximately right angle
12 to the roof while in high horizontal in-situ stress this
13 angle is less than 90° . Su and Peng (1987) on the ba-
14 sis of numerical analysis, using FEA and safety factor,
15 together with field observations reported the same pat-
16 tern of cutter roof in high vertical and horizontal in-situ
17 stress conditions.

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20 Figs. 14 to 19 show results of installing three differ-
21 ent truss bolt patterns on two identical tunnels under
22 high horizontal and vertical in-situ stresses. Compar-
23 ing these results with Fig. 12 and 13 (pattern of shear
24 cracks before installing truss bolt), it can be concluded
25 that truss bolt system reduces the possibility of cut-
26 ter roof by controlling shear crack propagation. It ap-
27 pears that truss bolt system by having inclined bolts
28 near the area of initial shear cracks (around the cor-
29 ners of the roof) prevents continuous cracking and re-
30 duces the possibility of cutter roof. It has been shown
31 in Section 4.2 that, because of the pretension force and
32 induced compressive stress around the inclined bolts,
33 a reinforced area will be created near the corners of
34 the roof. In high vertical in-situ stress, where inclined
35 bolts are well located at the area of shear crack propa-
36 gation, the applied compressive stress by inclined bolts
37 prevents continues shear crack propagation. In addition
38 to this, investigating the results of SSM factor around
39 truss bolt system shows another major reinforced area
40 which is similar to an arch shape between inclined bolts
41 above the roof (Fig. 9). Comparing patterns of shear
42 cracks before (Fig. 12) and after installing truss bolt
43 (Figs. 14 to 16) in high horizontal in-situ stress shows
44 that truss bolt prevents propagation of cracks at areas
45 near blocking points and above the roof. In fact, this
46 area is identical to the produced reinforced arch area
47 by truss bolt.

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51 Results of installing different truss bolt patterns on
52 preventing cutter roof illustrate that, depending on de-
53 sign parameters of truss bolt and in-situ stress distri-
54 bution, effectiveness of the system on preventing shear
55 crack propagation varies. It can be seen that in high ver-
56 tical in-situ stress, pattern 2 shows the best application.
57 Inclined bolts in this pattern exactly pass through the
58 initial area of cracking and, by reinforcing this area, this

pattern prevents further crack propagation (Fig. 18).
Fig. 19 shows that pattern 3 is also able to reduce the
possibility of cutter roof in this in-situ stress condition.
On the other hand, inclined bolts in pattern 1 are lo-
cated behind the area of initial cracking and even push
the crack propagation pattern slightly towards the mid-
dle of the roof instead of controlling it (Fig. 17).

Comparing results of installing different truss bolts
on a tunnel under high horizontal in-situ stress shows
that patterns 2 and 3 prevent shear crack propagation
to reach the plane of weakness. Whilst pattern 1 does
not have any significant effect on preventing cutter roof
and shear cracks reach the plane of weakness around
the middle of the roof. This is probably because of the
position of inclined bolts in pattern 1 which, similar
to Fig. 17 in high vertical in-situ stress, is located be-
hind the area of initial crack propagation. As discussed
in Section 4.2, pattern 3 by having long inclined bolts
and short tie-rod length produces a stronger reinforced
arch compared to other patterns. This enables it to ef-
fectively control the shear crack propagation above the
roof and shows the best response.

5 Discussion

The importance of a comprehensive consideration of all
the design parameters and site variables can be con-
cluded here. It has been shown that the shorter length
of inclined bolts produce better reinforced area around
the inclined bolts compared to longer bolts. If a truss
bolt system with short inclined bolts is located in the
right place to prevent crack propagation in high verti-
cal in-situ stress (by choosing suitable tie-rod length),
it can effectively prevent the cutter roof failure. On the
other hand, longer inclined bolts have the advantage
of adequate length of anchorage in passive zone behind
the rib line. The length of anchorage is a key parameter
to determine the capacity of the system. If the applied
load on truss bolt system exceeds the capacity of truss
bolt, the whole block with truss bolt will fail.

The length, position and angle of inclined bolts are
also important in controlling horizontal movement and
the area of the loosened rock. If inclined bolts pass
through the major area of slip (depending on the in-situ
stress distribution), the capacity of the truss bolt for
preventing horizontal movement increases significantly.
The area of slip varies with the in-situ stress conditions.
Results showed that medium length tie-rod locates the
inclined bolts at the best possible location to prevent
slip on the first bedding plane in high horizontal in-situ
stress. Further to the importance of length of tie-rod
in truss bolt, choosing an angle closer to horizon would
result in producing higher resisting force against high

1 horizontal in-situ stresses. It should be mentioned that
2 bolt angles less than 45° will result in significant reduction
3 in the capability of truss bolt to control the area
4 above the roof. Reinforcing this area above the roof is
5 vital to prevent cutter roof failure when horizontal in-
6 situ stress is high. In contrast, the area of slip in high
7 vertical in-situ stress is mainly above the roof where
8 short length tie-rod shows the best response. Same as
9 the latter case, capability of this truss bolt pattern in
10 controlling crack propagation should be taken into account.
11 Truss bolt with medium length of tie-rod and
12 45° inclined bolts shows the best response in controlling
13 shear crack propagation in high vertical in-situ stress.
14

15 Studying the effects of installing truss bolt on the
16 position of natural roof arch also shows that changing
17 the design parameters of truss bolt would result in re-
18 inforcing different areas above the roof and corners of
19 the tunnel. These results match perfectly with results of
20 SSM factor where short span truss bolt with wide angle
21 inclined bolts are able to reinforce the area above the
22 roof. By increasing the length of tie-rod and decreasing
23 the length of inclined bolts, the main area of reinforcing
24 effect of truss bolt shifts from an area above the middle
25 of the roof to the area around inclined bolts.
26

27 It has been shown that, impact of truss bolt sys-
28 tem changes with respect to the condition of the in-
29 situ stress distribution. There are many other geolog-
30 ical features that might have significant influence on
31 the practice of truss bolt systems, such as thickness of
32 the rock layers, strength parameters of rock, condition
33 of discontinuities, time factor, etc. (Neall et al 1978).
34 Consequently, it can be concluded that obtaining an
35 optimum design for truss bolt systems entails consid-
36 eration of effects of each individual design parameter
37 alongside with comprehensive study of all of the exter-
38 nal geological and ground controlling parameters.
39

40 6 Conclusion

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44 Truss bolt systems have proved effective in control-
45 ling the stability of underground excavations in severe
46 ground conditions particularly in coal mines and lay-
47 ered strata. Despite this, knowing the mechanism of
48 truss bolt systems on reinforcing underground excava-
49 tions is vital. The objective of this study was to un-
50 derstand the mechanism of truss bolt by means of nu-
51 merical modelling. To evaluate and monitor the effects
52 of truss bolt on load distribution around the tunnel
53 and understand the mechanism of reinforcement, sev-
54 eral stability indicators have been introduced. These
55 indicators cover several features of a reinforcement sys-
56 tem and are, namely, area of the loosened rock above
57 the roof, stress safety margin, slip on the first bedding
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plane and shear crack propagation. None of these in-
dicators alone is able to determine the stability of an
underground excavation, but together, they help to un-
derstand the effects and mechanism of truss bolt sys-
tem.

Results of employing these stability indicators re-
veal that truss bolt systems stabilize underground ex-
cavations in several ways such as repositioning the nat-
ural reinforced arch and reducing the area of loosened
rock above the roof, creating a trapezoid reinforced area
in which an arch shape structure is the major rein-
forced area, reducing horizontal movement of rock lay-
ers, preventing shear crack propagation, and decreasing
the chance of cutter roof failure. Results of studying
several truss bolt patterns also showed that changing
the design parameters of the truss bolt will change the
effectiveness of the system in facing different stability
problems. Parameters such as angle and length of the
inclined bolts and the span of the system or length of
the tie-rod have been changed and results have been
studied. It has shown that to reinforce the loosened
area beneath the natural arch a short span truss bolt
with wide angle inclined bolts is more appropriate while
in high horizontal in-situ stress, to prevent horizontal
movement of the immediate layer, a wider span and
sharper angle of inclination response better. In case of
cutter roof failure, to prevent shear crack propagation
in high vertical in-situ stress, a pattern with medium
length of tie-rod and inclined bolts and 45° inclined
bolts results in the best application whilst other pat-
terns do not show considerable improvement.

Results have showed that obtaining an optimum,
safe and efficient design of a truss bolt system is only
possible by considering all the design parameters, site
variables and the interacting effects of each parameter
on the other. This study has provided the necessary
understanding of the mechanism of truss bolt which is
an important step towards achieving a comprehensive
guideline to design a truss bolt pattern.

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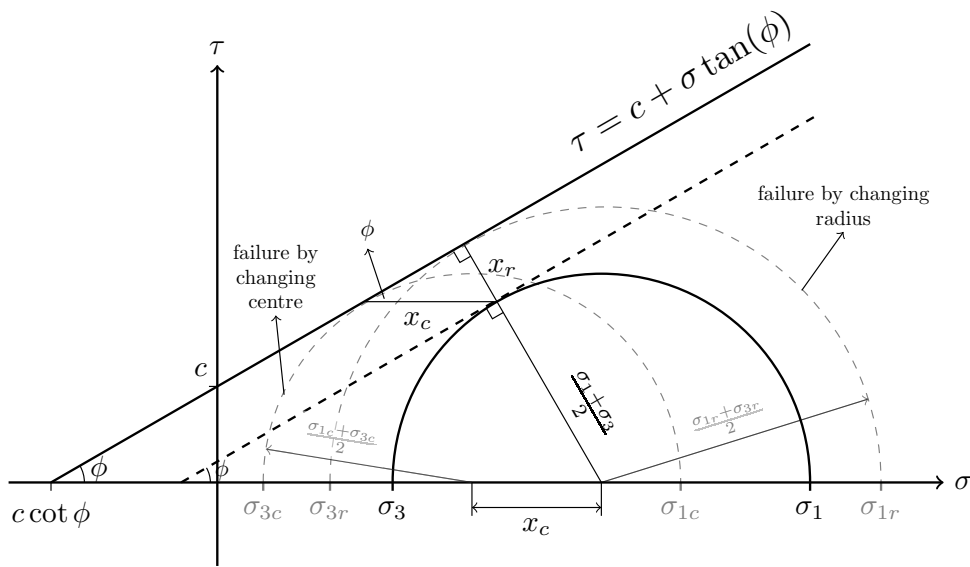


Fig. 5 Two possible paths of failure in Mohr-Coulomb failure model

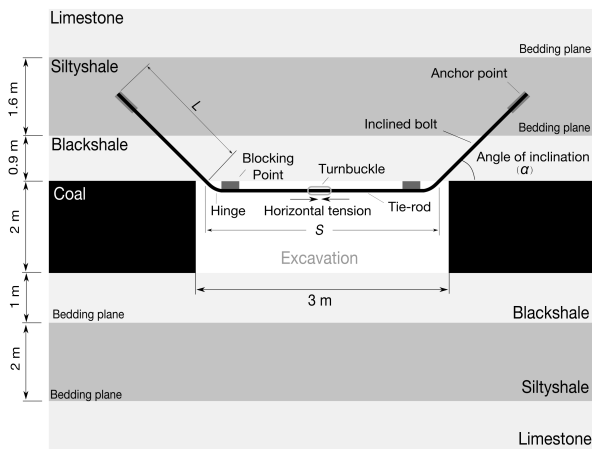


Fig. 1 Schematic view of truss bolt, tunnel and model dimensions

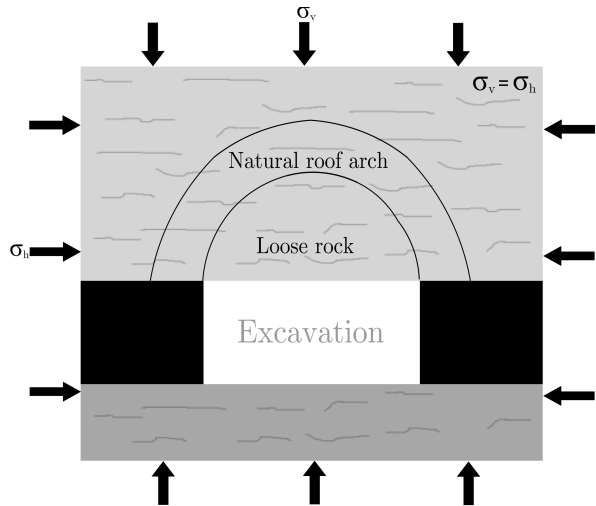


Fig. 3 Natural arch and loosened area

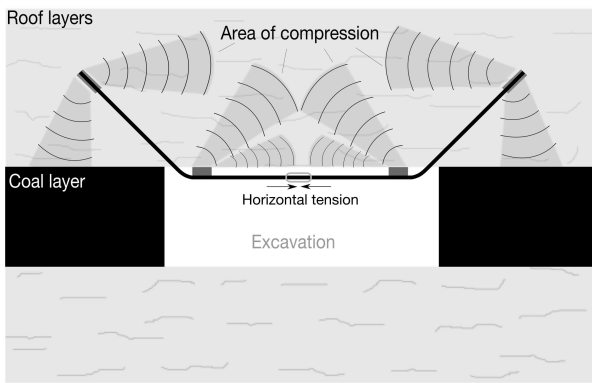


Fig. 2 Compressive areas around truss bolt

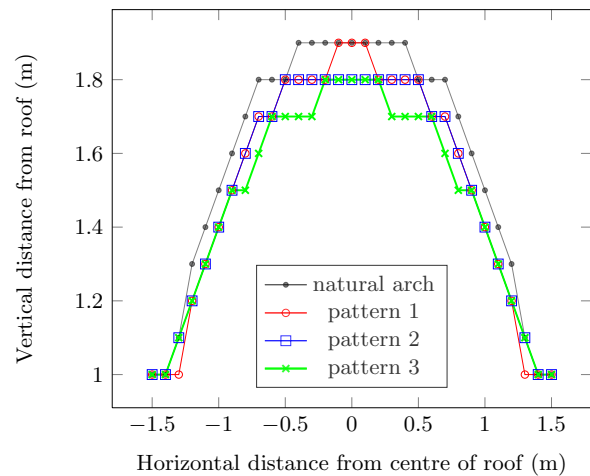


Fig. 4 Reinforced arch after installing truss bolt patterns

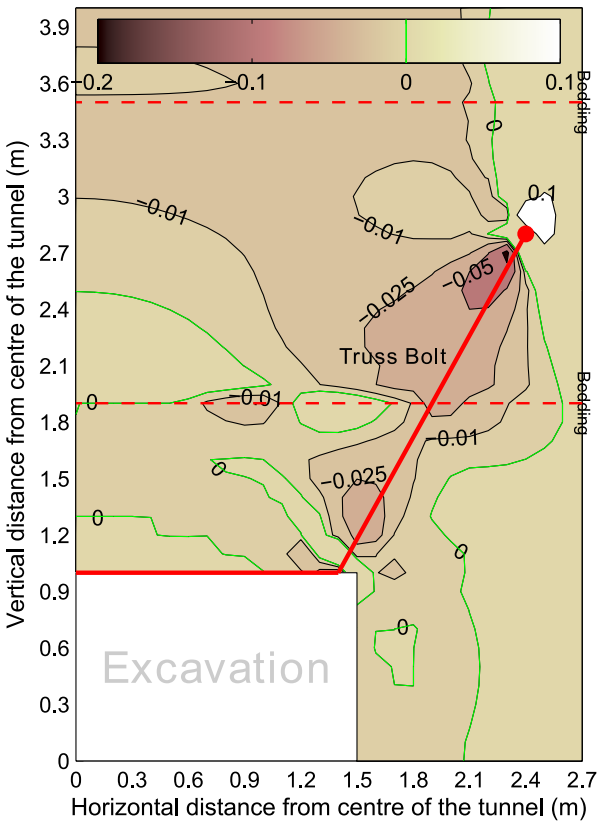


Fig. 6 Effect of pattern 1 on SSM

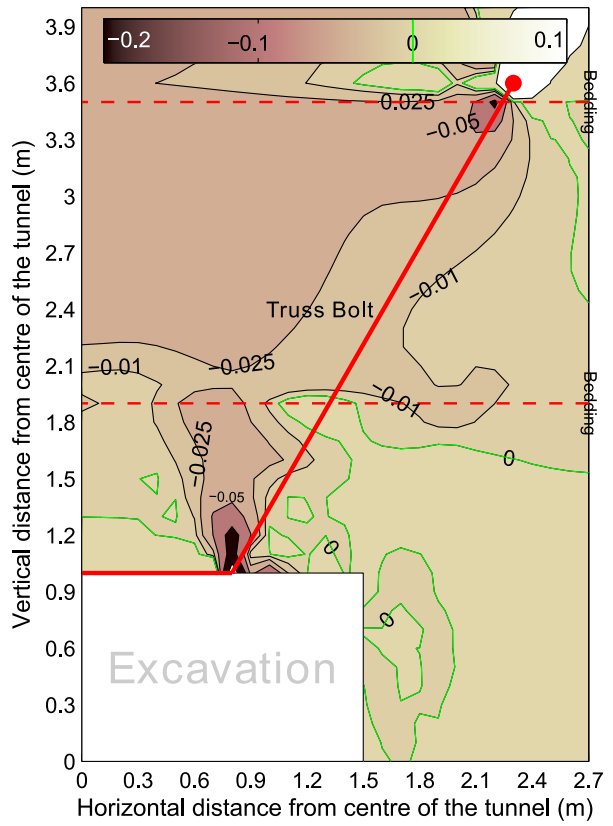


Fig. 8 Effect of pattern 3 on SSM

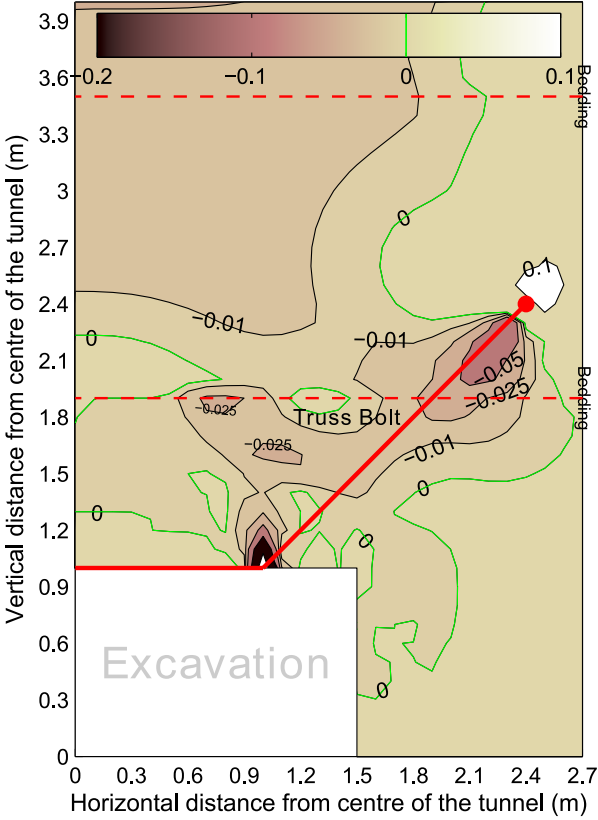


Fig. 7 Effect of pattern 2 on SSM

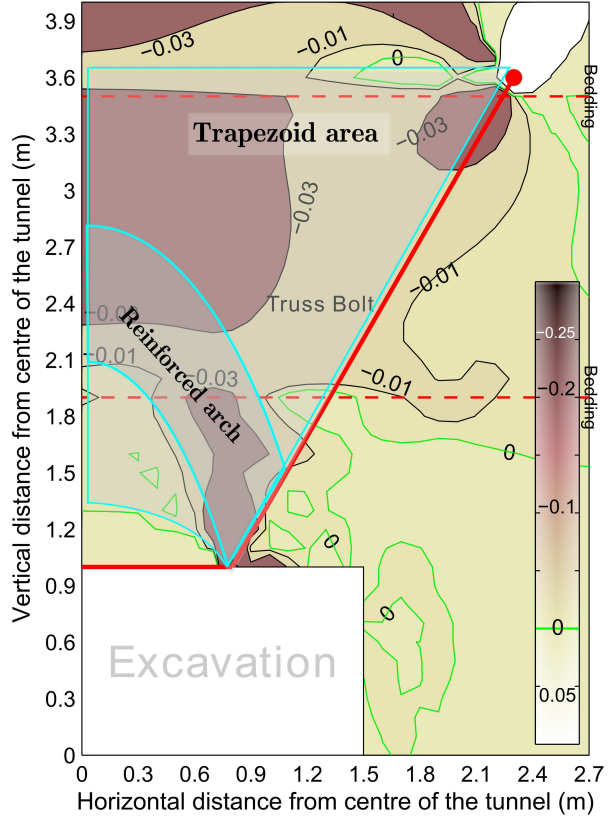


Fig. 9 Different reinforced areas around pattern 3

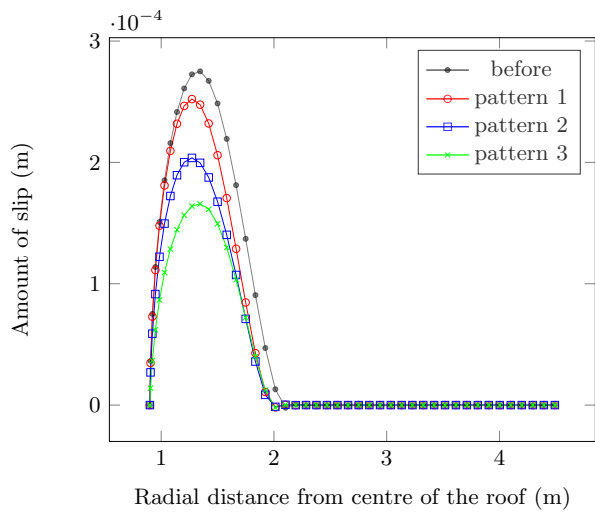


Fig. 10 Amount of slip on the first bedding plane ($\sigma_v = 2\sigma_h$)

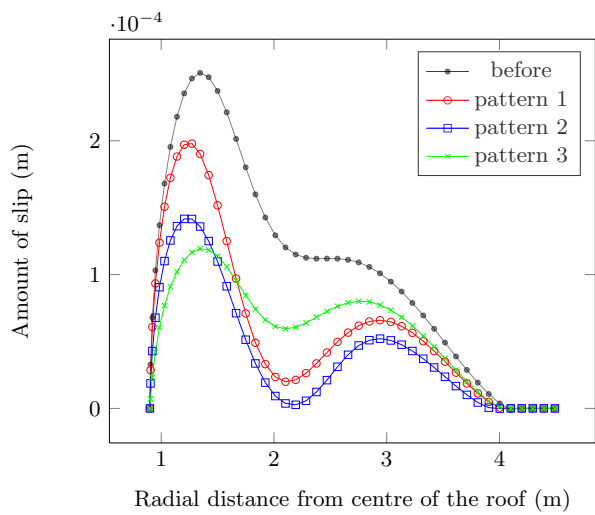


Fig. 11 Amount of slip on the first bedding plane ($\sigma_v = 1/2\sigma_h$)

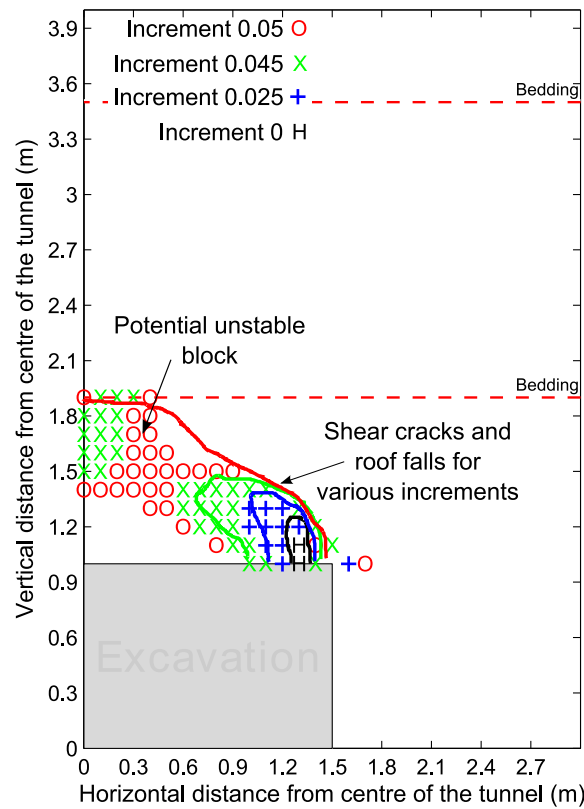


Fig. 12 Pattern of shear crack propagation ($\sigma_v = 1/2\sigma_h$)

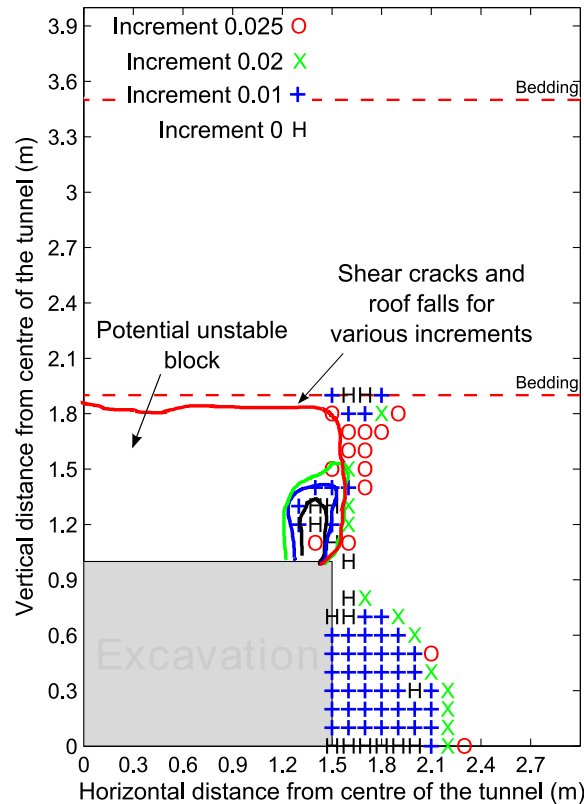


Fig. 13 Pattern of shear crack propagation ($\sigma_v = 2\sigma_h$)

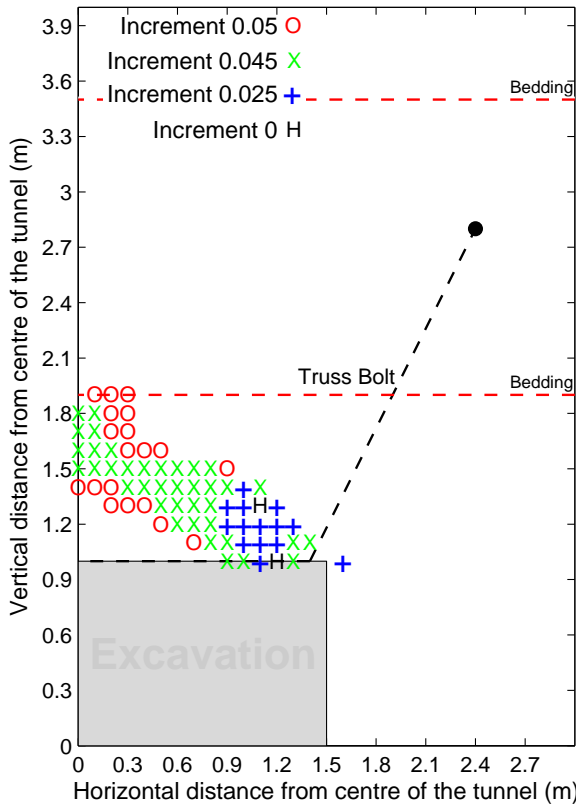


Fig. 14 Pattern of shear crack around pattern 1 ($\sigma_v = 1/2\sigma_h$)

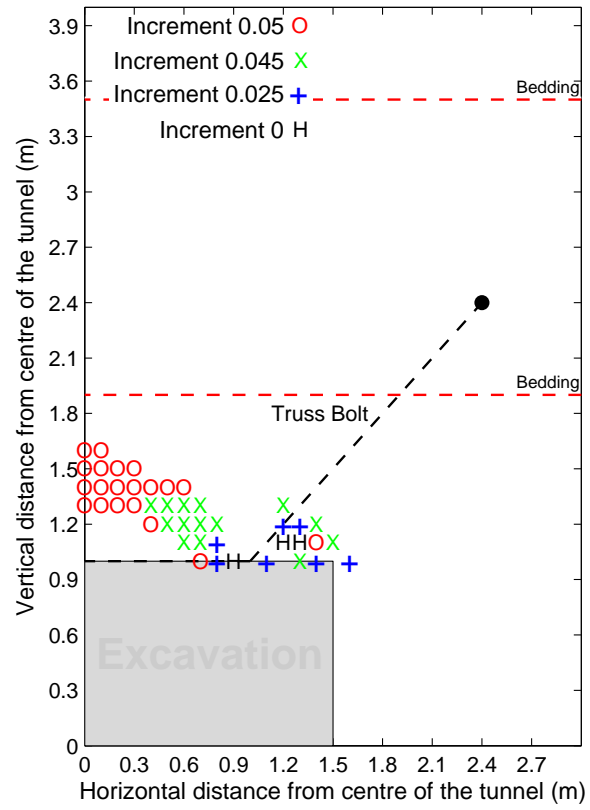


Fig. 15 Pattern of shear crack around pattern 2 ($\sigma_v = 1/2\sigma_h$)

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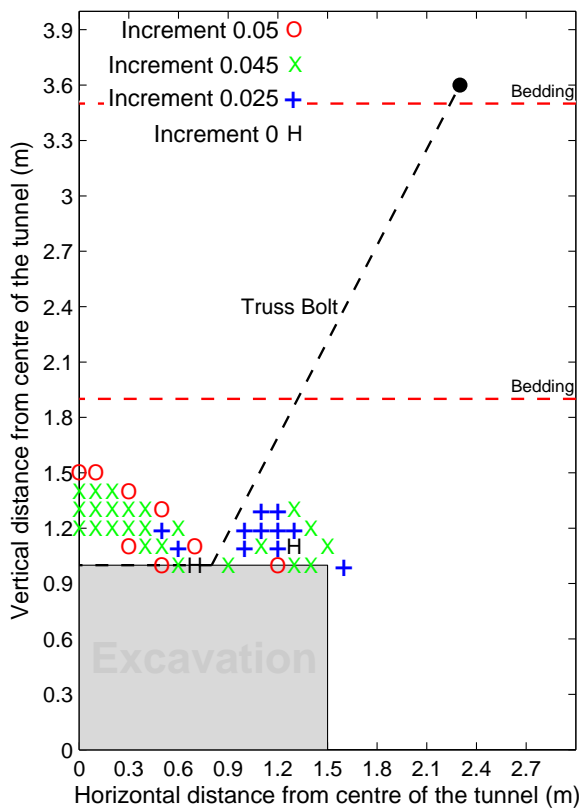


Fig. 16 Pattern of shear crack around pattern 3 ($\sigma_v = 1/2\sigma_h$)

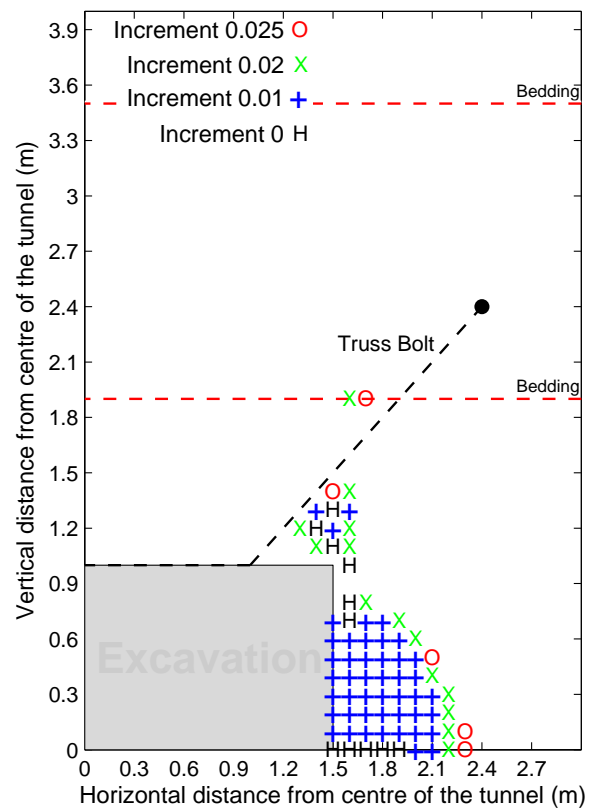


Fig. 18 Pattern of shear crack around pattern 2 ($\sigma_v = 2\sigma_h$)

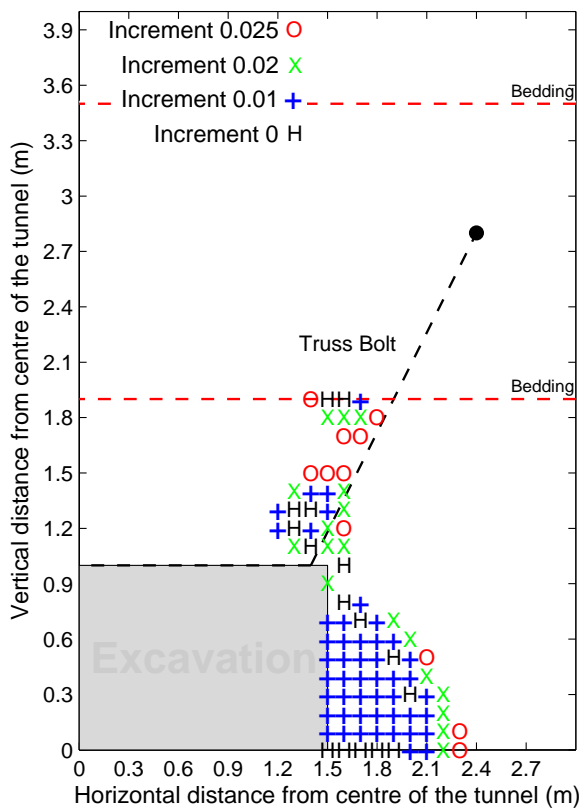


Fig. 17 Pattern of shear crack around pattern 1 ($\sigma_v = 2\sigma_h$)

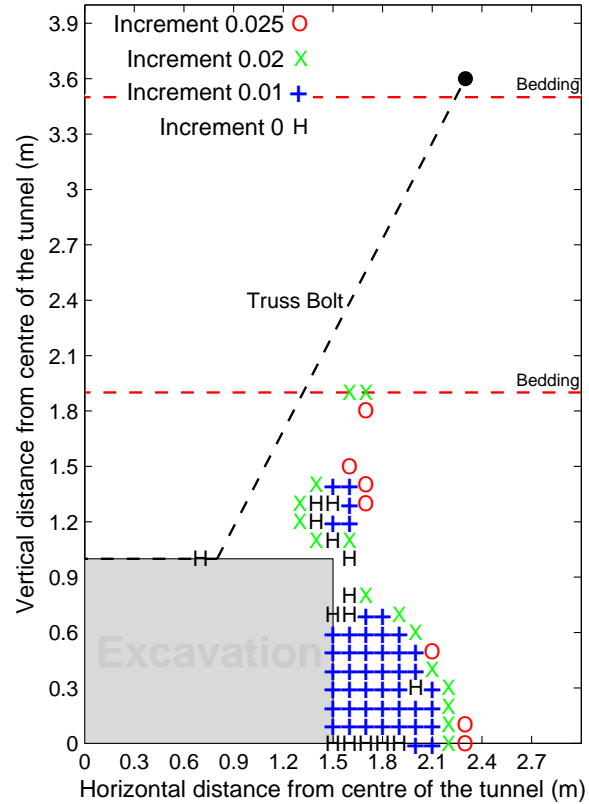


Fig. 19 Pattern of shear crack around pattern 3 ($\sigma_v = 2\sigma_h$)

Table 1 Bolt strength properties

| Bolt properties | |
|---------------------------|---------------------|
| Cross-sectional area | 313 mm ² |
| Module of elasticity | 200 Gpa |
| Ultimate tensile strength | 1670 Mpa |
| Mass per meter-cable | 2.482 kg/m |

Table 2 Three different truss bolt patterns (see Fig. 1)

| Truss bolt patterns | $L(m)$ | $S(m)$ | $\alpha(^{\circ})$ |
|---------------------------------|--------|--------|--------------------|
| Pattern 1 (Liu et al 2005) | 2 | 2.8 | 60 |
| Pattern 2 (Cox and Cox 1978) | 2 | 2 | 45 |
| Pattern 3 (Ghabraie et al 2012) | 3 | 1.6 | 60 |

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